



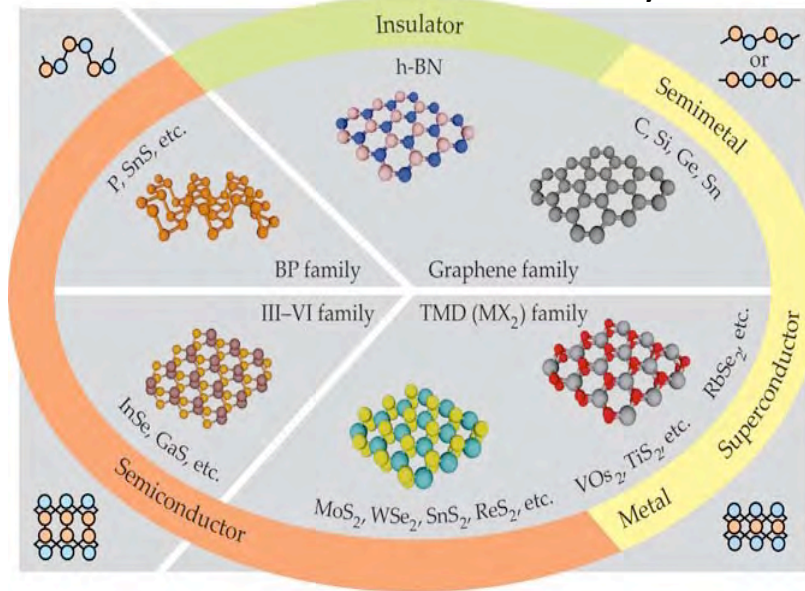
Moiré superlattice in van der Waals interface: Experimental opportunities and challenges

Philip Kim

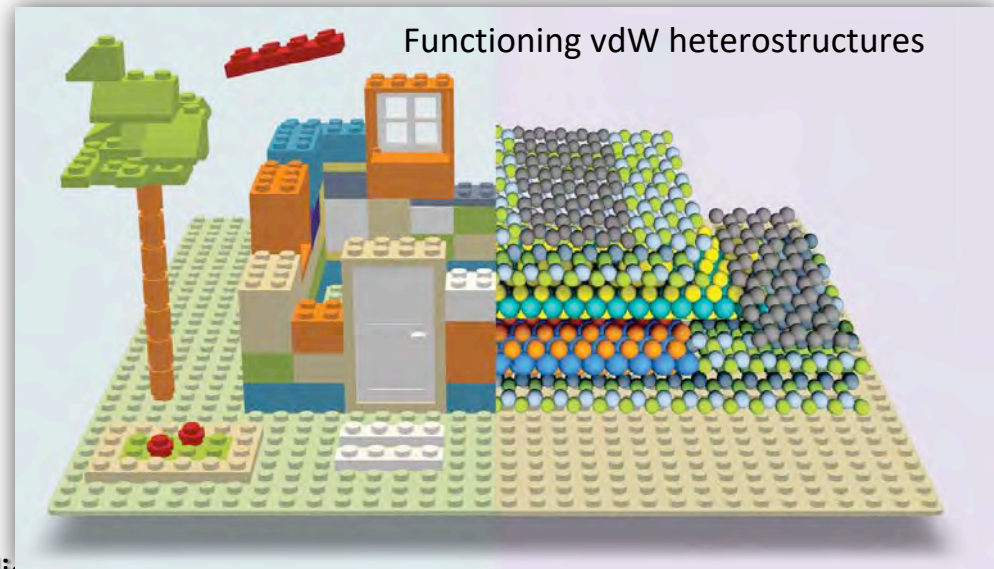
Department of Physics, Harvard University

Assembling van der Waals Materials

2D van der Waals Materials Family

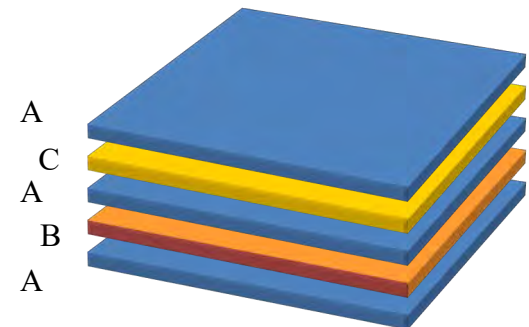


Ajayan, Kim and Banerjee, Physics Today (2016)

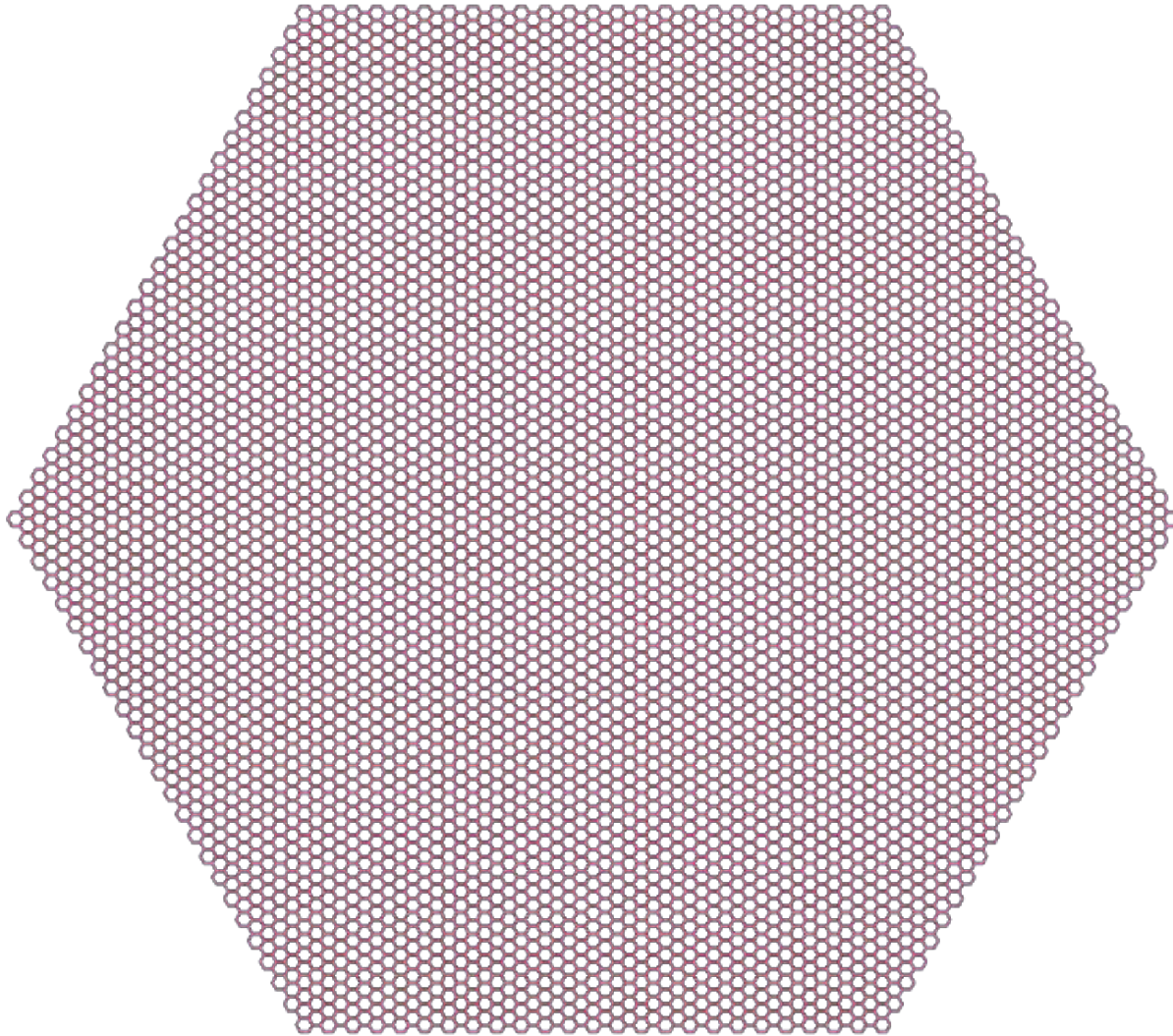


Experimentally popular vdW Materials (partial list)

- **Semiconducting materials:** WSe_2 , MoSe_2 , MoS_2 , WS_2 , BP...
- **Complex-metallic compounds :** TaSe_2 , TaS_2 , ...
- **Magnetic materials:** Fe-TaS_2 , CrSiTe_3 , CrI_3 ...
- **Superconducting:** NbSe_2 , $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8-x}$, ...
- **Topological Insulator/Weyl SM:** Bi_2Se_3 , MoTe_2



Moire Superlattice Engineering in van der Waals Interface

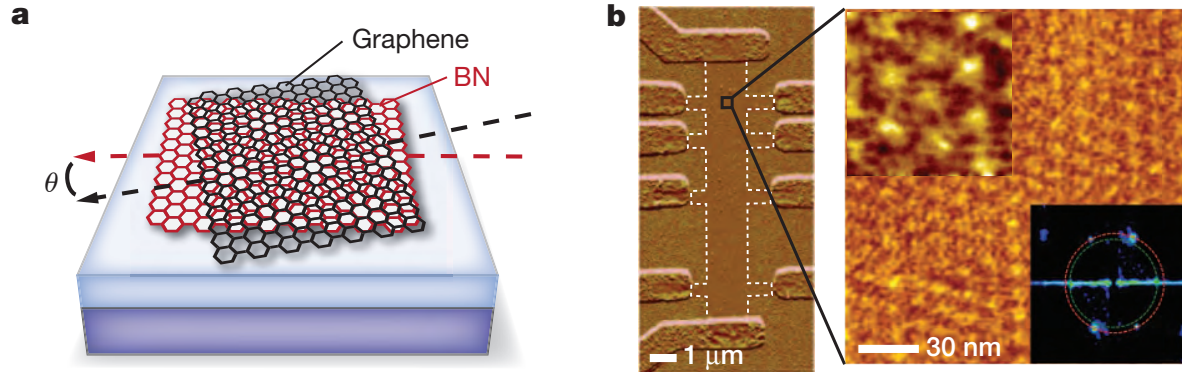


Twisted van der Waal interface of homo & hetero structure

Moire Superlattice Engineering in van der Waals Interface

Dean *et al.*, Nature (2013)

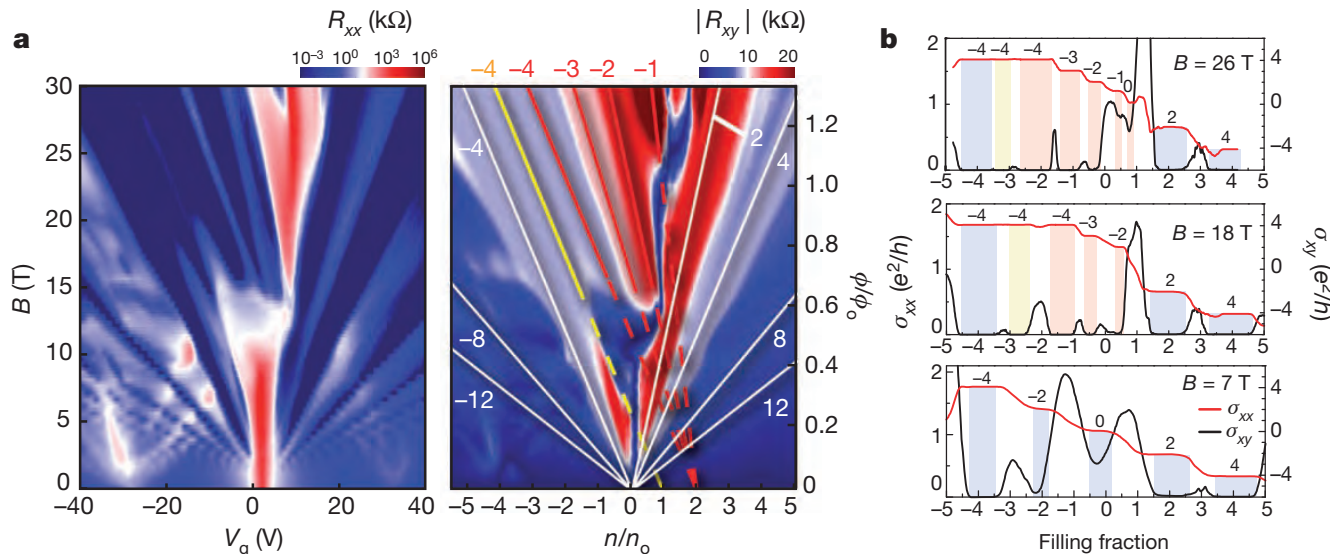
Graphene on hBN: moire superlattice



Moire wavelength:

$$\lambda = \frac{(1 + \delta)a}{\sqrt{2(1 + \delta)(1 - \cos(\phi)) + \delta^2}}$$

Hofstadter's butterfly spectrum and Fractal quantum Hall effect



See also

Ponomarenko *et al.*, Nature (2013)

Hunt *et al.*, Science (2013)

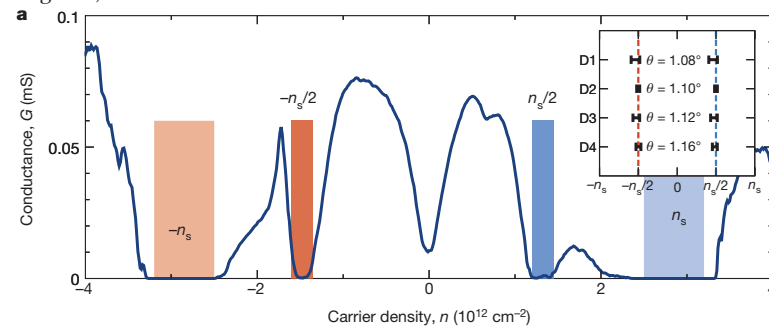
LETTER

doi:10.1038/nature26154

Correlated insulator behaviour at half-filling in magic-angle graphene superlattices

Yuan Cao¹, Valla Fatemi¹, Ahmet Demir¹, Shiang Fang², Spencer L. Tomarken¹, Jason Y. Luo¹, Javier D. Sanchez-Yamagishi², Kenji Watanabe³, Takashi Taniguchi³, Efthimios Kaxiras^{2,4}, Ray C. Ashoori¹ & Pablo Jarillo-Herrero¹

5 APRIL 2018 | VOL 556 | NATURE | 43

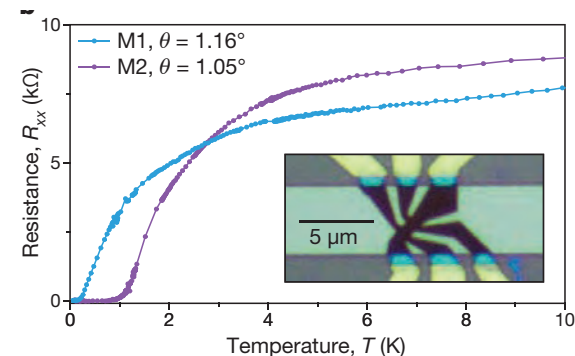


ARTICLE

doi:10.1038/nature26160

Unconventional superconductivity in magic-angle graphene superlattices

Yuan Cao¹, Valla Fatemi¹, Shiang Fang², Kenji Watanabe³, Takashi Taniguchi³, Efthimios Kaxiras^{2,4} & Pablo Jarillo-Herrero¹



Twistronics: 2D materials beyond Legoland

Correlated insulator

Cao et al., Nature 556, 80–84 (2018).

Burg et al., PRL 123, 197702 (2019).

Unconventional superconductivity

Cao et al., Nature 556, 43–50 (2018).

Yankowitz et al., Science 363, 1059–1064 (2019).

Lu et al., Nature 574, 653–657 (2019).

Magnetism and Quantum Anomalous Hall Effect

Sharpe et al., Science 365, 605–608 (2019).

Serlin et al., arXiv:1907.00261 (2019).

Trilayers double bilayers

Chen et al. Nature Physics 15, 237–241 (2019).

Chen et al., Nature 572, 215219 (2019). She et al., ArXiv 2019

Double bilayers

Shen et al., arXiv:1903.06952 (2019).

Liu et al., arXiv:1903.08130 (2019).

Cao et al., arXiv:1903.08596 (2019).

Adak et al., arXiv:2001.09916 (2020)

TMDC/TMDC

Tang et al. arXiv:1910.08673 (2019).

Regan et al., arXiv:1910.09047 (2019).

Wang et al., arXiv:1910.12147 (2019).

STM

Jiang et al., Nature 572 91-95 (2019).

Kerelsky et al., Nature 572 95-100 (2019).

Xie et al., Nature 572 101-105 (2019).

Scanning Probes

Cao et al., Nature 556, 43–50 (2018).

Yankowitz et al., Science 363, 1059–1064 (2019).

Lu et al., Nature 574, 653–657 (2019).

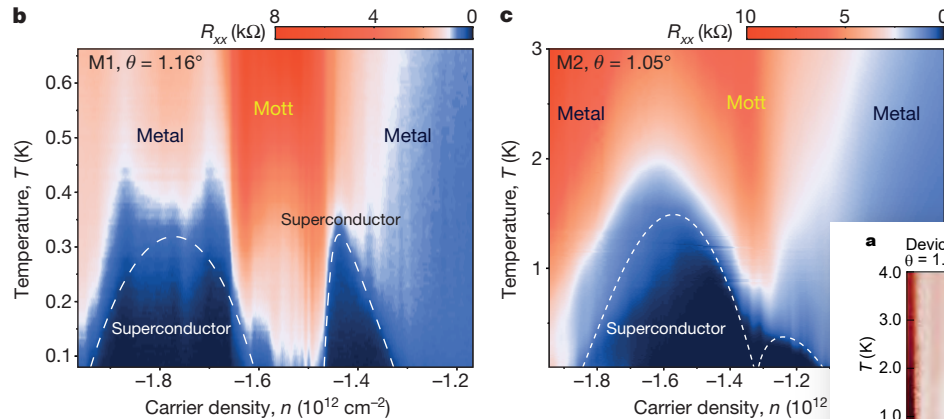
Optical Spectroscopy (excitons in moire)

Tran, K. et al. Nature 567, 71–75 (2019).

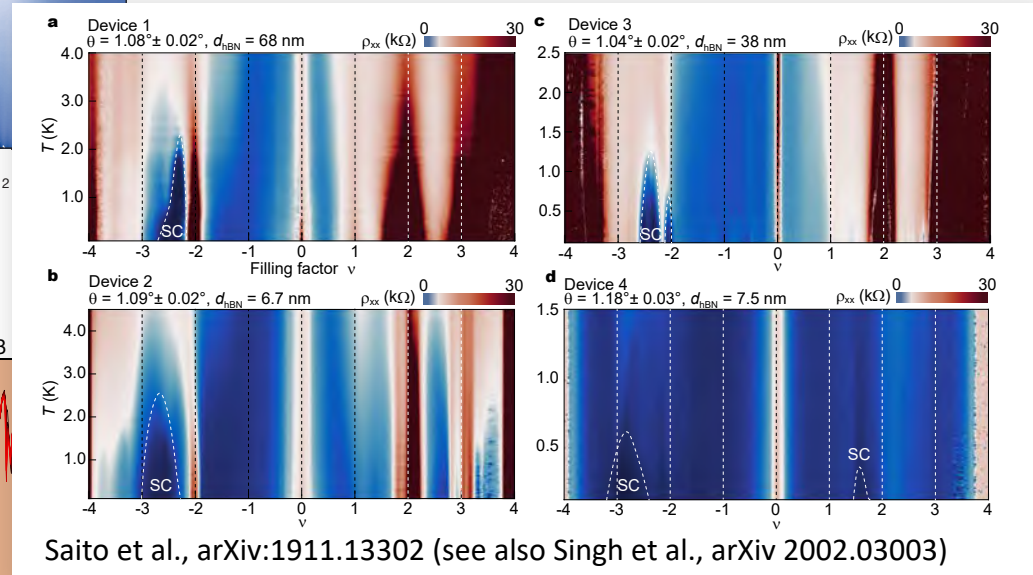
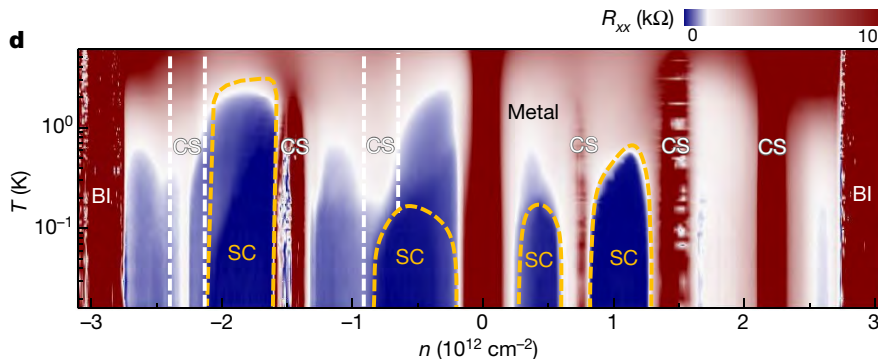
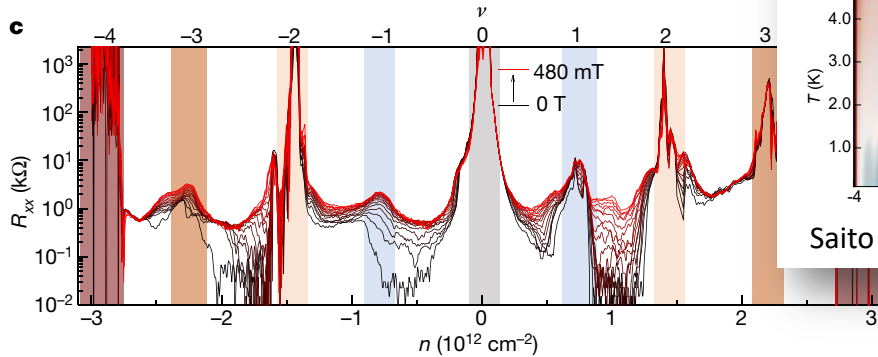
Seyler, K. L. et al. Nature 567, 66–70 (2019).

Jin, C. et al. Nature 567, 76–80 (2019).

Superconducting Phase Diagram for MA TBG



Cao et al., Nature 556, 43–50 (2018).



Saito et al., arXiv:1911.13302 (see also Singh et al., arXiv 2002.03003)

Lu et al, Nature 574, 653–657 (2019).

Local Variation of Twisting Angles

Scanning SQUID Measurement

Uri et al., arXiv:190804595 (2019)

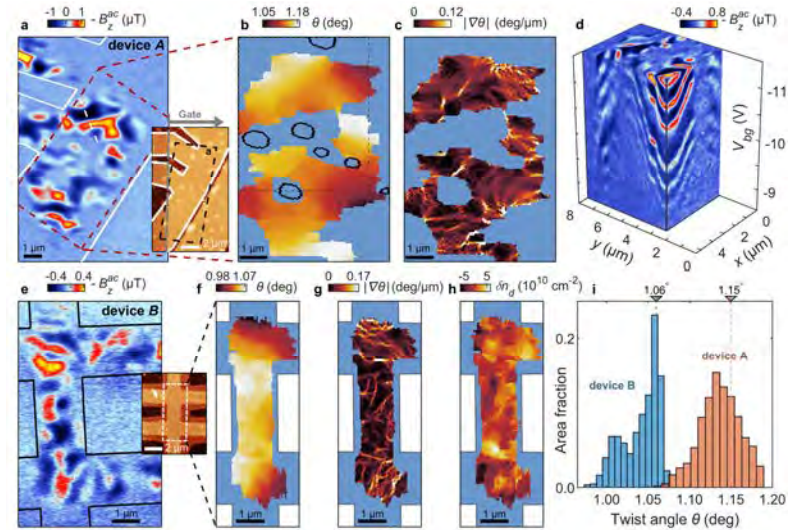
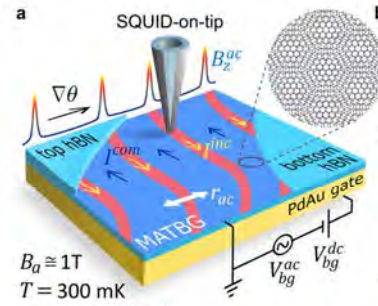
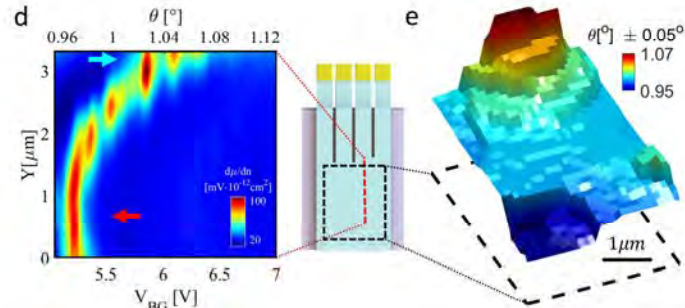
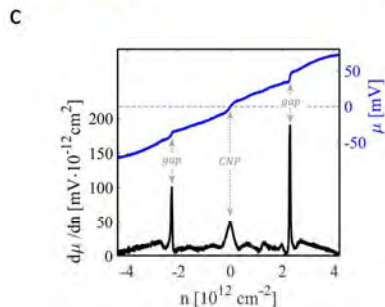
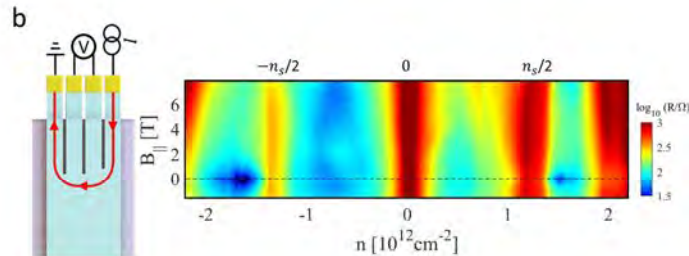
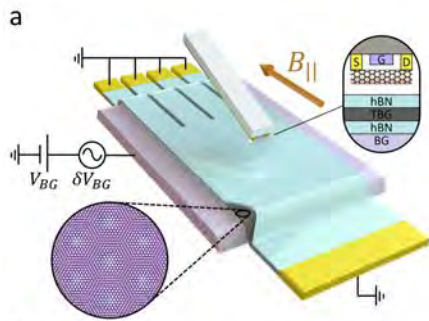


Fig. 3. Mapping the twist angle and Landau levels in MATBG. (a) B_z^{ac} image of the dashed area in the

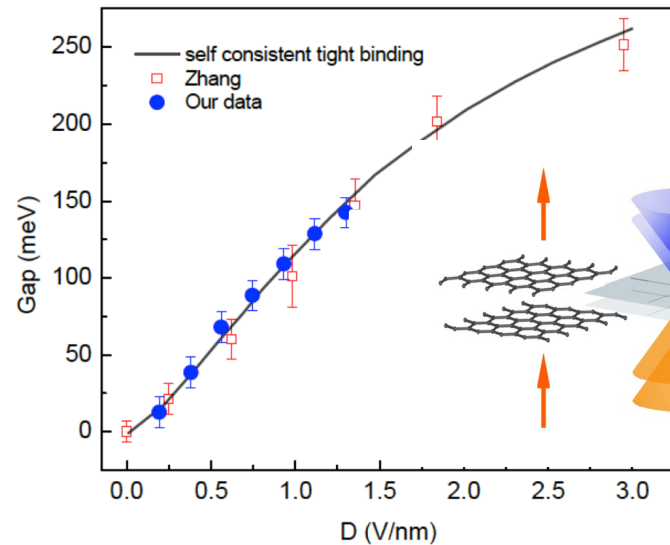
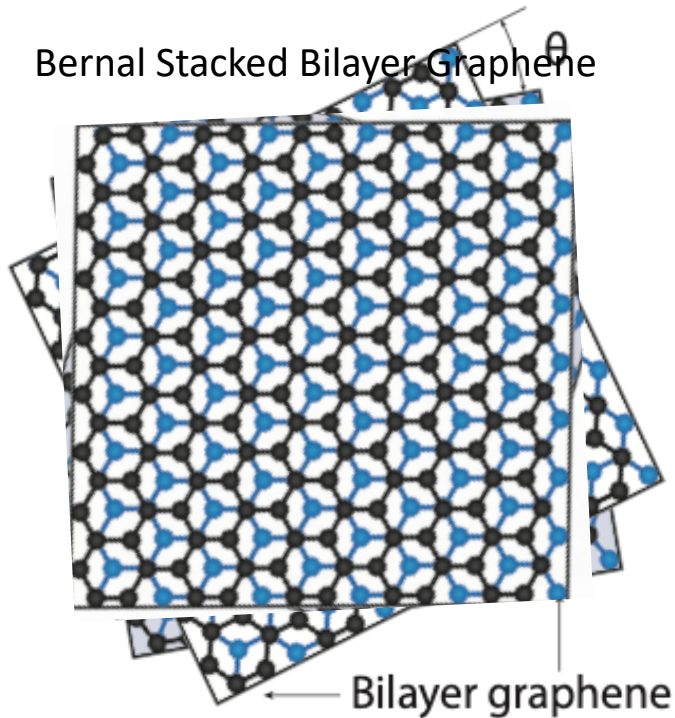


Scanning nanotube SET

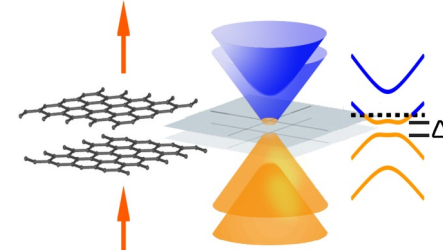
Zondiner et al., arXiv:191206150 (2019)

Twisted Double Bilayer Graphene

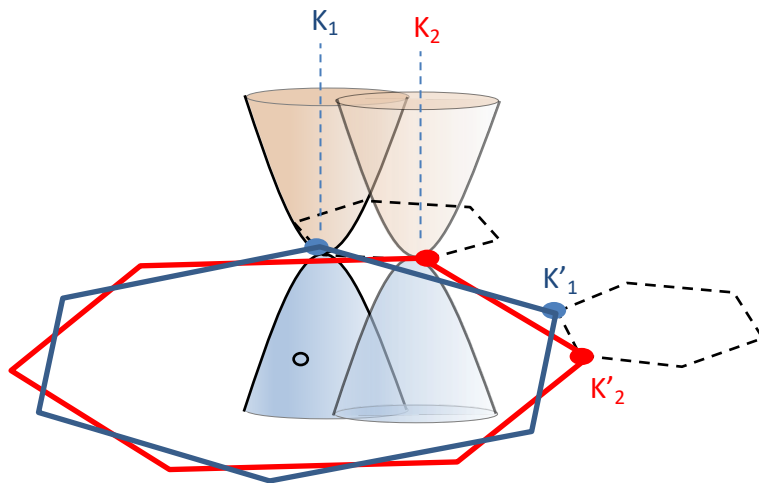
Bernal Stacked Bilayer Graphene



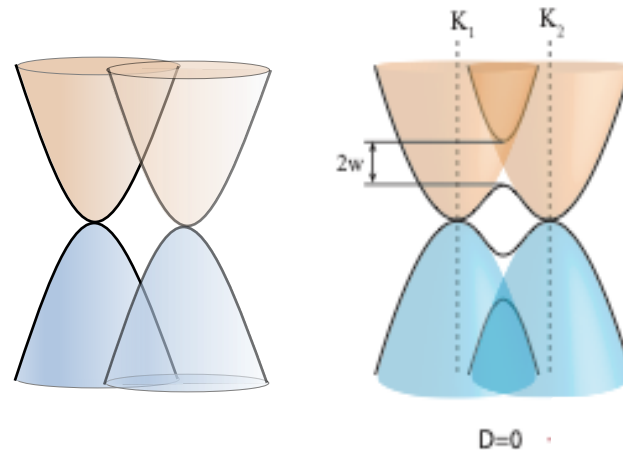
Gate tunable Gap opening in bilayer



Zhang et al. Nature (2008)



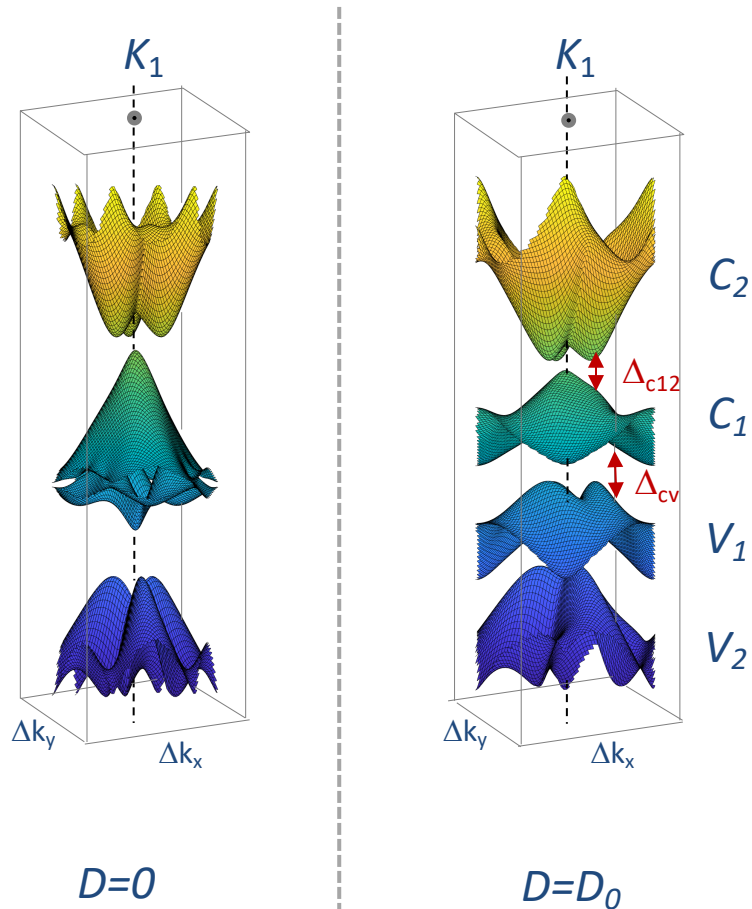
Twisted Double Bilayer Graphene (tDBG)



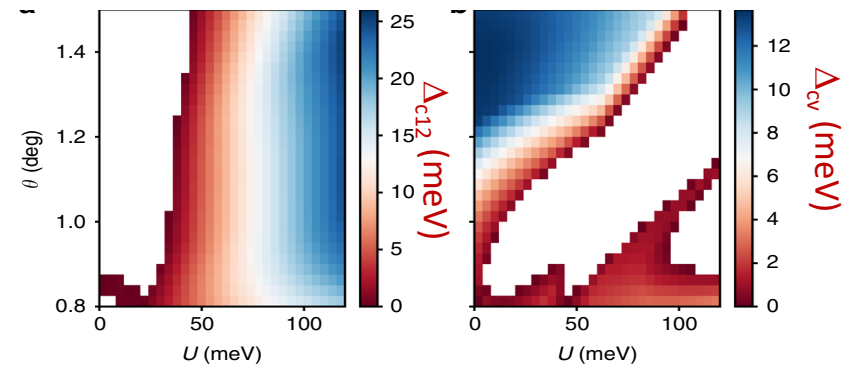
Gate tunable flat bands, no exact angle control needed!

Twisted Double Bilayer Graphene: Tunability

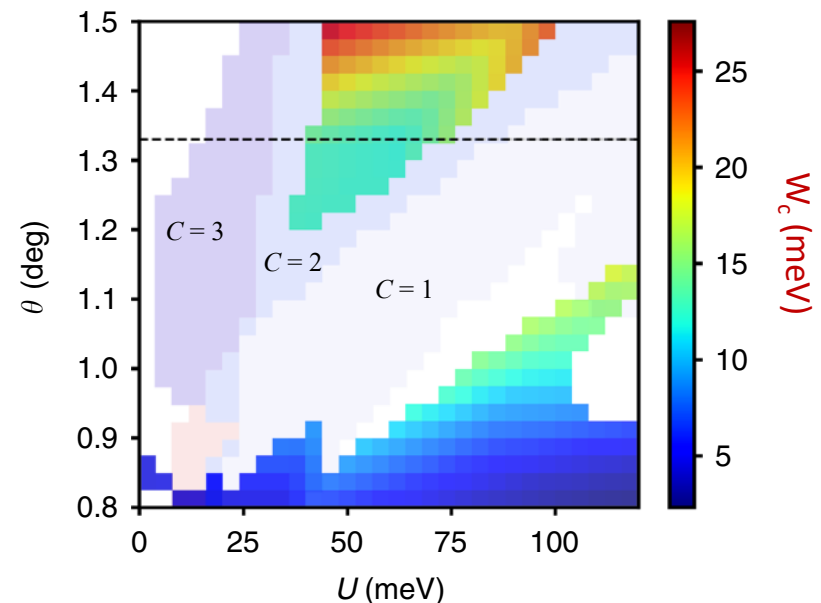
Tight binding with effective Wannier orbits



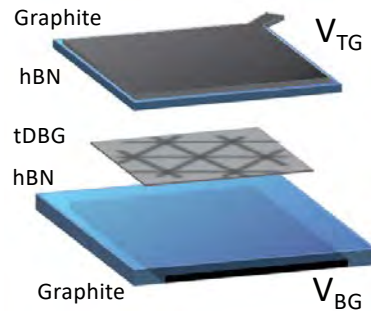
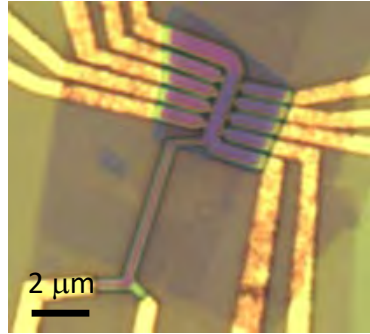
Band Gaps



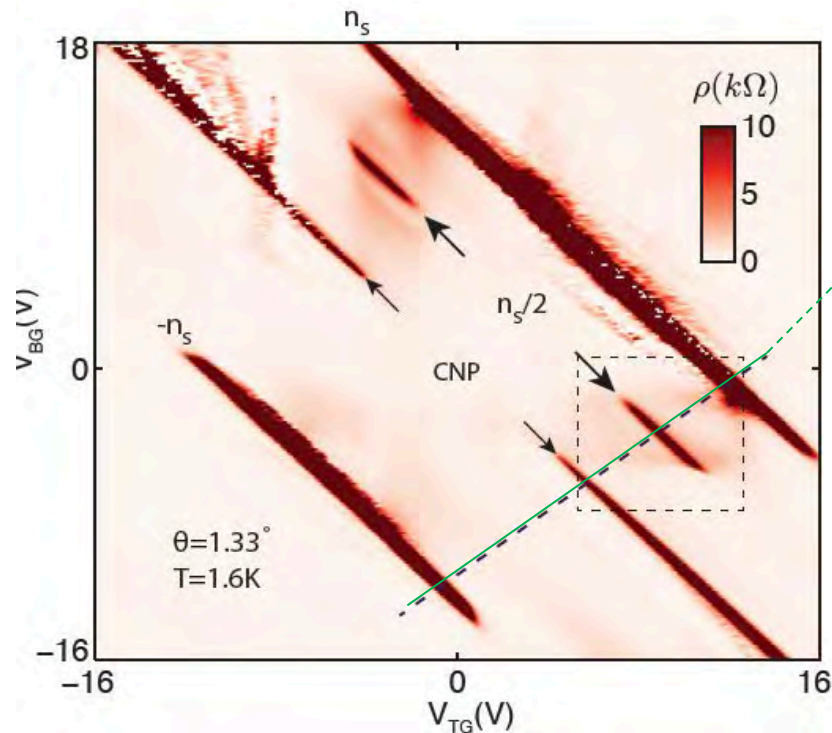
Isolated Conduction band width



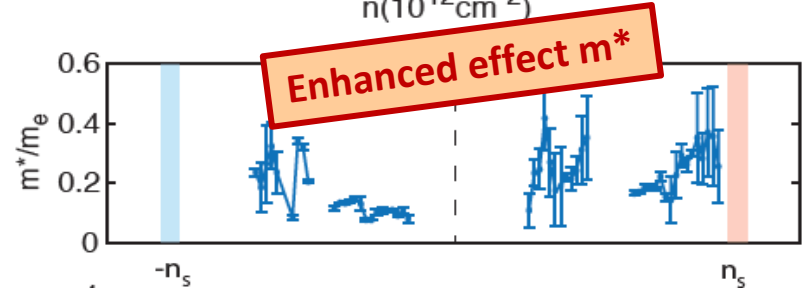
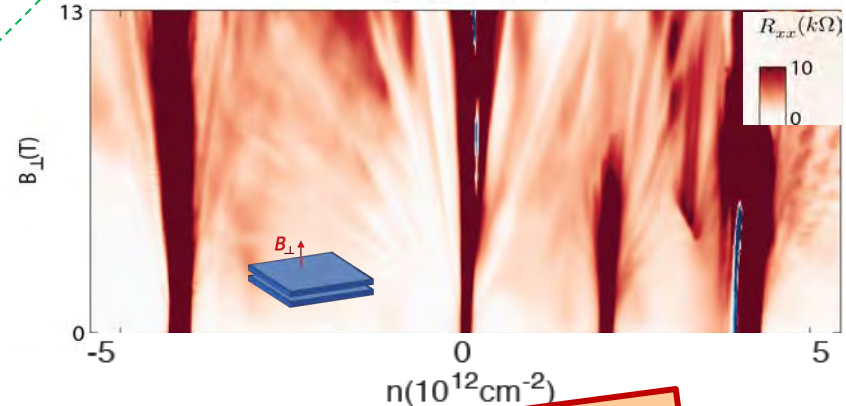
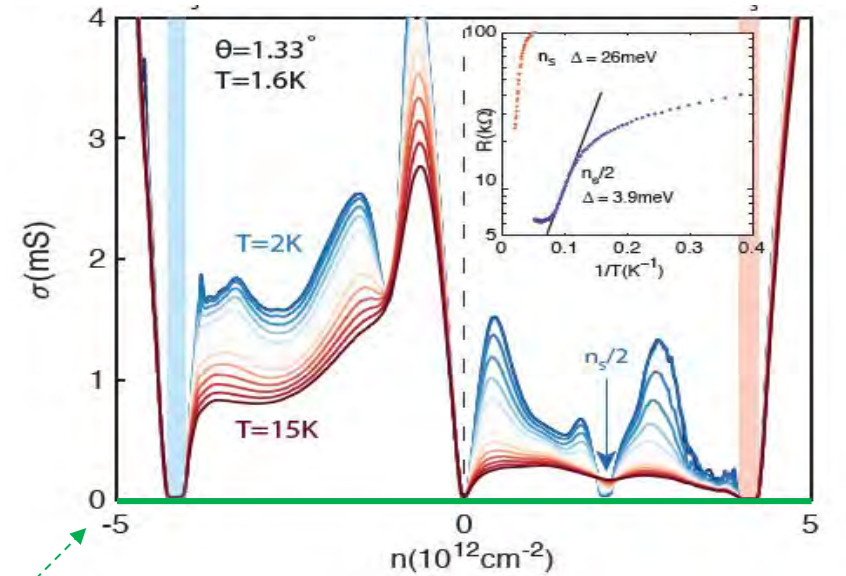
Mott Insulators in tDBG: $\theta = 1.33^\circ$



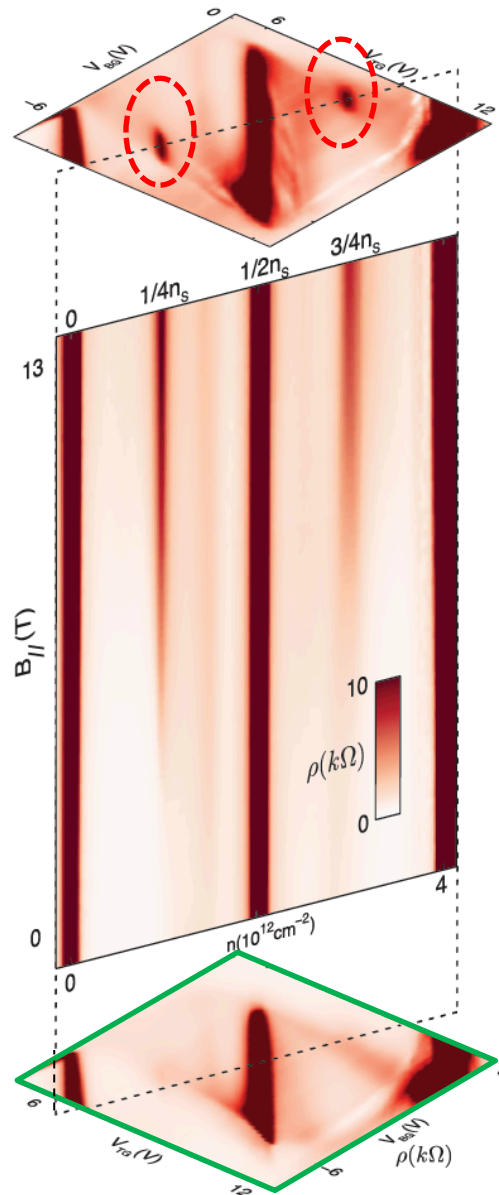
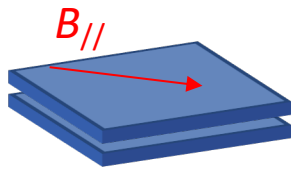
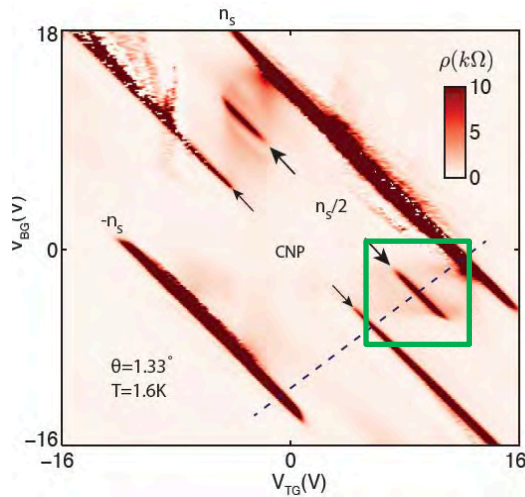
Top and bottom Gate dependent 4-terminal ρ



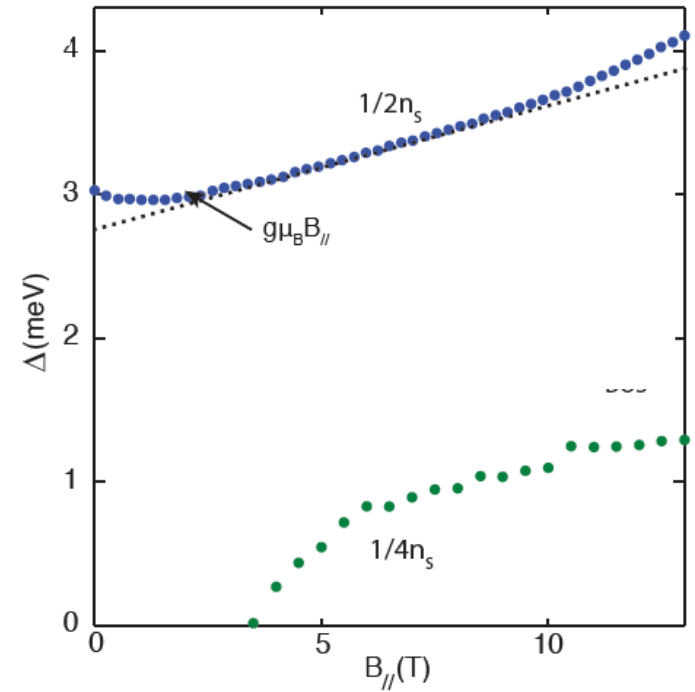
Temperature dependent 2-p conductance



Ferromagnetic Mott Insulators in tDBG $\theta = 1.33^\circ$



- $n_s/4$ & $3n_s/4$ gaps appear at finite $B_{||}$
- $n_s/2$ states become stronger

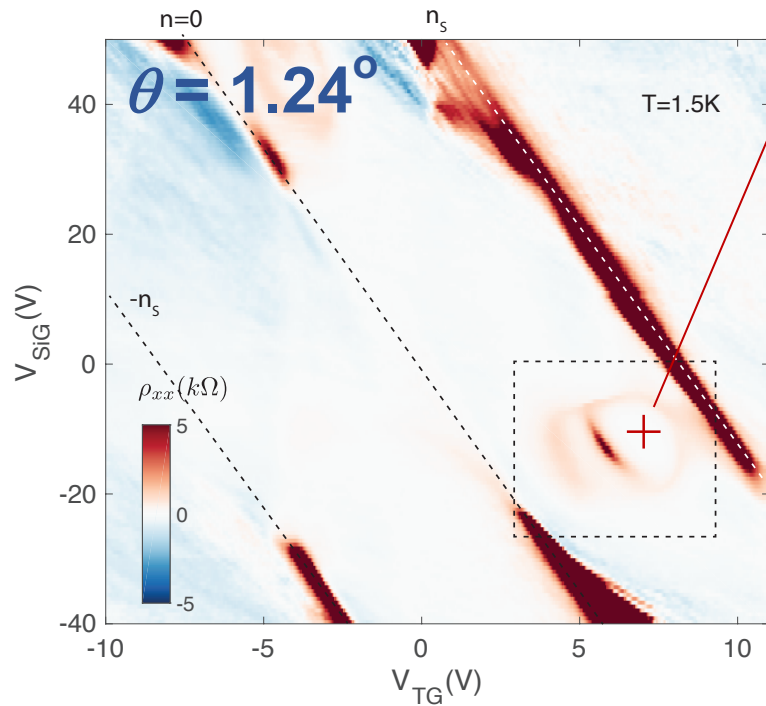
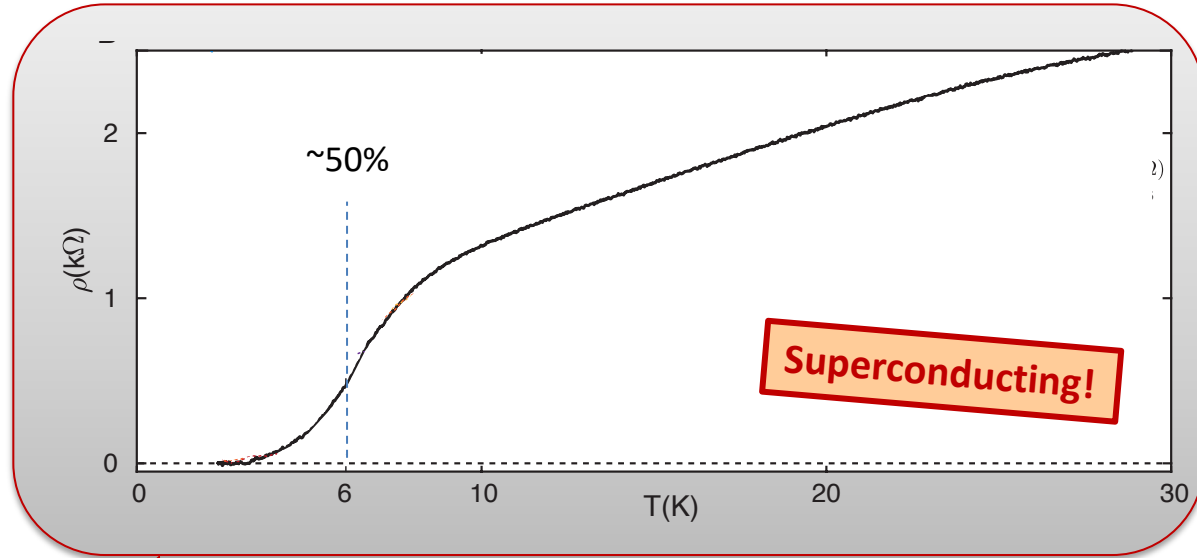
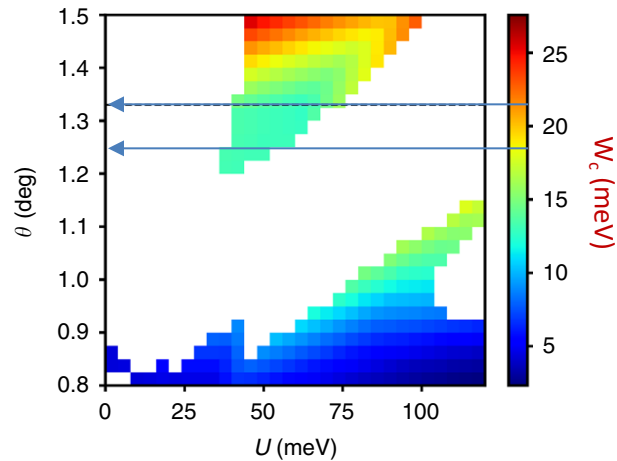


- Gap increases with $B_{||}$
- $g \approx 2$

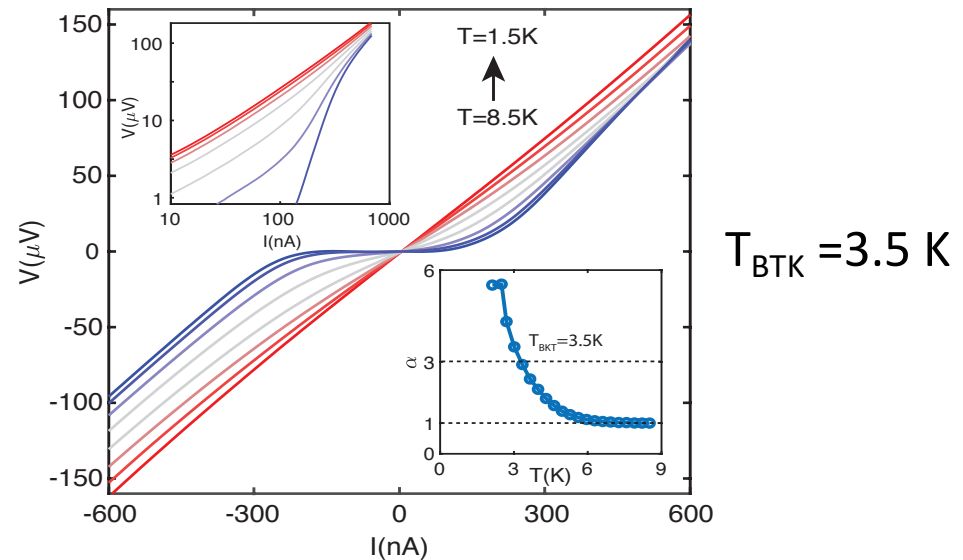
Spin polarized Mott State!

Superconductivity in tDBG

Isolated Conduction band width

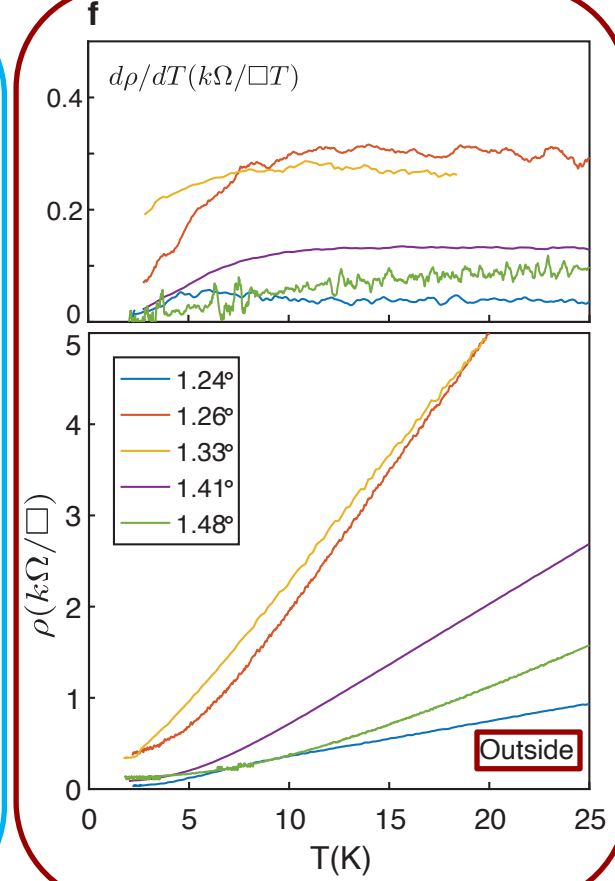
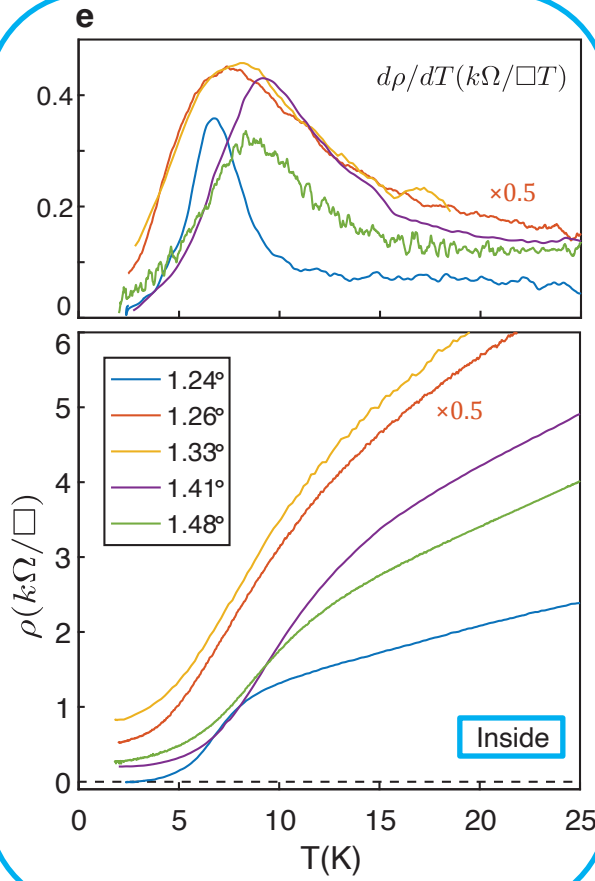
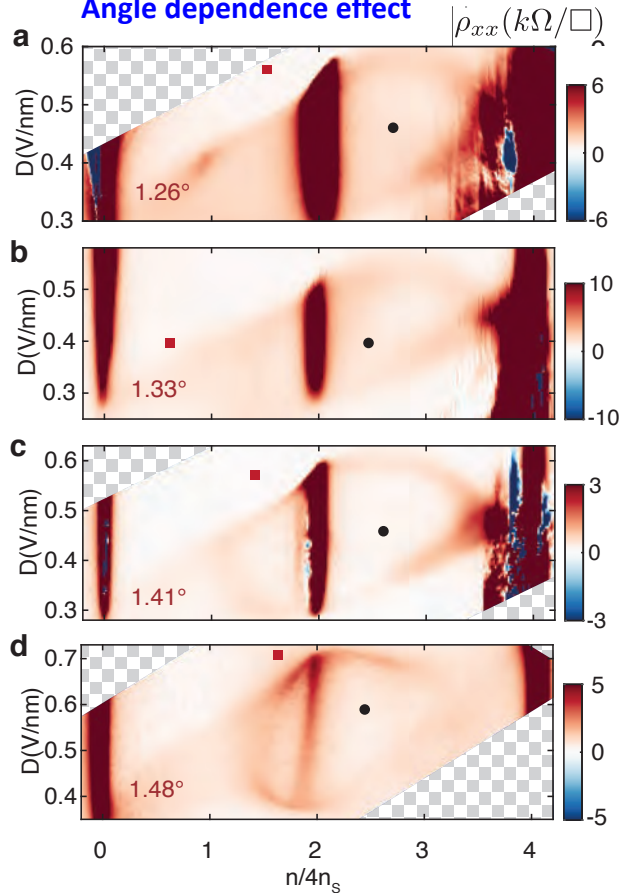


I-V characteristics: BTK Transition

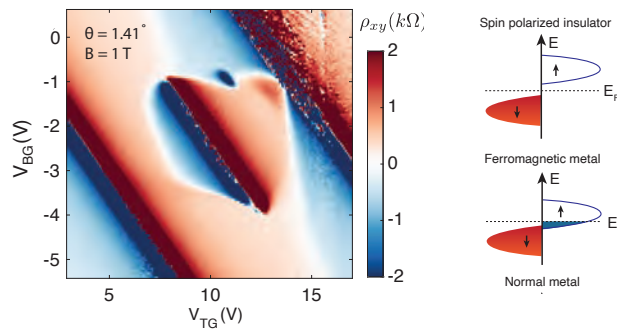


Superconducting Or Not Superconducting?

Angle dependence effect

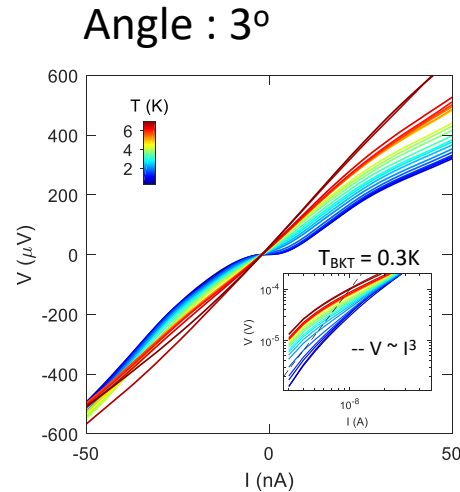
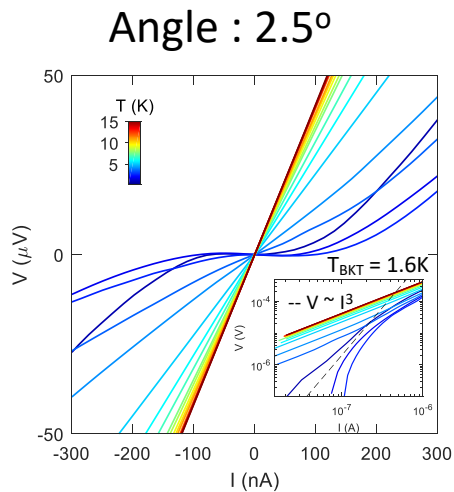
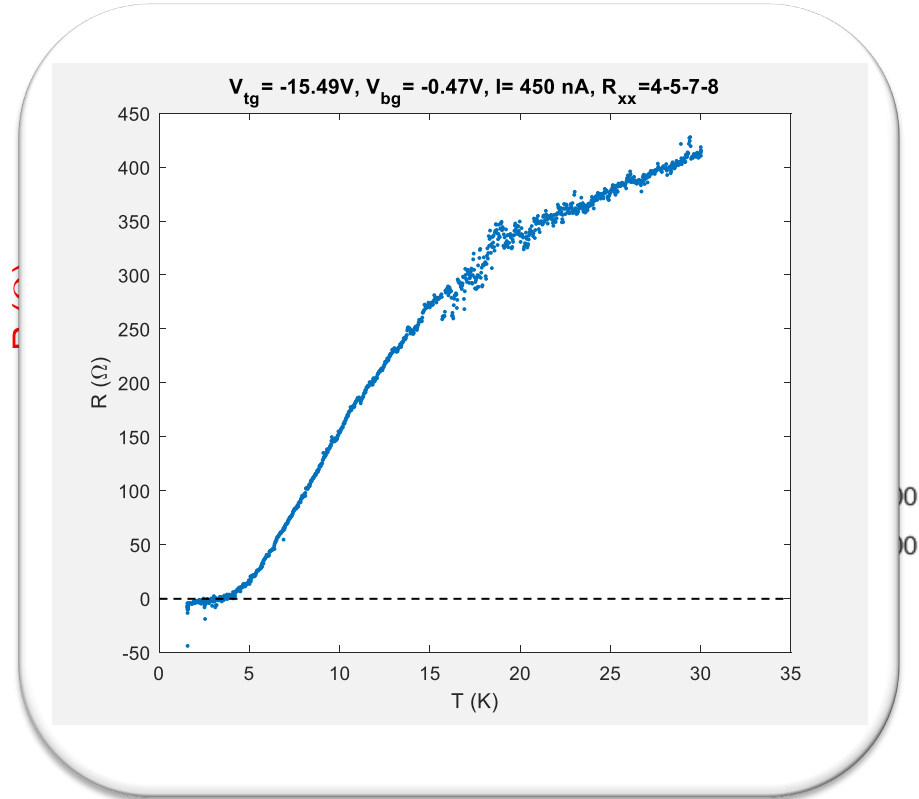
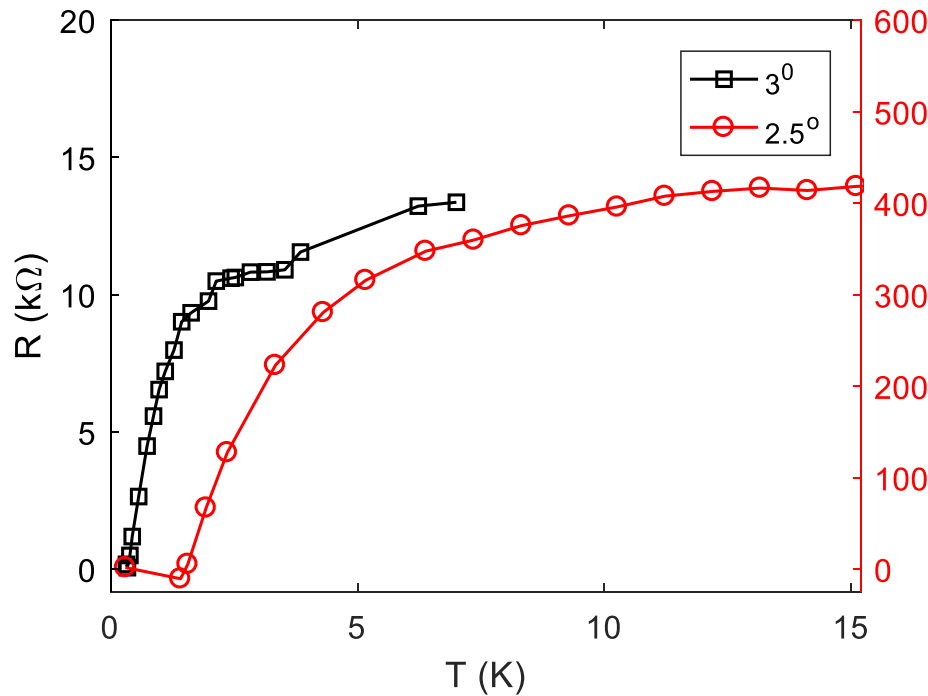


Hall sign change across the gap



- Critical transition behavior near the spin polarized gaps
- However, we have just one sample showing \sim zero resistance.

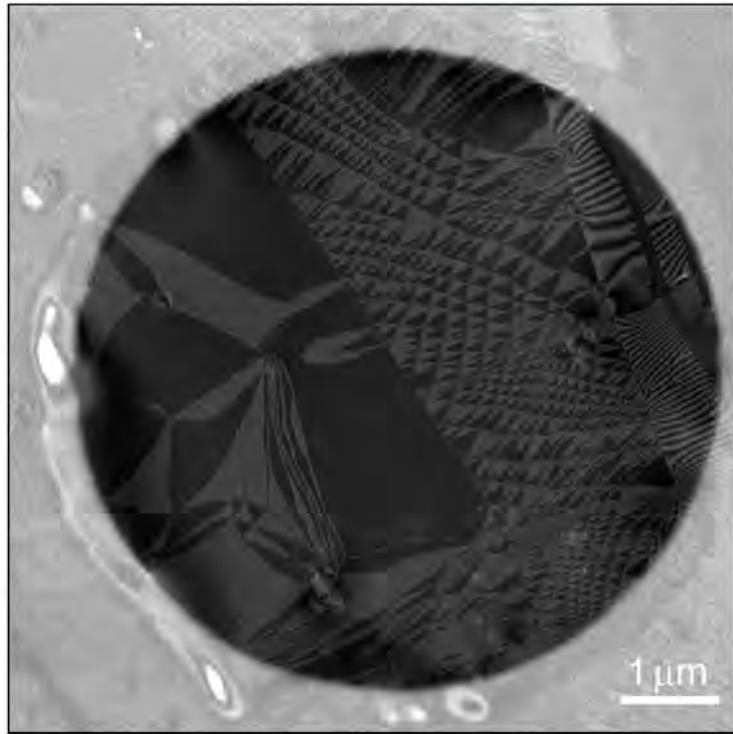
Superconducting(?) Twisted bilayer WSe₂



~ 8 K
Superconducting-like state $T_c \sim 0.3 - 3 K$
has been realized in a wide angle range!

See also similar data in An *et al.*, arXiv:1907.03966

Random Moire: Domain and Domains Boundaries



Random domains in
WSe₂/WSe₂ with small angel

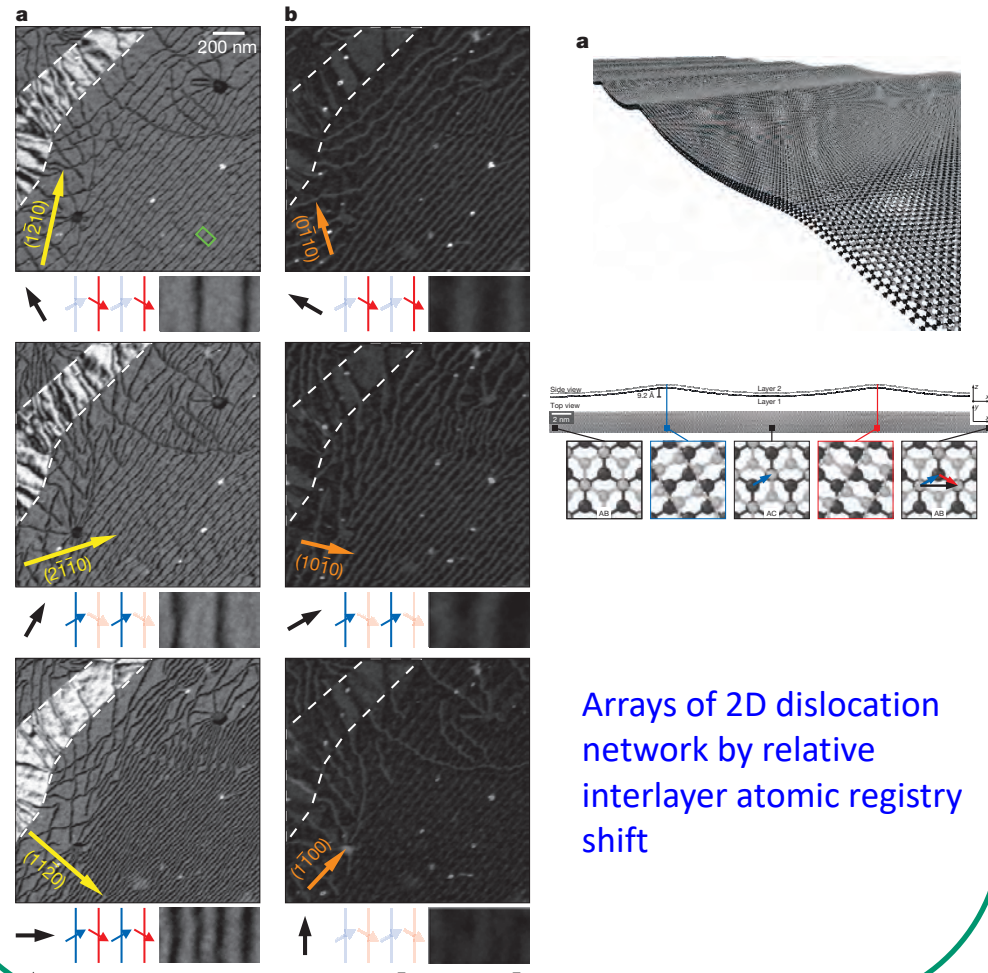
Moire lattice can be viewed as 2D
network of dislocation lines.

23 JANUARY 2014 | VOL 505 | NATURE | 533

doi:10.1038/nature12780

Dislocations in bilayer graphene

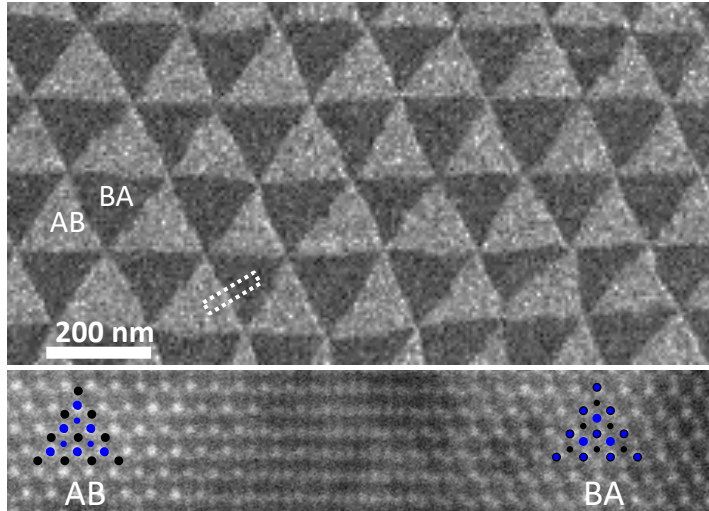
Benjamin Butz¹, Christian Dolle¹, Florian Niekel¹, Konstantin Weber², Daniel Waldmann³, Heiko B. Weber³, Bernd Meyer² & Erdmann Spiecker¹



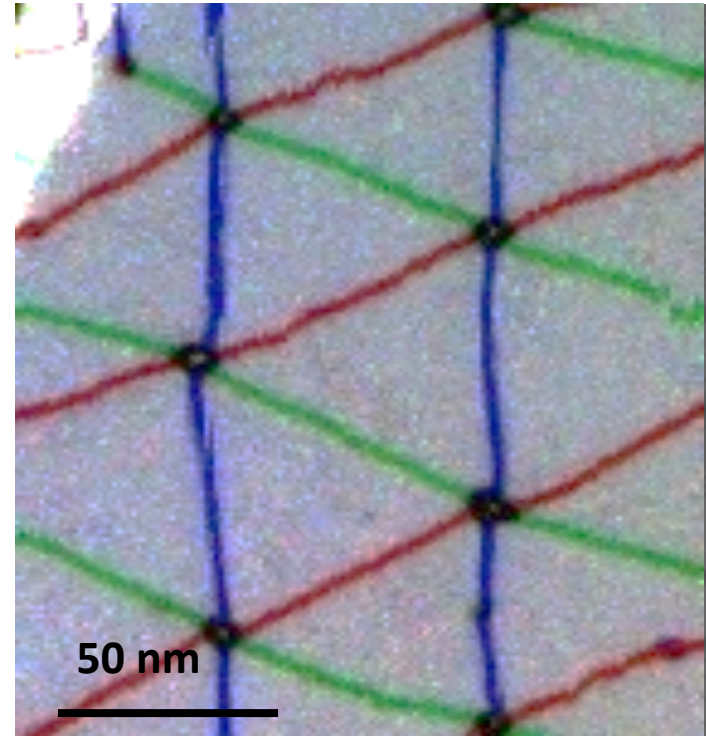
Arrays of 2D dislocation
network by relative
interlayer atomic registry
shift

Burgers Vector for Moire Boundaries in TBG

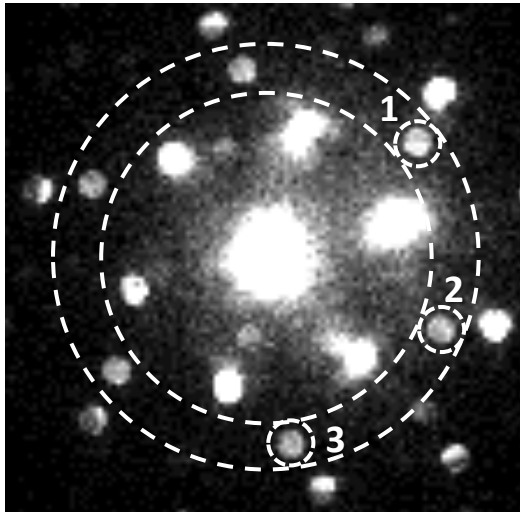
Dark field TEM/ Atomic-resolution Scanning TEM



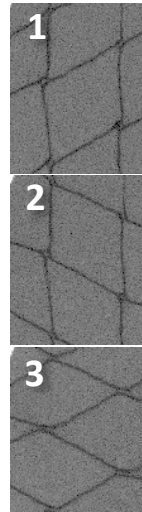
Domain Boundary Coloring by Burgers Vector



Electron diffraction



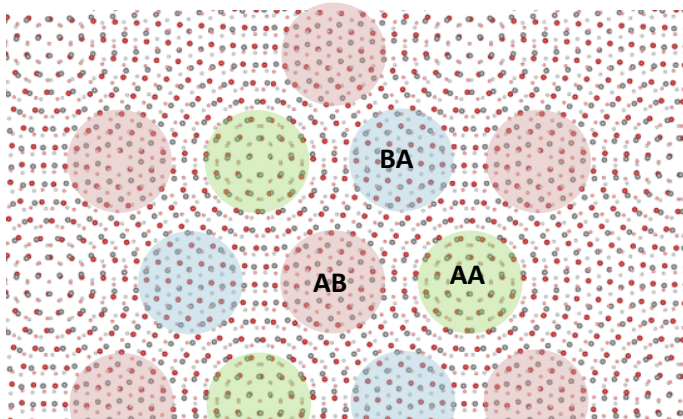
Second Order Bragg Peak
Dark field imaging



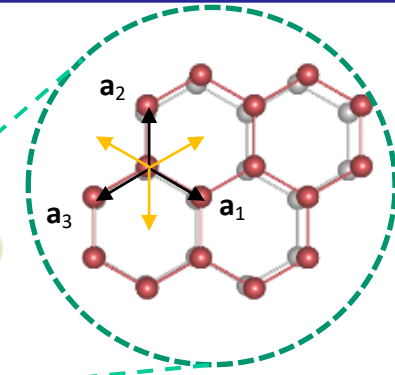
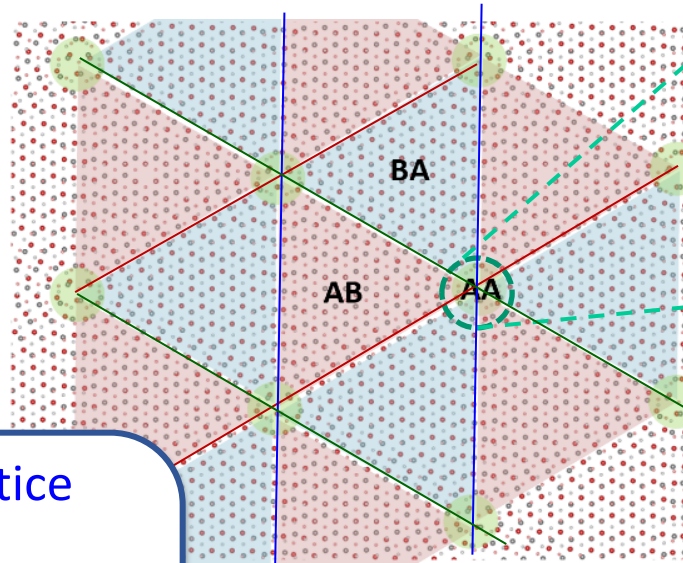
After the lattice relaxation, AA site is a junction for three dislocation lines intersect!

Lattice Shift Vector: Order Parameter for Relaxation Process

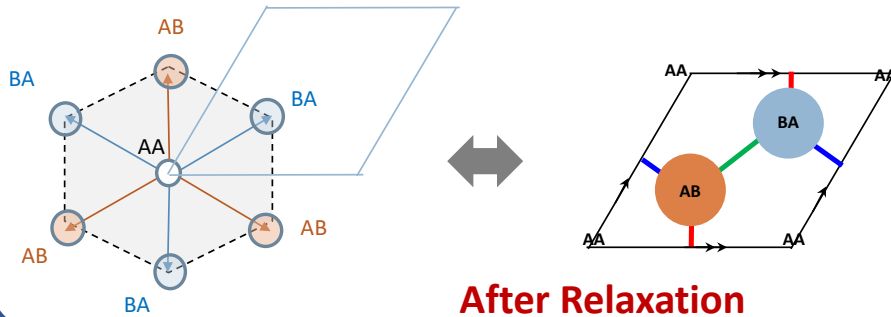
Unrelaxed



Relaxed



Order parameter \mathbf{u} in periodic lattice



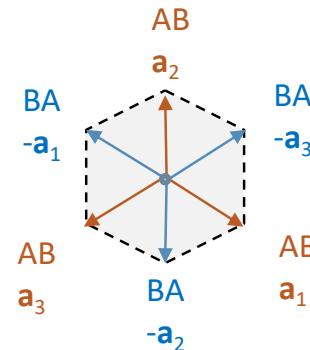
After Relaxation

Define Lattice Shift Vector:

$$\mathbf{u} = [\mathbf{R}(\text{upper layer}) - \mathbf{R}(\text{lower layer})]_{\text{unit cell}}$$

We also define $\mathbf{u} = 0$ for untwisted sample and $\mathbf{u} = 0$ for a AA site as a rotational center.

Shift vector: \mathbf{u}

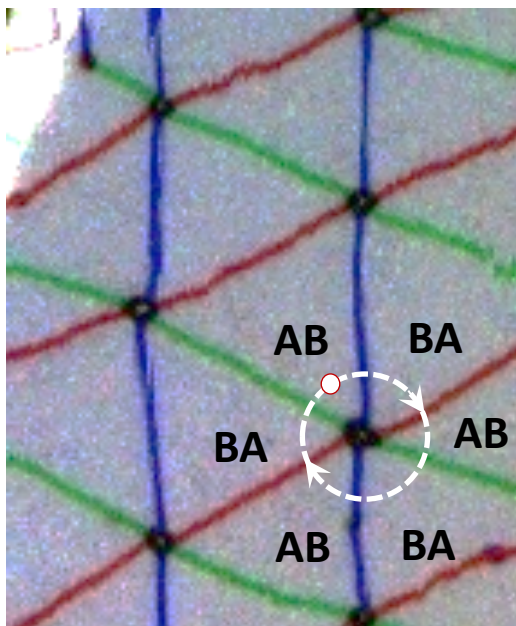


Order parameter
Configuration space
(periodic unit cell)

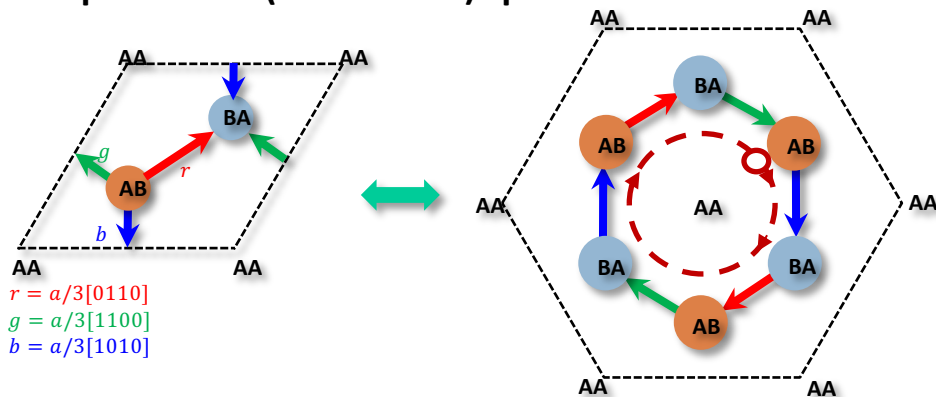
Topology of Moire Network

Han et al., preparation

Real Space Dark Field Moire Images



Order parameter (shift vector) space

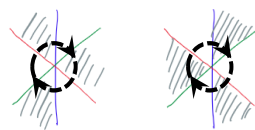


Topology of F2 Free Group Elements

Monopole

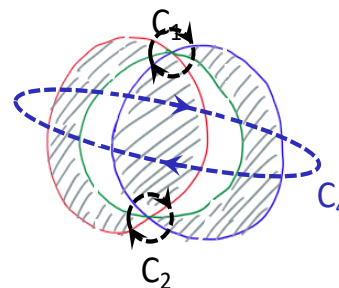


Vortices: $RLR^{-1}L^{-1} = T$



Anti-vortices: $LRL^{-1}R^{-1} = T^{-1}$

Dipole



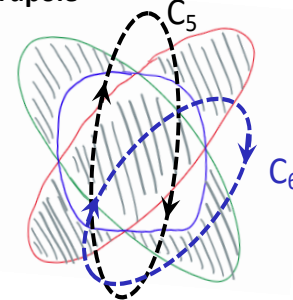
$C_1: LRL^{-1}R^{-1} = T^{-1}$

$C_2: RLR^{-1}L^{-1} = T$

$C_3: RR^{-1} = T^0$

$C_4: LR^{-1}RL^{-1} = T^0$

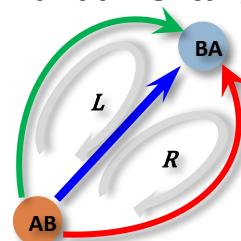
Quadrupole



$C_5: LRL^{-1}R^{-1}LRL^{-1}R^{-1} = T^{-2}$

$C_6: LR^{-1}L^{-1}LRL^{-1} = T^0$

Topological Fundamental group of order parameter space



Free group on 2 generators

$\rightarrow RL \neq LR$

$L = gb^{-1}$

$R = br^{-1}$

A loop around AA site corresponds to

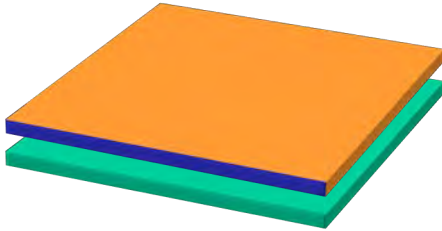
$$RLR^{-1}L^{-1} = br^{-1}gb^{-1}rg^{-1}$$

Equivalent to the topology of punctured torus



Vortex and Anti-Vortex Pair

Interlayer relative elastic deformation



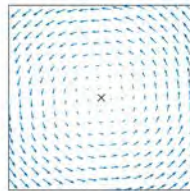
$$\mathbf{u}(\mathbf{r}) = \left(\mathbf{1} + \frac{\partial u_i}{\partial r_j} \right) \mathbf{r} = \begin{cases} \begin{pmatrix} \cos(\theta) - 1 & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) - 1 \end{pmatrix} & \text{Rotation} \\ \begin{pmatrix} \alpha & 0 \\ 0 & \alpha \end{pmatrix} & \text{Isotropic} \\ \begin{pmatrix} \beta_1 & 0 \\ 0 & -\beta_1 \end{pmatrix} & \text{Uniaxial} \\ \begin{pmatrix} 0 & \beta_2 \\ \beta_2 & 0 \end{pmatrix} & \text{Shear} \end{cases}$$

$\mathbf{u}(\mathbf{r})$ map in different elastic deformation

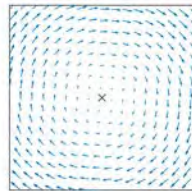
Corresponding dislocation network

Vortex

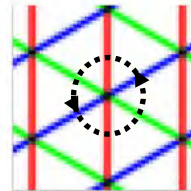
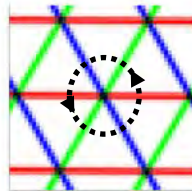
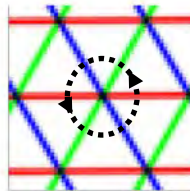
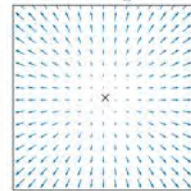
CW



CCW

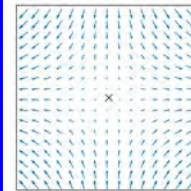


Isotropic

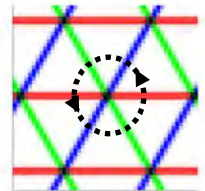
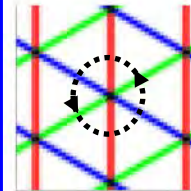
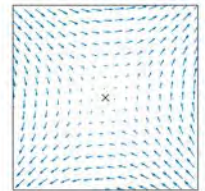


Anti-Vortex

Uniaxial

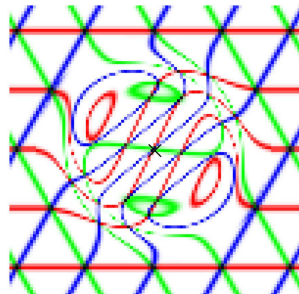
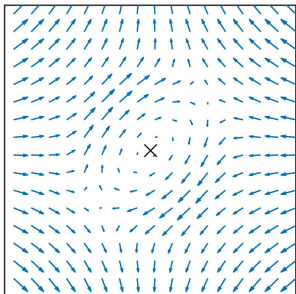


Shear



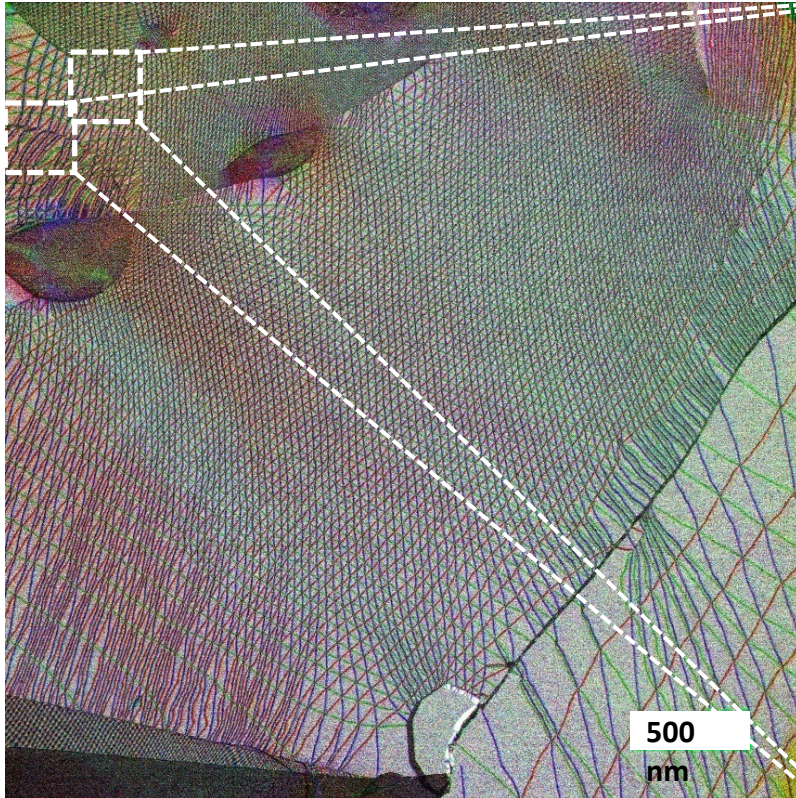
$$RLR^{-1}L^{-1} = br^{-1}gb^{-1}rg^{-1}$$

$$LRL^{-1}R^{-1} = gr^{-1}bg^{-1}rb^{-1}$$

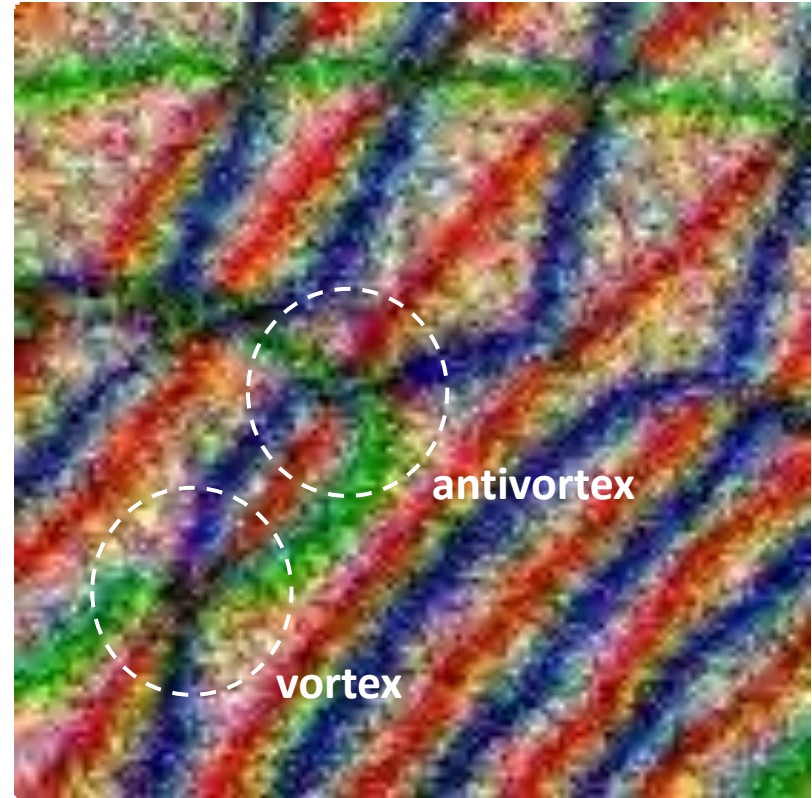


Vortices and Antivortices in mixed (shear + rotation) elastic deformation

Realization of Vortex and Anti-Vortex Pair



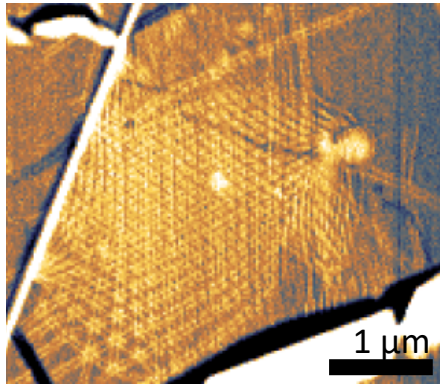
Vortex: **rgb**rgb, antivortex: **rbg**rbg



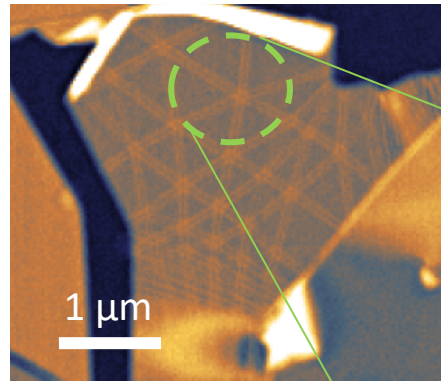
Toward Transport Through A Vortex

Designing with ultra-small twist angles

$\sim 0.1^\circ$ twist

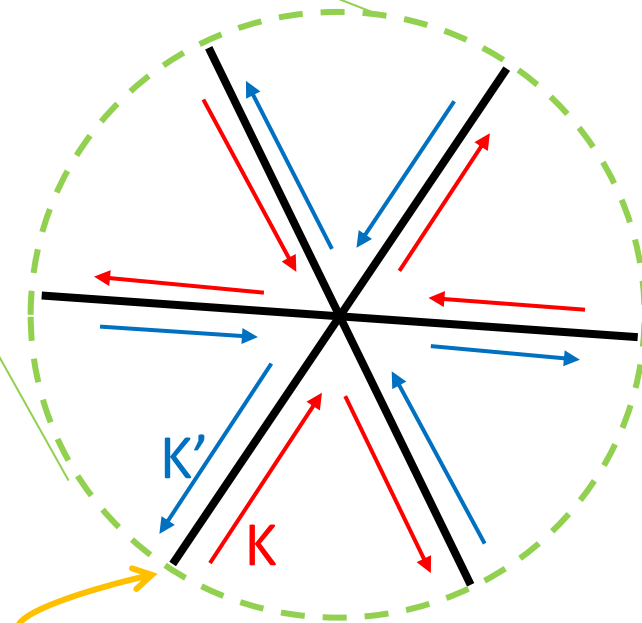


$\sim 0.01^\circ$ twist



Near field IR scanning microscopy by Yue Luo

Investigate transport at vortex
formed by intersecting domain walls

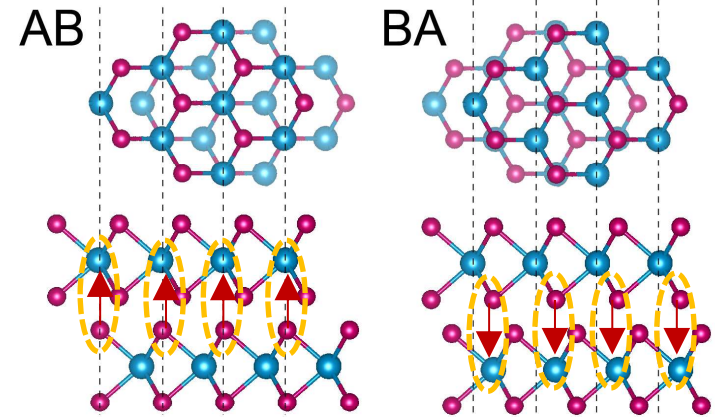
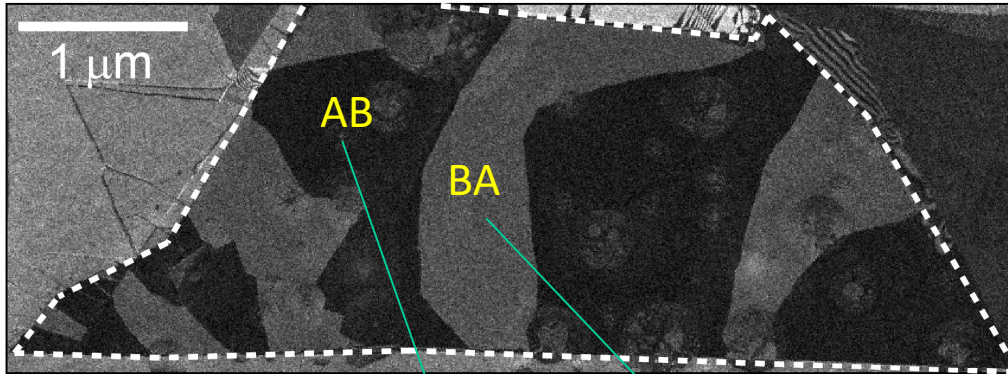


Imaging -> rational device
design based on structure

Valley-selective topologically protected modes

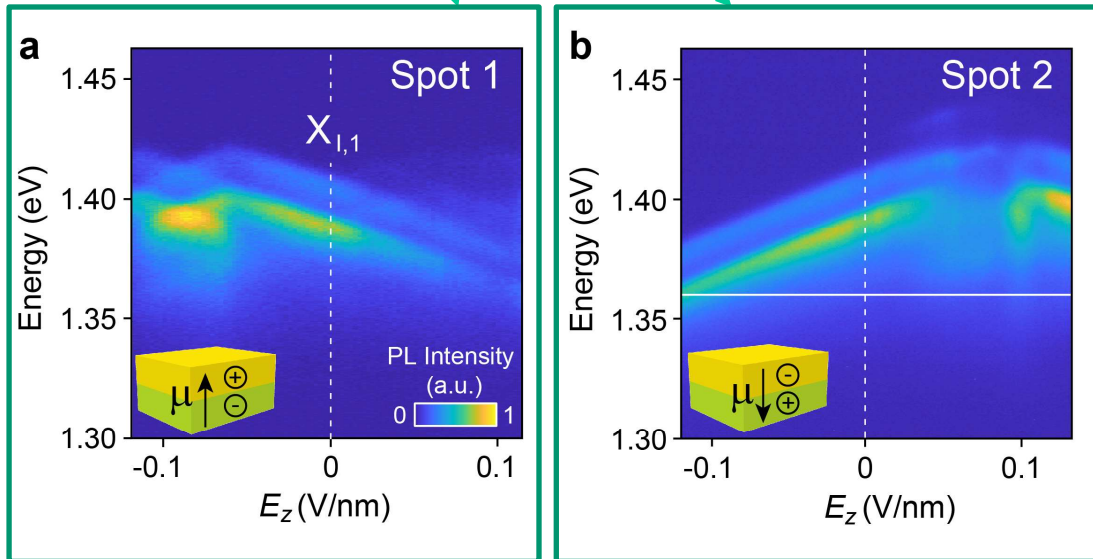
Broken Mirror Symmetry and Spontaneous Dipoles

MoSe₂/MoSe₂ near 0 degree

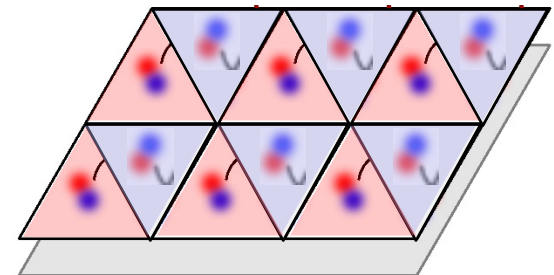


Interlayer dipole moment due to charge transfer!

Electric Field Dependent Photoluminescence



Arrays of alternating dipole moment interlayer excitons due to broken mirror/inversion symmetry in the AB and BA domains.



Summary and Outlook

- Moire superlattice fabrication in vdW interfaces provide band structure engineering in nanometer length scale.
- Correlated physical states appear in magic angle twisted bilayer graphene.
- Spin polarized correlated insulator in twisted double bilayers.
- AA site of moire lattice can be considered as topological defects.

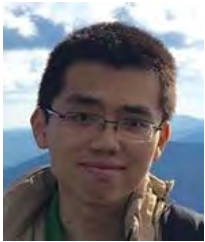
Going Forward:

- Symmetry elements in the materials can be engineered by twist angle control.
- Can we generate topologically non-trivial electronic structures from twisted vdW stacks?

Acknowledgement

Experiments

Double bilayer



Xiaomeng Liu



Zeyu Hao

WSe₂/WSe₂

Louis Jauregui, Andres Mire-Valdivia

2D dislocation network

Hyobin Yoo, Rebecca Engelke

BSCCO/BSCCO

Frank Zhao, Nicola Poccia

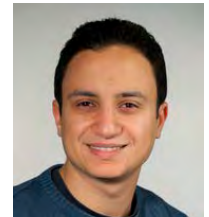
Theory



Ashvin Vishwanath



Jong Yeon Lee



Eslam khalaf



Efthimios Kaxiras



Shiang Fang



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