
WÜRZBURG

## AG Sangiovanni

## Engineering correlated orbitals: metal-insulator and topological phase transitions

## In collaboration with

- Severino Adler Philipp Eck

- Domenico Di Sante (Würzburg)
- Alessandro Toschi Karsten Held (Vienna)
- Tim Wehling (Bremen)

Roser Valentí (Frankfurt)

- Adriano Amaricci

Massimo Capone (Trieste)

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Julius-Maximilians-

## UNIVERSITÄT

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- splitting of two $e_{g}$ orbitals, $\mathrm{d}^{7}-\mathrm{d}^{8}$ physics
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"effective" crystal-field splitting
$\Delta_{\mathrm{eff}}^{e_{g}}=\Delta_{\mathrm{DFT}}^{e_{g}}+\operatorname{Re} \Sigma_{3 z^{2}-r^{2}}(\omega \rightarrow 0)-\operatorname{Re} \Sigma_{x^{2}-y^{2}}(\omega \rightarrow 0)$


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## $2^{\text {nd }}$ part of my talk correlated Tls twisted-bilayer TMD


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- always useful/meaningful?
- what happens when we lose such simple single-particle picture?
- inclusion of many-body effects $\Longrightarrow$ two possible results



## Oxide Heterostructures

- highly active field, even several years after the first pioneering contributions by H. Hwang, A. Millis, etc... [previous talk by Divine Kumah]
- platform for superconductivity and magnetism
- d-electrons: strong responses beyond bulk phase diagrams


## $\mathrm{LaTiO}_{3} / \mathrm{SrTiO}_{3}$

Okamoto, et al. PRL (2006)



Mannhart et al. MRS Bull. (2008)


Bert et al. Nature Phys. (2011)


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thickness-induced metal-insulator transitions



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- thin films of good-old-friend $\mathrm{SrVO}_{3}$ on $\mathrm{SrTiO}_{3}$
- weight at $E_{F}$ disappears for small values of $n$


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## Julius-Maximilians <br> UNIVERSITÅT WÜRZBURG

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- SVO thin films in DFT ( $\mathrm{n}=2$ )
- splitting of the $\mathrm{t}_{2 g}$


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## Device concept?

RL 114, 246401 (2015)
PHYSICAL REVIEW LETTERS

## Electronics with Correlated Oxides: $\mathrm{SrVO}_{3} / \mathrm{SrTiO}_{3}$ as a Mott Transistor

 Zhicheng Zhong, ${ }^{1}$ Markus Wallerberger, ${ }^{1}$ Jan M. Tomczak, ${ }^{1}$ Ciro Taranto, ${ }^{1}$ Nicolaus Parragh, ${ }^{2}$ Alessandro Toschi, ${ }^{1}$ Giorgio Sangiovanni, ${ }^{2}$ and Karsten Held ${ }^{1}$- 2 V-layers ( $\mathrm{n}=2$ ): insulating in DFT+DMFT
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- smooth correction within Hartree-Fock ( $\mathrm{Re} \mathbf{\Sigma} \sim \mathrm{Un}$ )
- DMFT: non-linear effects/first-order behavior



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## Device concept?

PRL 114, 246401 (2015

- orbital polarization easy to switch ON and OFF!
(thickness, pressure, strain, temperature, gating,...)
- 2 V-layers ( $\mathrm{n}=2$ ): insulating in DFT+DMFT
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- $\mathrm{VO}_{2}+\sqrt{ } 2 \times \sqrt{ } 2$ oxygen reconstruction
- solution: capping!

- surprising result:
critical thickness much bigger than
Yoshimatsu, et al. and DFT+DMFT


## Surface of SVO thin films

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- enhancement, but in which direction? importance of the sign of $\Delta_{\mathrm{DFT}}^{t_{2 g}}$
- work in progress (Würzburg + Vienna)


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STO cap

- 。 . . • Ti ${ }^{4+}$
- ••••• $V^{4+}$
- ••••• $V^{4+}$

$\mathrm{O} \cdot \mathrm{Ti} \cdot \mathrm{Sr} \bullet \mathrm{V}$
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- iridium thin films (spin-orbit)
$5 \underline{\underline{\underline{\underline{\underline{D}}}}}$


week ending 22 DECEMBER 201

Dimensionality-Driven Metal-Insulator Transition in Spin-Orbit-Coupled $\mathrm{SrIrO}_{3}$

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\text { M.-A. Husanu, }{ }^{5,6} \text { V. N. Strocov, }{ }^{6} \text { G. Sangiovanni, }{ }^{2} \text { M. Sing, }{ }^{1} \text { and R. Claessen }{ }^{1}
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- mimicking the Ruddlesden-Popper series:
H. Zhang, et al. PRL (2013)




PRL 119, 256404 (2017)

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- interplay between SOC, structural distortions and magnetism
- see poster by Severino Adler on 5d3 Osmates



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Termination conservation

$$
2 \cdot \mathrm{IrO}_{2}(\text { solid })+\mathrm{O}
$$

Termination conversion
confirmed by DFT+U calculations (Domenico Di Sante)
$P$. Schütz, et al. submitted



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- in nickel heterostructures: when the $d$-shell gets closer to $\mathrm{d}^{8}$
- Hund's tendecy to high-spin triplet Mott insulator in the $e_{g}$ doublet


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- HgTe (BHZ model) A. Bernevig, et al. Science (2006)
- Two orbitals ( $\mathbf{s} \mathbf{p}$ ) and spin 1/2
- Time-reversal

$$
\mathbf{H}_{4 \times 4}(\mathbf{k})=\left(\begin{array}{c:c}
\hat{h}_{0}(\mathbf{k}) & \uparrow \downarrow \\
\hdashline \downarrow \ldots \ldots \ldots \ldots \ldots \ldots \\
\hdashline \downarrow & \hat{h}_{0}^{*}(-\mathbf{k})
\end{array}\right) \quad \hat{h}_{0}(\mathbf{k})=\vec{d}(\mathbf{k}) \cdot \vec{\tau}
$$

- $\mathrm{U}(1)_{\text {spin }}$ symmetry

$$
\vec{d}(\mathbf{k})=\left(\begin{array}{c}
\lambda \sin k_{x} \\
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Pauli matrices in orbital space
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$\mathscr{C}_{1}=0$

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$\mathscr{C}_{1}=1$

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## BHZ-Hubbard model

- orbital structure of interaction for the BHZ + Hubbard $U$, Hund $J$
- simplest local interaction term
[see A. Georges, L. de’ Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

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zeroth-order correction: $M_{\text {eff }}$
Y. Tada, et al. PRB (2012) T. Yoshida, et al. PRB (2012) L. Wang, et al. EPL (2012) J. Budich, et al. PRB (2012) J. Budich, et al. PRB (2013)


- Intra- + inter-orbital $J$ (Hund) interaction
- U suppresses double occupancies $\Longrightarrow$ reduced effective orbital splitting $M_{\text {eff }}$


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- QSH extends at large- $U$ and large $-M$, as a "precursor" of the high-spin phase

 solver: CT-HYB
antiferromagnetic insulator


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UB"


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- QSH extends at large- $U$ and large- $M$, as a "precursor" of the high-spin phase
- ...but there is more to that: see color coding in the phase diagram!

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- where do the colors come from?

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M-\operatorname{Re} \Sigma(0)-\cos k_{x}-\cos k_{y}
\end{array}\right)
$$



- distinction between flat "Hartree-Fock" and
- pronounced $\omega$-structure of many-body nature



## UNIVERSITÄT WÜZZBURG

## BHZ-Hubbard model

- where do the colors come from?

$$
\mathcal{H}_{\mathrm{int}}(\mathrm{i})=(U-J) \frac{N_{\mathrm{i}}\left(N_{\mathrm{i}}-1\right)}{2}-J\left(\frac{N_{\mathrm{i}}^{2}}{4}+S_{z \mathrm{i}}^{2}-2 T_{z \mathrm{i}}^{2}\right) \quad \vec{d}(\mathbf{k})=\left(\begin{array}{c}
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color scale:
$|\operatorname{Re} \Sigma(\omega=0)-\operatorname{Re} \Sigma(\omega=\infty)| \stackrel{\uparrow}{+}$



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- distinction between flat "Hartree-Fock" and
- pronounced $\omega$-structure of many-body nature
- QSHI and BI no longer smoothly connected
- Gap inversion occurring via a jump

1st-order QSH transition also in Xue\&MacDonald PRL (2018)

## Consequences on the topological phase transition

- gap closing: for $U<U_{c}$ smooth topological phase transition (green $\rightarrow$ green)
- no semimetal for $U \backslash U_{c}$ when the $\mathbb{Z}_{2}$ topological invariant changes (green $\rightarrow$ red)!
- new termodynamics, beyond single-particle effective description



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$$
H=t \sum_{\langle i j\rangle, \alpha} c_{i, \alpha}^{\dagger} c_{j, \alpha}+i \lambda_{\mathrm{SO}} \sum_{\langle\langle i j\rangle\rangle, \alpha \alpha^{\prime}} \nu_{i j} c_{i, \alpha}^{\dagger} s_{\alpha \alpha^{\prime}}^{z} c_{j, \alpha^{\prime}}+i \lambda_{R} \sum_{\langle i j\rangle, \alpha \alpha^{\prime}} c_{i, \alpha}^{\dagger}\left(\mathbf{s} \times \hat{\mathbf{d}}_{i j}\right)_{\alpha \alpha^{\prime}}^{z} c_{j, \alpha^{\prime}}
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## A/B splitting

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H=t \sum_{\langle i j\rangle, \alpha} c_{i, \alpha}^{\dagger} c_{j, \alpha}+i \lambda_{\mathrm{SO}} \sum_{\langle\langle i j\rangle\rangle, \alpha \alpha^{\prime}} v_{i j} c_{i, \alpha}^{\dagger} s_{\alpha \alpha^{\prime}}^{z} c_{j, \alpha^{\prime}}+i \lambda_{R} \sum_{\langle i j\rangle, \alpha \alpha^{\prime}} c_{i, \alpha}^{\dagger}\left(\mathbf{s} \times \hat{\mathbf{d}}_{i j}\right)_{\alpha \alpha^{\prime}}^{z} c_{j, \alpha^{\prime}}+\mathrm{M} \sum_{i, \alpha}^{\mathrm{A}, \mathrm{~B}} \xi_{i} c_{i, \alpha}^{\dagger} c_{i, \alpha}
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 PRL (2005)

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## Material realization?

- $\mathrm{TaSe}_{2}$ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome) + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" $\sqrt{ } 13 \times \sqrt{ } 13$ CDW reconstructions



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flat Ta d-band


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- bilayer: shifted triangular layers $\boldsymbol{\Rightarrow}$ buckled honeycomb!



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- "deconfinement" of Mott localized electrons into correlated Dirac fermions

opposite strategy w.r.t. twisted bilayer graphene



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honeycomb dispersion


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## Material realization?

- we can tune $M$ by means of electric field along $z(\sim 1-4 \mathrm{meV} / \AA ̊)$



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- we can tune $M$ by means of electric field along $z(\sim 1-4 \mathrm{meV} / \mathrm{A})$
- from $\boldsymbol{D}_{6 n}$ to $\boldsymbol{C}_{3 \mathrm{v}}$

$$
\begin{array}{r}
\lambda_{\mathrm{SOO}} \\
\quad B
\end{array}
$$



$$
B \cdot \tau_{z}^{\mathrm{K}, \mathrm{~K}^{\prime}} \cdot \sigma_{z}^{\text {spin }} \cdot S^{\text {sulatt }}
$$




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- we can tune $M$ by means of electric field along $z(\sim 1-4 \mathrm{meV} / \AA ̊)$
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## Strong correlations and orbital texture in single-layer 1T-TaSe ${ }_{2}$ <br> nature physics

strong correlation


Side view

Yi Chen ${ }^{(1), 2,13}$, Wei Ruan ${ }^{1,2,13}$, Meng Wu ${ }^{1,2,13}$, Shujie Tang ${ }^{\left({ }^{(1)}\right.}{ }^{3,4,5,6,7,13}$, Hyejin Ryu ${ }^{5,8}$, Hsin-Zon Tsai ${ }^{1,9}$, Ryan Lee ${ }^{1}$, Salman Kahn ${ }^{1}$, Franklin Liou ${ }^{1}$, Caihong Jia ${ }^{1,2,10}$, Oliver R. Albertini ${ }^{11}$, Hongyu Xiong ${ }^{()^{3,4}}$, Tao Jia ${ }^{3,4}$, Zhi Liu ${ }^{6}$, Jonathan A. Sobota ${ }^{(1)}{ }^{3,5}$, Amy Y. Liu ${ }^{11}$, Joel E. Moore ${ }^{1,2}$, Zhi-Xun Shen $\mathbb{D}^{3,4}$,

## ARTICLES

https://doi.org/10.1038/s41567-019-0744-9




## Conclusions

- many-body correction to the orbital splitting: either favoring or opposing the bare tendency



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## Conclusions

- many-body correction to the orbital splitting: either favoring or opposing the bare tendency
- thickness-induced metal-insulator transition in oxide heterostructures
- local criticality of orbital fluctuations in correlated topological insulators
- possible material realization and tuning in transition-metal dichalcogenides




