



Engineering correlated orbitals: metal-insulator and topological phase transitions

In collaboration with

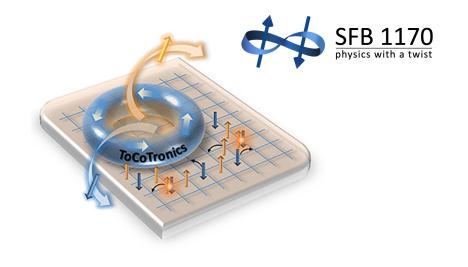
 Severino Adler Philipp Eck



- Domenico Di Sante (Würzburg)
- Alessandro Toschi Karsten Held (Vienna)
- Tim Wehling (Bremen)
 Roser Valentí (Frankfurt)
- Adriano Amaricci
 Massimo Capone (Trieste)
- Jan Budich (Dresden)
 Björn Trauzettel (Würzburg)



Aspen (virtually), March 11. 2020



References: PRB **88**, 195116 (2013) — PRL **114**, 185701 (2015) — PRL **114**, 246401 (2015) — PRL **119**, 256404 (2017) — arXiv:2001.04102 (2020)





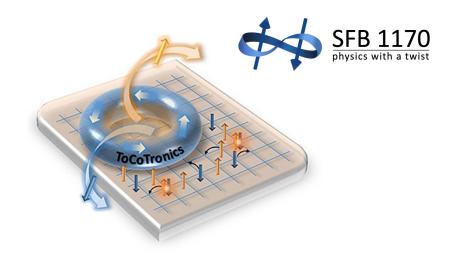
Engineering correlated orbitals: metal-insulator and topological phase transitions

In collaboration with

- Severino Adler Philipp Eck
- Domenico Di Sante (Würzburg)
- Alessandro Toschi Karsten Held (Vienna)
- Tim Wehling (Bremen)
 Roser Valentí (Frankfurt)
- Adriano Amaricci
 Massimo Capone (Trieste)
- Jan Budich (Dresden)
 Björn Trauzettel (Würzburg)



Aspen (virtually), March 11. 2020

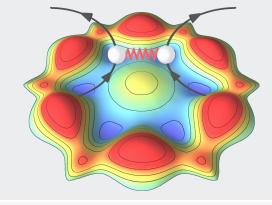


lifting of orbital degeneracy in many-body systems



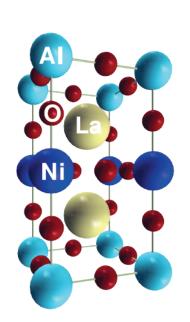
more than just renormalizing single-particle Hamiltonian parameters

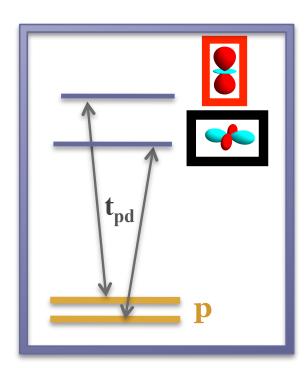
References: PRB **88**, 195116 (2013) — PRL **114**, 185701 (2015) — PRL **114**, 246401 (2015) — PRL **119**, 256404 (2017) — arXiv:2001.04102 (2020)



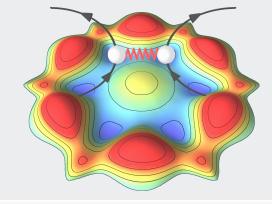
- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics

- J. Chaloupka, et al., PRL (2007)
- A. Poteryaev, , *et al.*, PRB (2008)
- P. Hansmann, et al., PRL (2009)
- N. Parragh, *et al.*, PRB (2013)
- H. Park, *et al.*, PRB (2014)
- A. Rüegg, *et al.*, PRB (2014)
- O. Peil, et al., PRB (2014)



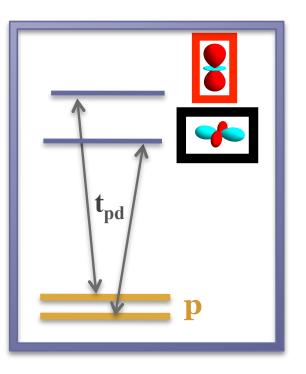






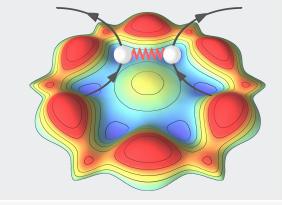
- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects
 ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , et al., PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, *et al.*, PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)





"effective" crystal-field splitting

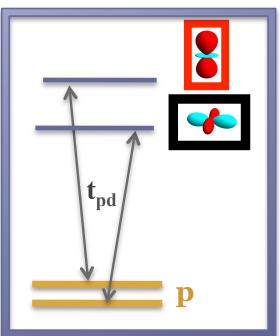
$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2 - r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2 - y^2}(\omega \to 0)$$



• example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity — H. Hwang)

- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , *et al.*, PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, et al., PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)





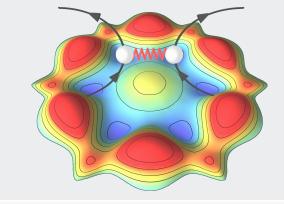


"effective" crystal-field splitting

$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2-r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2-y^2}(\omega \to 0)$$

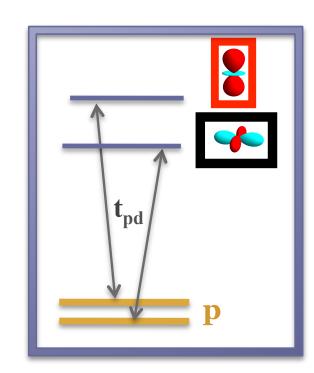






- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , *et al.*, PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, *et al.*, PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)







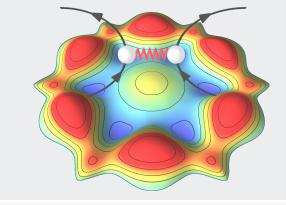
$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2-r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2-y^2}(\omega \to 0)$$





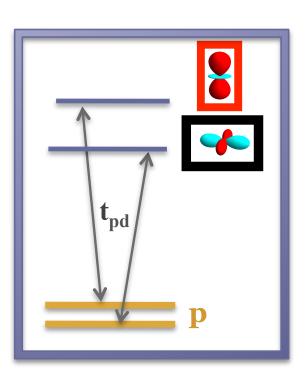






- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , *et al.*, PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, *et al.*, PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)



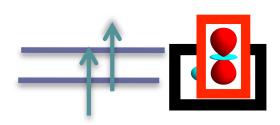


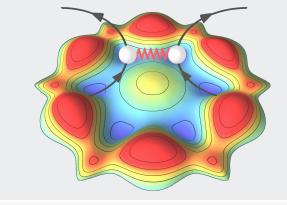
"effective" crystal-field splitting

$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2 - r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2 - y^2}(\omega \to 0)$$



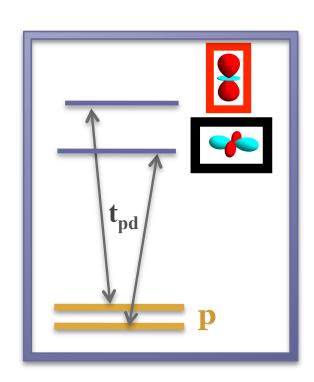






- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , *et al.*, PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, *et al.*, PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)





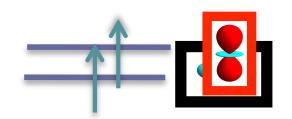
1st part of my talk oxide heterostructures

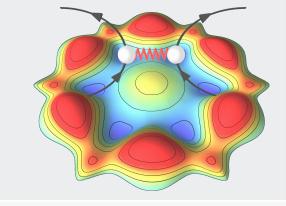


"effective" crystal-field splitting

$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2 - r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2 - y^2}(\omega \to 0)$$

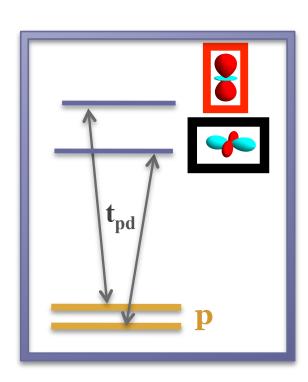
2nd part of my talk correlated TIs twisted-bilayer TMD





- example of nickelate heterostructures (pre-d⁹ nickel-age of superconductivity H. Hwang)
- splitting of two e_g orbitals, d^7 - d^8 physics
- inclusion of many-body effects ⇒ two possible results
 - J. Chaloupka, et al., PRL (2007)
 - A. Poteryaev, , *et al.*, PRB (2008)
 - P. Hansmann, et al., PRL (2009)
 - N. Parragh, *et al.*, PRB (2013)
 - H. Park, et al., PRB (2014)
 - A. Rüegg, *et al.*, PRB (2014)
 - O. Peil, et al., PRB (2014)





1st part of my talk oxide heterostructures

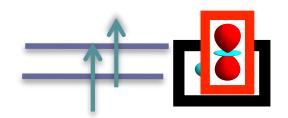


"effective" crystal-field splitting

$$\Delta_{\text{eff}}^{e_g} = \Delta_{\text{DFT}}^{e_g} + \text{Re}\Sigma_{3z^2 - r^2}(\omega \to 0) - \text{Re}\Sigma_{x^2 - y^2}(\omega \to 0)$$

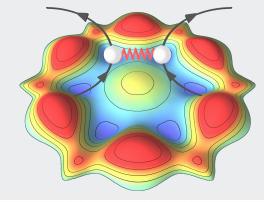
- always useful/meaningful?
- what happens when we lose such simple single-particle picture?

2nd part of my talk correlated TIs twisted-bilayer TMD



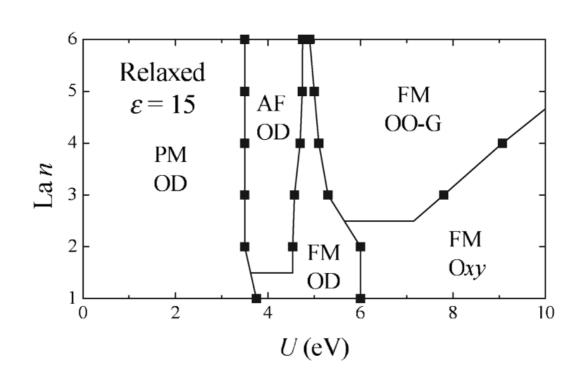


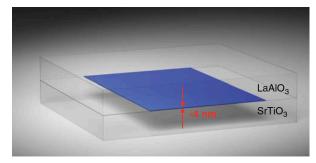
Oxide Heterostructures



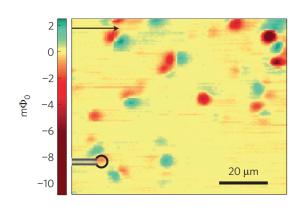
- highly active field, even several years after the first pioneering contributions by H. Hwang, A. Millis, etc... [previous talk by Divine Kumah]
- platform for superconductivity and magnetism
- d-electrons: strong responses beyond bulk phase diagrams

LaTiO₃/SrTiO₃
Okamoto, *et al.* PRL (2006)

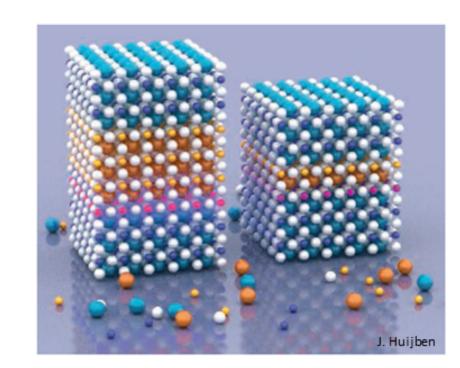




Mannhart et al. MRS Bull. (2008)

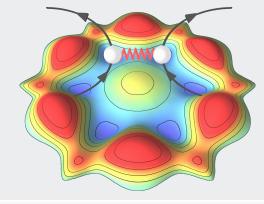


Bert et al. Nature Phys. (2011)





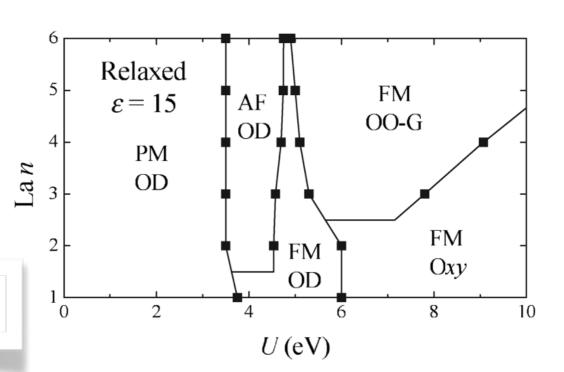
Oxide Heterostructures

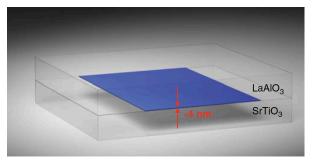


- highly active field, even several years after the first pioneering contributions by H. Hwang, A. Millis, etc... [previous talk by Divine Kumah]
- platform for superconductivity and magnetism
- *d*-electrons: strong responses beyond bulk phase diagrams

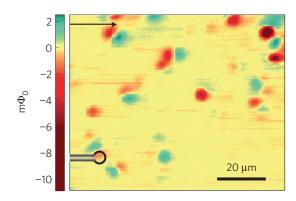
LaTiO₃/SrTiO₃
Okamoto, *et al.* PRL (2006)

thickness-induced metal-insulator transitions

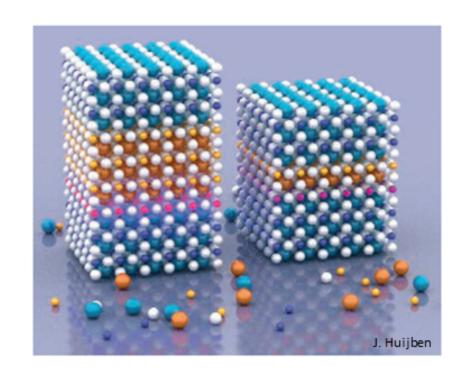




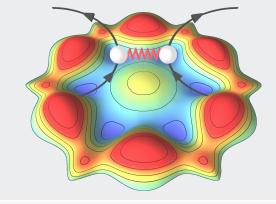
Mannhart et al. MRS Bull. (2008)



Bert et al. Nature Phys. (2011)



Oxide Heterostructures



• highly active field, even several years after the first pioneering contributions by H. Hwang, A. Millis, etc... [previous talk by Divine Kumah]

*t*₂*g*

- platform for superconductivity and magnetism
- *d*-electrons: strong responses beyond bulk phase diagrams

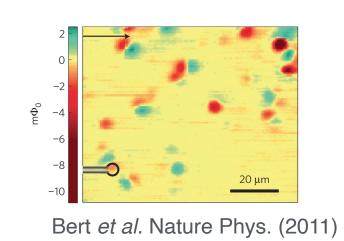
LaTiO₃/SrTiO₃

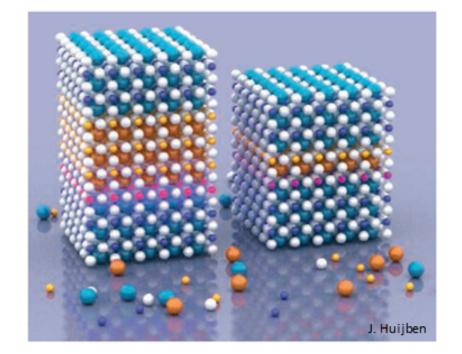
Okamoto, et al. PRL (2006)

Solve and the second sec

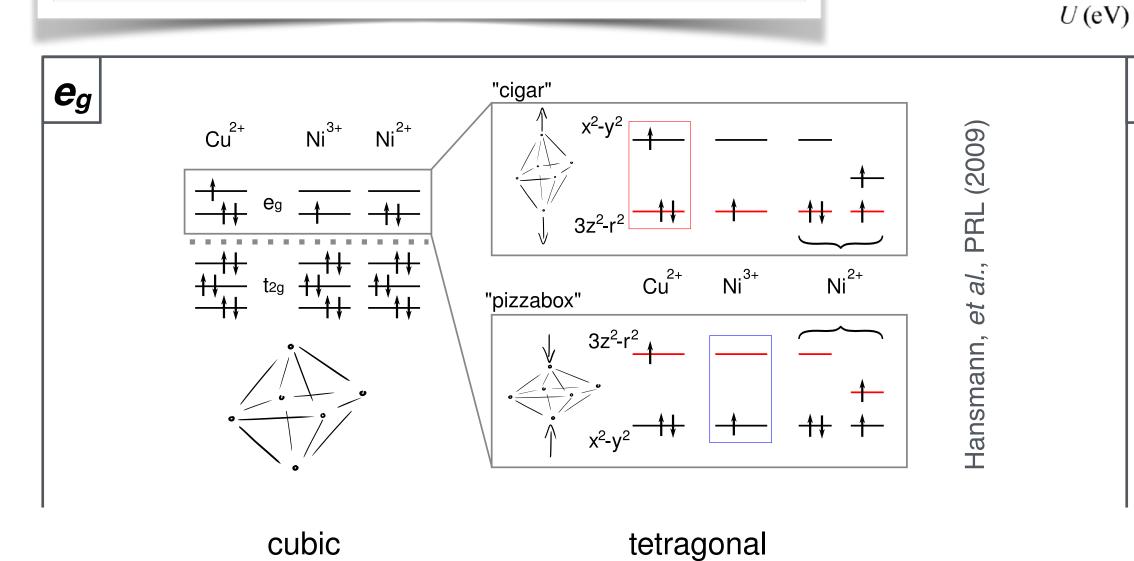
LaAlO₃
SrTiO₃

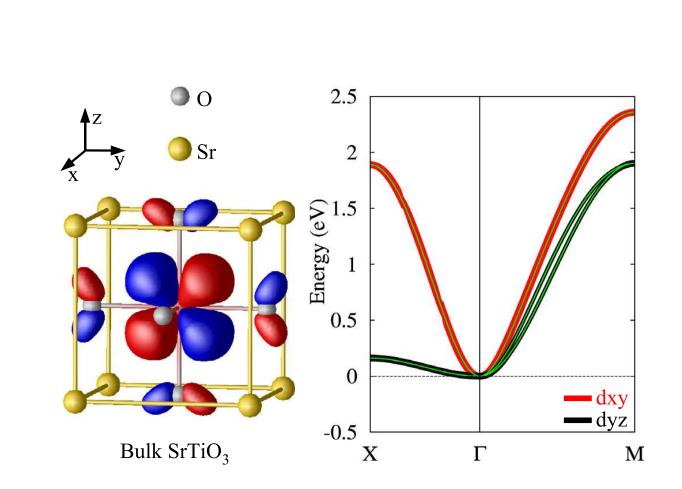
Mannhart et al. MRS Bull. (2008)

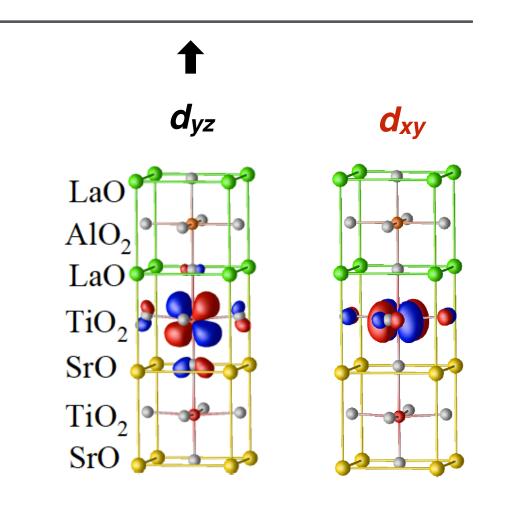




thickness-induced metal-insulator transitions

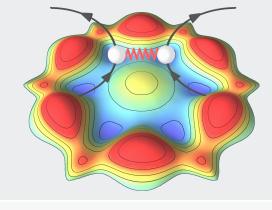




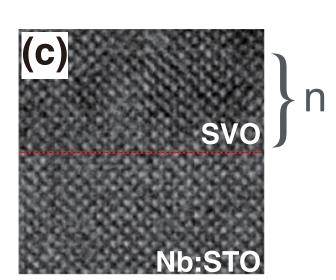


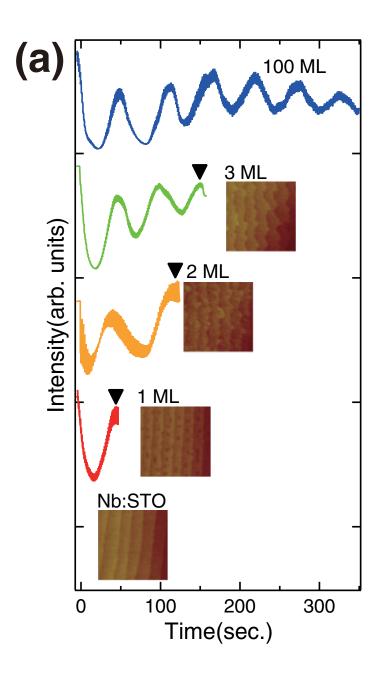


Thickness-induced metal-insulator transition in vanadium think films

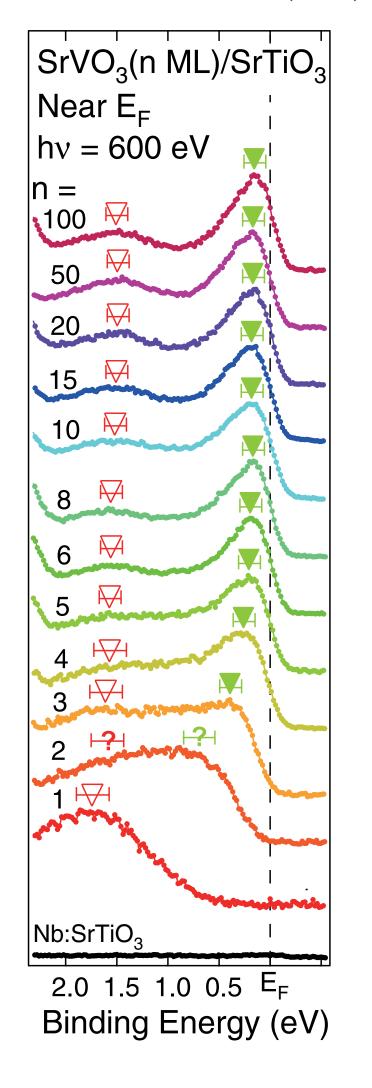


- thin films of good-old-friend SrVO₃ on SrTiO₃
- weight at E_F disappears for small values of n



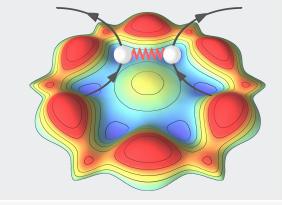


Yoshimatsu, et al., PRL (2010)



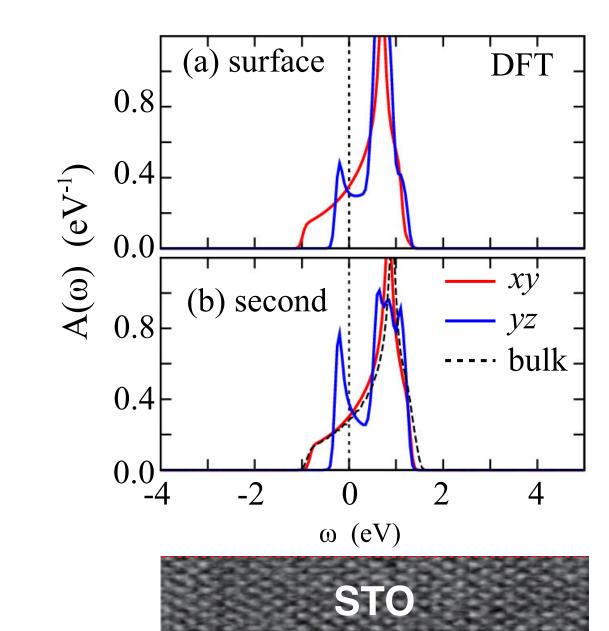


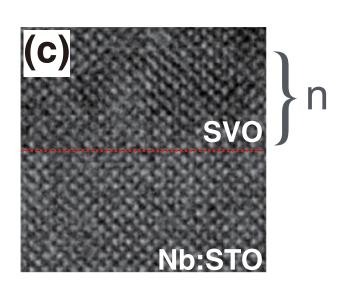
Thickness-induced metal-insulator transition in vanadium think films

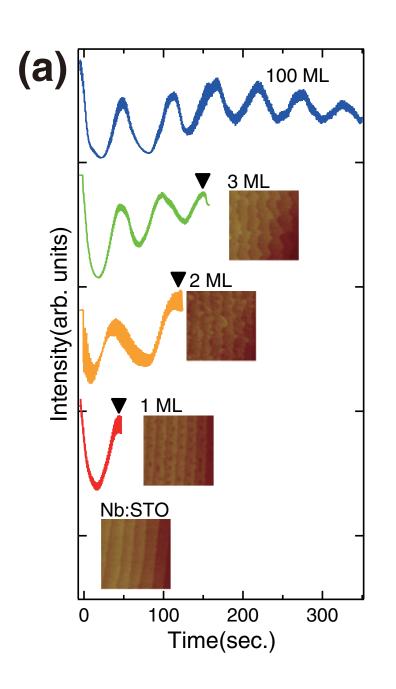


- thin films of good-old-friend SrVO₃ on SrTiO₃
- weight at E_F disappears for small values of n

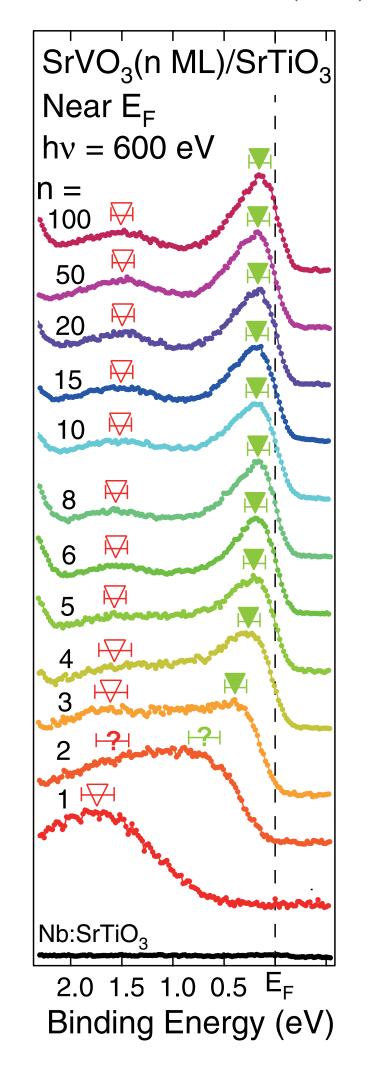
- SVO thin films in DFT (n=2)
- splitting of the t_{2g}





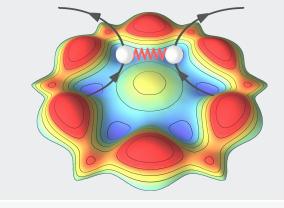


Yoshimatsu, et al., PRL (2010)

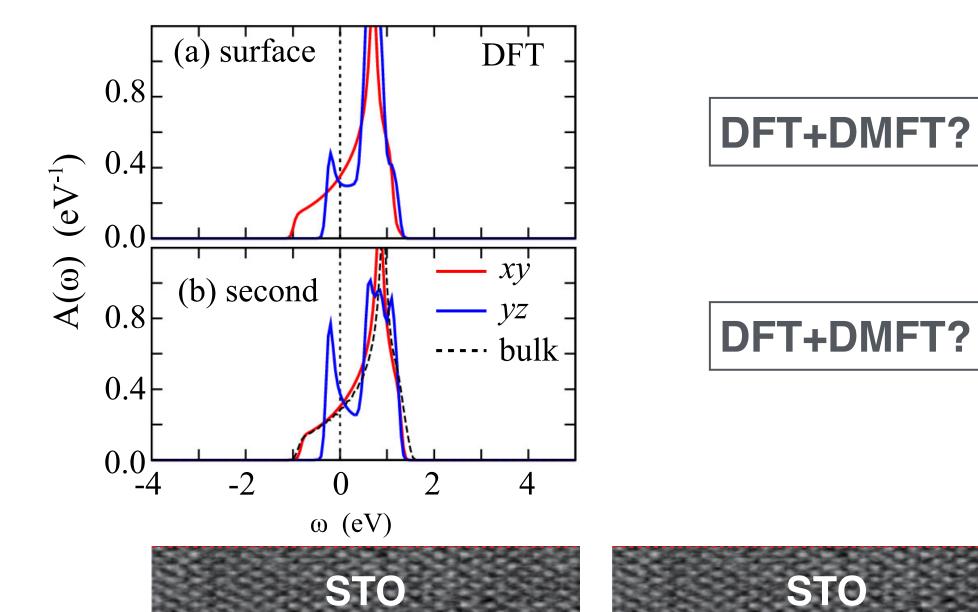


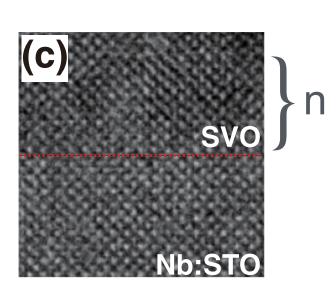


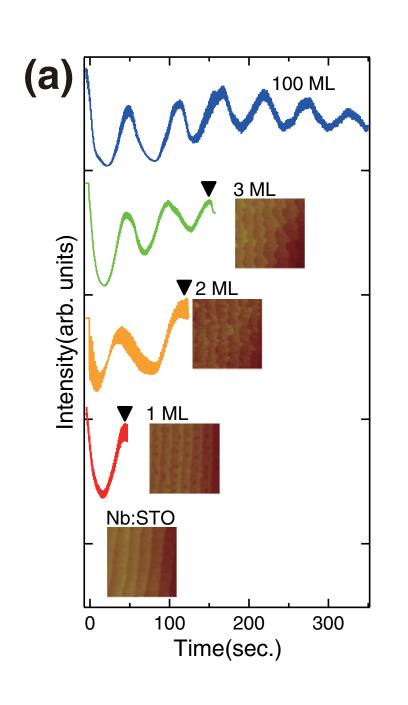
Thickness-induced metal-insulator transition in vanadium think films



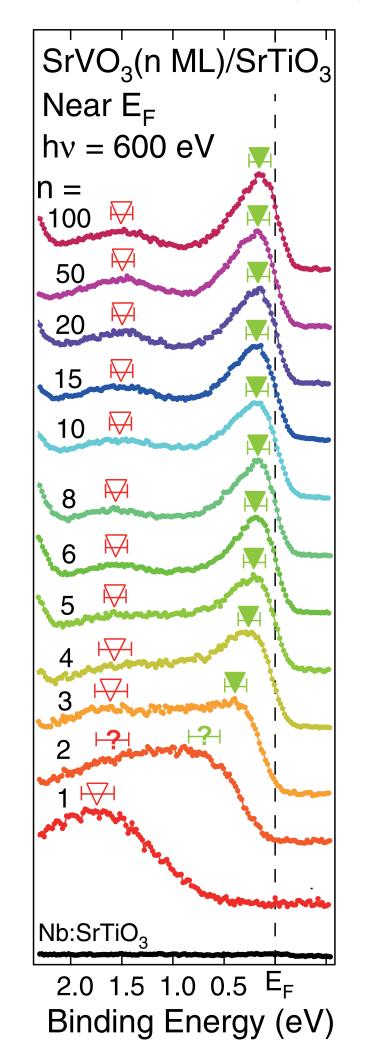
- thin films of good-old-friend SrVO₃ on SrTiO₃
- weight at E_F disappears for small values of n
- SVO thin films in DFT (n=2)
- splitting of the t_{2g}





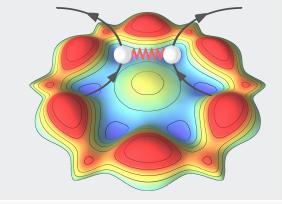


Yoshimatsu, et al., PRL (2010)





Device concept?



PRL **114,** 246401 (2015)

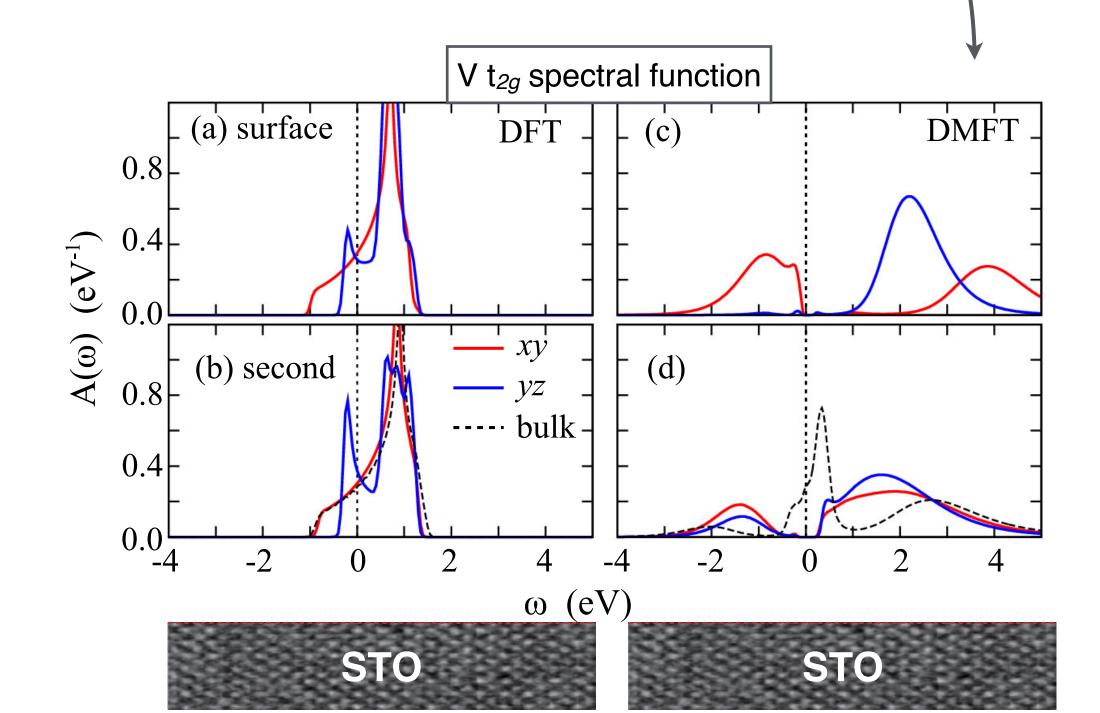
PHYSICAL REVIEW LETTERS

week ending 19 JUNE 2015

orbital polarization easy to switch ON and OFF! (thickness, pressure, strain, temperature, gating,...)

• 2 V-layers (n=2): insulating in DFT+DMFT

n=3 already metallic



Electronics with Correlated Oxides: SrVO₃/SrTiO₃ as a Mott Transistor

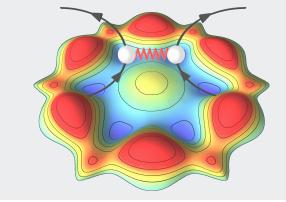
Zhicheng Zhong,¹ Markus Wallerberger,¹ Jan M. Tomczak,¹ Ciro Taranto,¹ Nicolaus Parragh,² Alessandro Toschi,¹ Giorgio Sangiovanni,² and Karsten Held¹

$$\Delta_{\text{eff}}^{t_{2g}} = \Delta_{\text{DFT}}^{t_{2g}} + \text{Re}\Sigma_{yz/xz}(\omega \to 0) - \text{Re}\Sigma_{xy}(\omega \to 0)$$





Device concept?



PRL **114**, 246401 (2015)

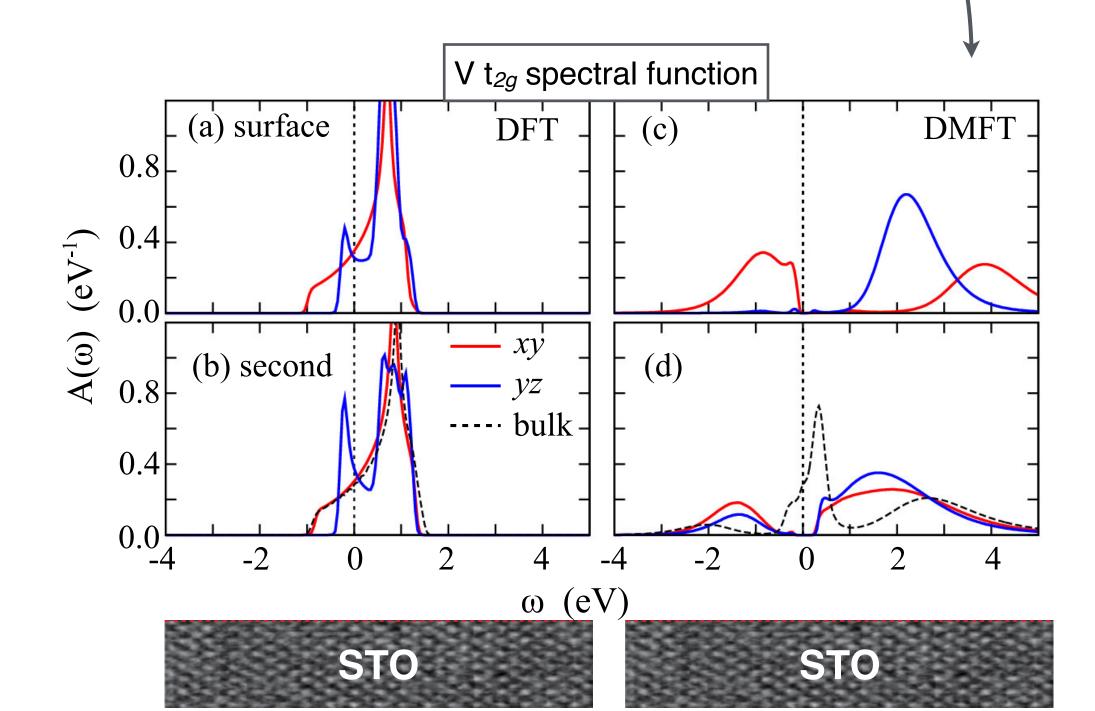
PHYSICAL REVIEW LETTERS

week ending 19 JUNE 2015

orbital polarization easy to switch ON and OFF!
 (thickness, pressure, strain, temperature, gating,...)

• 2 V-layers (n=2): insulating in DFT+DMFT

n=3 already metallic

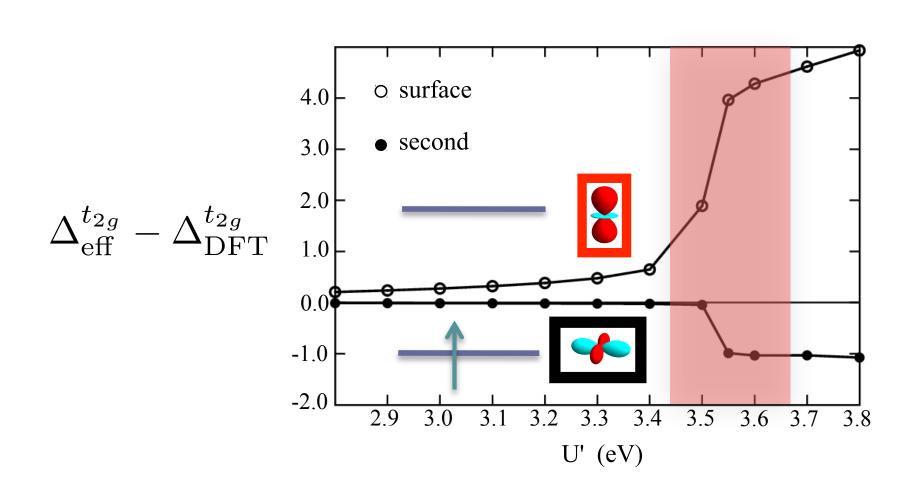


Electronics with Correlated Oxides: SrVO₃/SrTiO₃ as a Mott Transistor

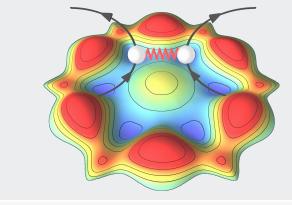
Zhicheng Zhong,¹ Markus Wallerberger,¹ Jan M. Tomczak,¹ Ciro Taranto,¹ Nicolaus Parragh,² Alessandro Toschi,¹ Giorgio Sangiovanni,² and Karsten Held¹

$$\Delta_{\text{eff}}^{t_{2g}} = \Delta_{\text{DFT}}^{t_{2g}} + \text{Re}\Sigma_{yz/xz}(\omega \to 0) - \text{Re}\Sigma_{xy}(\omega \to 0)$$

- smooth correction within Hartree-Fock ($Re\Sigma\sim Un$)
- DMFT: non-linear effects/first-order behavior



Device concept?



PRL **114,** 246401 (2015)

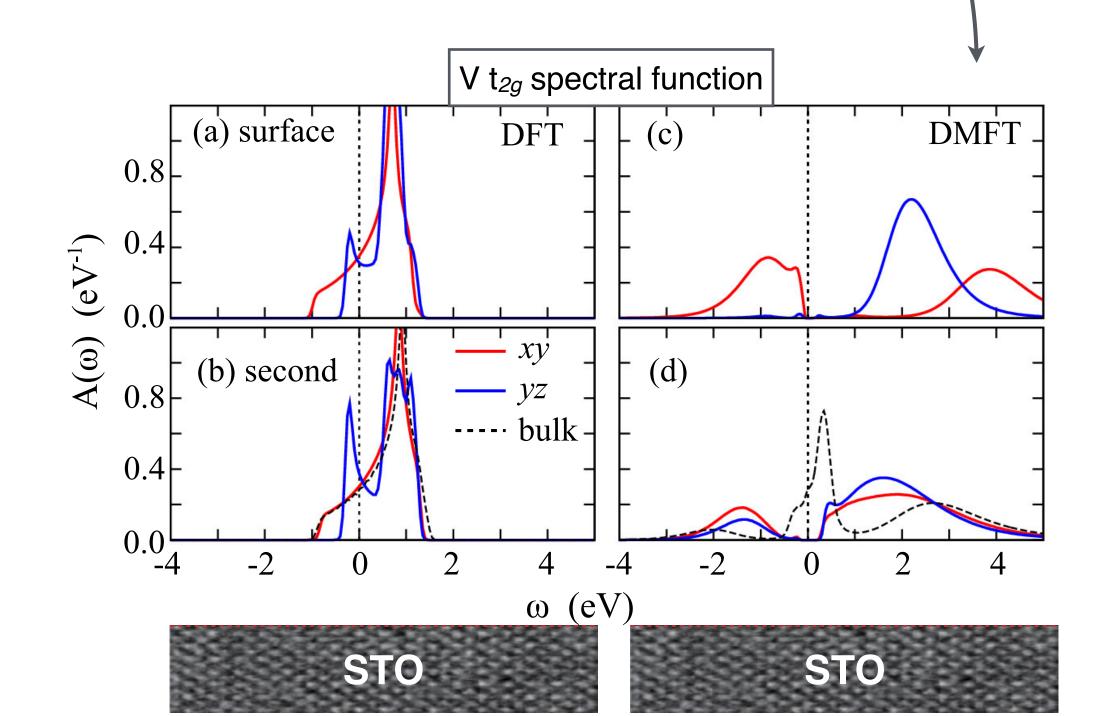
PHYSICAL REVIEW LETTERS

week ending 19 JUNE 2015

orbital polarization easy to switch ON and OFF!
 (thickness, pressure, strain, temperature, gating,...)

• 2 V-layers (n=2): insulating in DFT+DMFT

n=3 already metallic

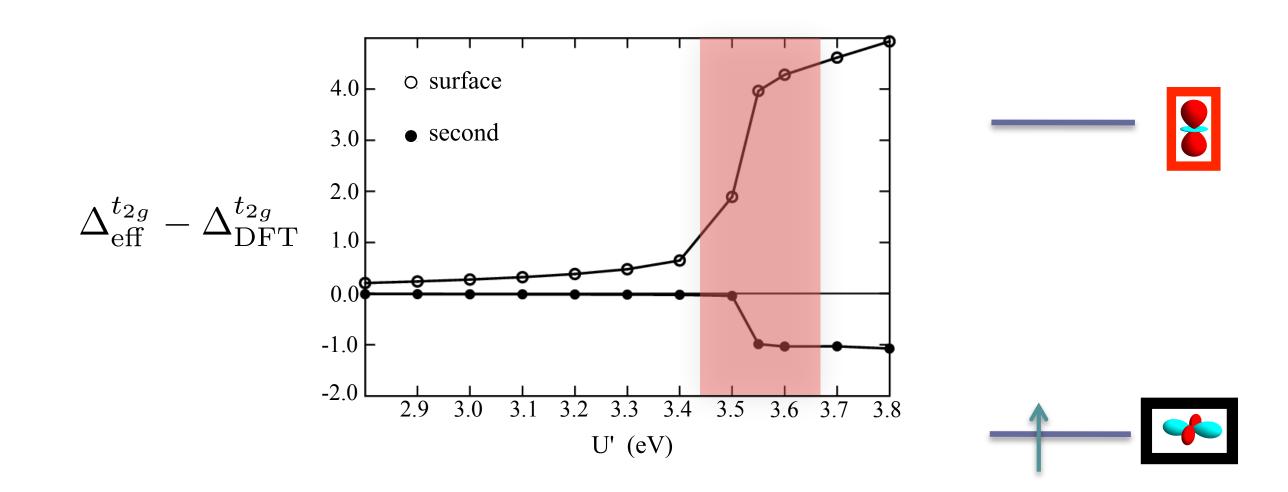


Electronics with Correlated Oxides: SrVO₃/SrTiO₃ as a Mott Transistor

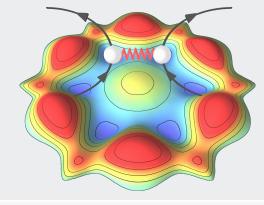
Zhicheng Zhong,¹ Markus Wallerberger,¹ Jan M. Tomczak,¹ Ciro Taranto,¹ Nicolaus Parragh,² Alessandro Toschi,¹ Giorgio Sangiovanni,² and Karsten Held¹

$$\Delta_{\text{eff}}^{t_{2g}} = \Delta_{\text{DFT}}^{t_{2g}} + \text{Re}\Sigma_{yz/xz}(\omega \to 0) - \text{Re}\Sigma_{xy}(\omega \to 0)$$

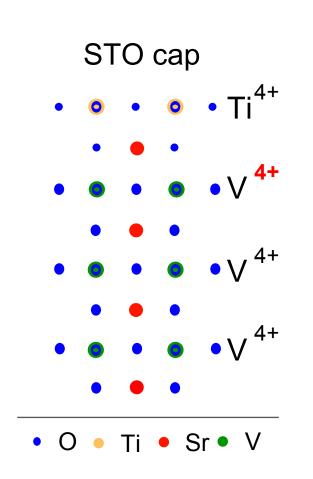
- smooth correction within Hartree-Fock ($Re\Sigma\sim Un$)
- DMFT: non-linear effects/first-order behavior

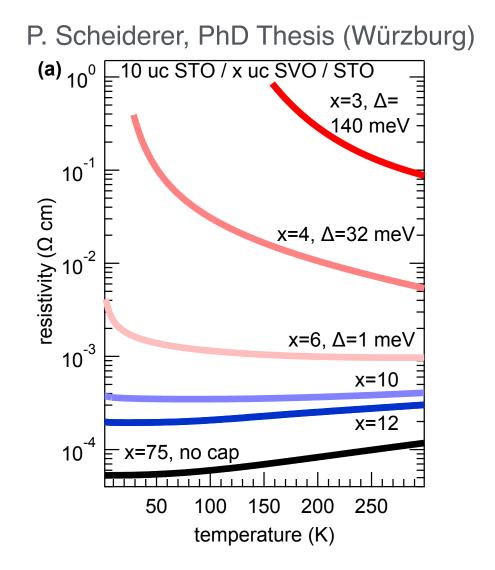


Surface of SVO thin films



- termination for SrVO₃ fims on SrTiO₃
- $VO_2 + \sqrt{2} \times \sqrt{2}$ oxygen reconstruction
- solution: capping!

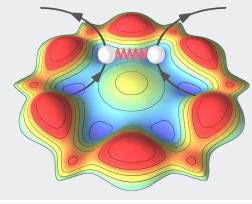




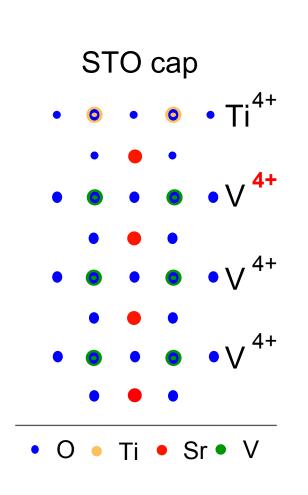
surprising result:
 critical thickness much bigger than
 Yoshimatsu, et al. and DFT+DMFT

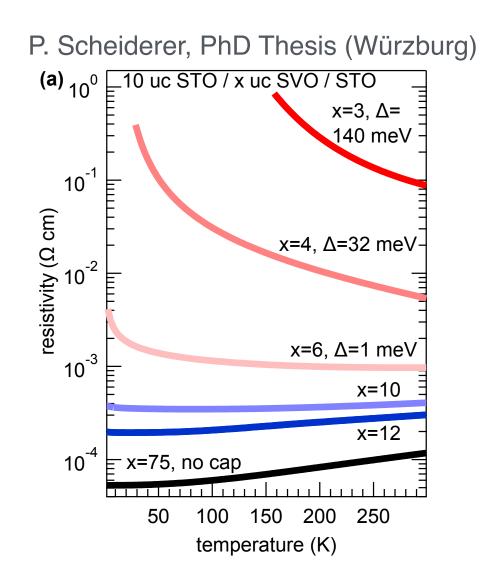
Julius-MaximiliansUNIVERSITÄT WÜRZBURG

Surface of SVO thin films



- termination for SrVO₃ fims on SrTiO₃
- $VO_2 + \sqrt{2} \times \sqrt{2}$ oxygen reconstruction
- solution: capping!

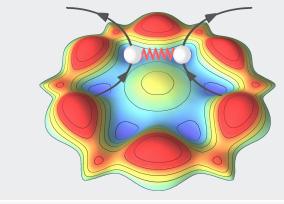




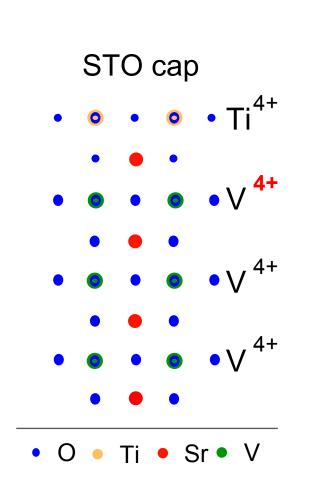
surprising result:
 critical thickness much bigger than
 Yoshimatsu, et al. and DFT+DMFT

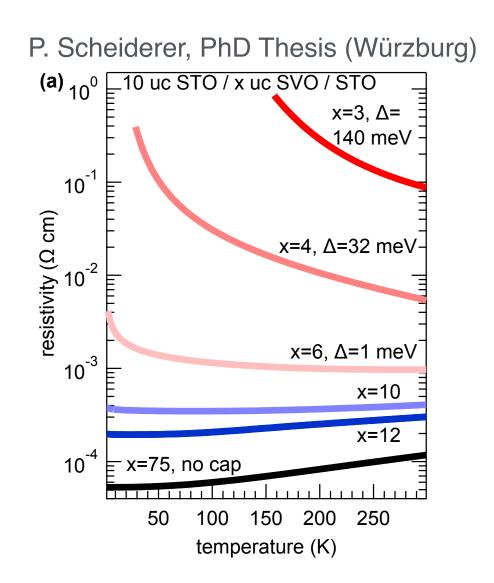
- many-body correction to $\Delta_{
 m DFT}^{t_{2g}}$ determines orbital polarization
- enhancement, but in which direction? importance of the sign of $\Delta_{
 m DFT}^{t_{2g}}$
- work in progress (Würzburg + Vienna)

Surface of SVO thin films



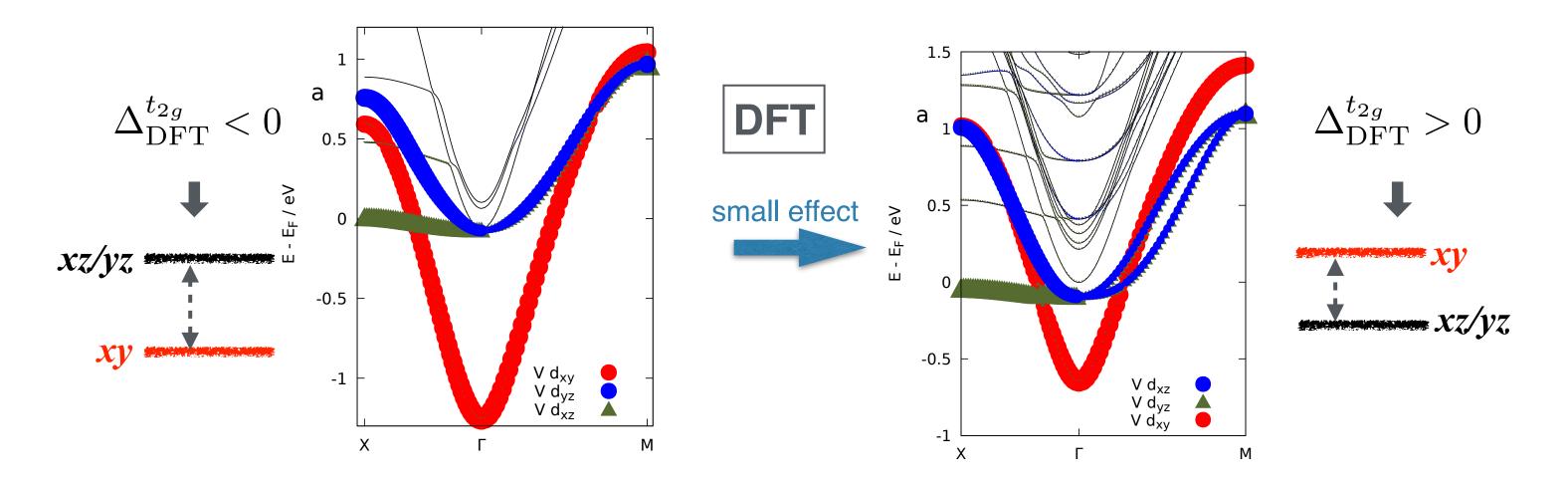
- termination for SrVO₃ fims on SrTiO₃
- $VO_2 + \sqrt{2} \times \sqrt{2}$ oxygen reconstruction
- solution: capping!





surprising result:
 critical thickness much bigger than
 Yoshimatsu, et al. and DFT+DMFT

- many-body correction to $\Delta_{
 m DFT}^{t_{2g}}$ determines orbital polarization
- enhancement, but in which direction? importance of the sign of $\Delta_{
 m DFT}^{t_{2g}}$
- work in progress (Würzburg + Vienna)

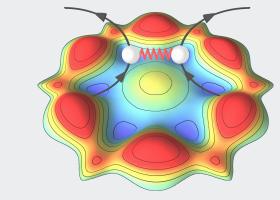


SrO termination (i.e. complete octahedra)

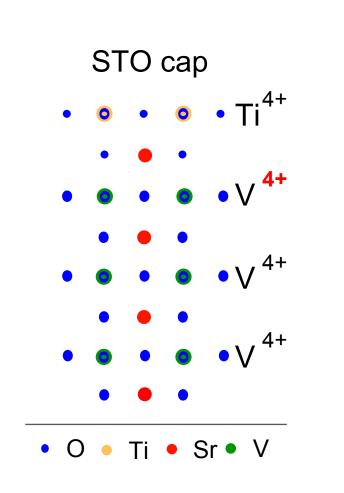
ideal VO₂ termination

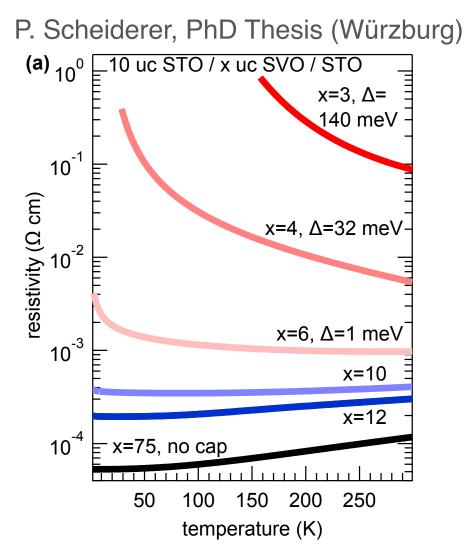
DFT+DMFT

Surface of SVO thin films



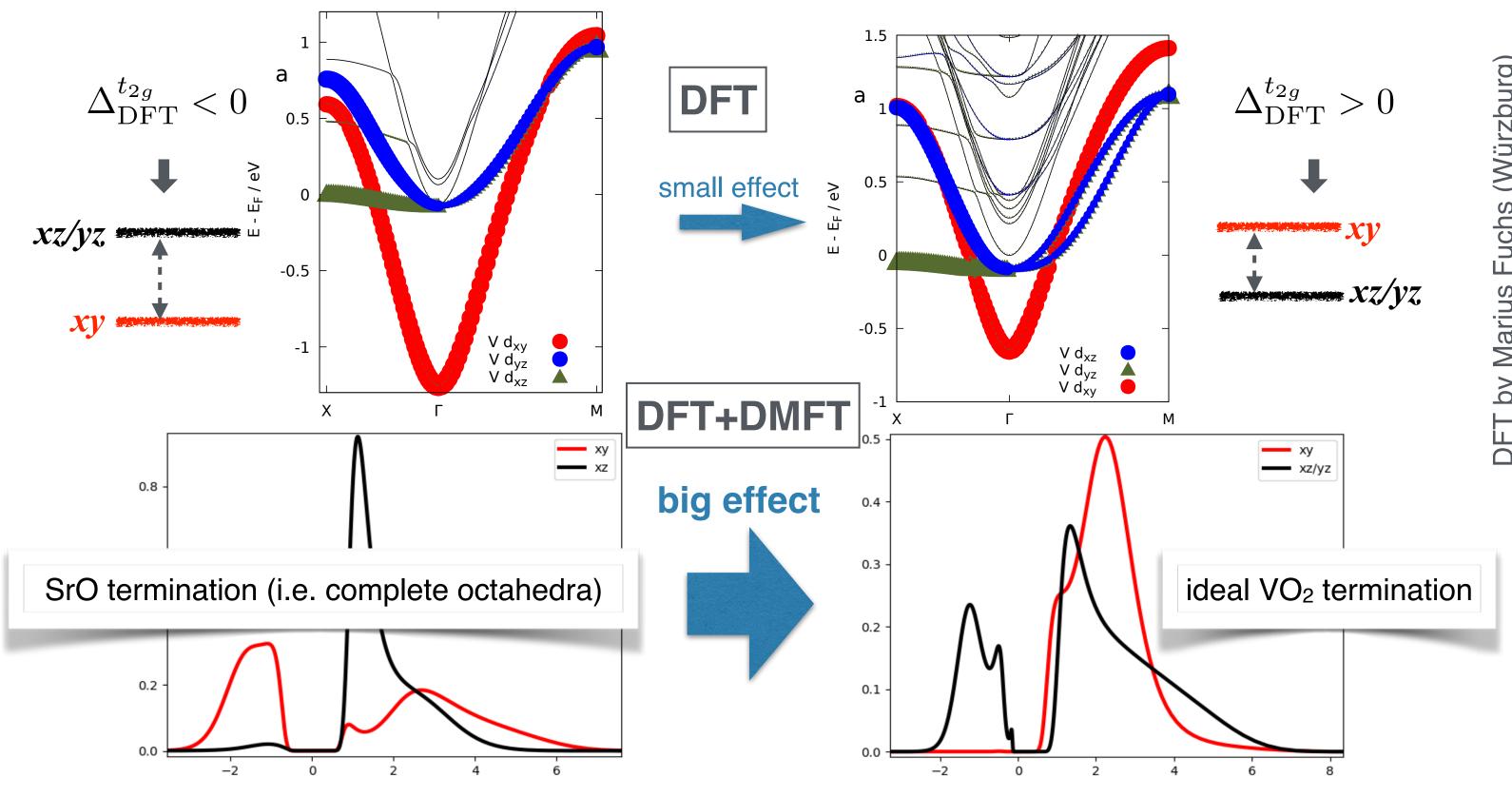
- termination for SrVO₃ fims on SrTiO₃
- $VO_2 + \sqrt{2} \times \sqrt{2}$ oxygen reconstruction
- solution: capping!





surprising result:
 critical thickness much bigger than
 Yoshimatsu, et al. and DFT+DMFT

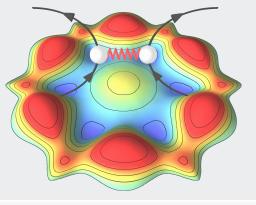
- many-body correction to $\Delta_{
 m DFT}^{t_{2g}}$ determines orbital polarization
- enhancement, but in which direction? importance of the sign of $\Delta_{
 m DFT}^{t_{2g}}$
- work in progress (Würzburg + Vienna)

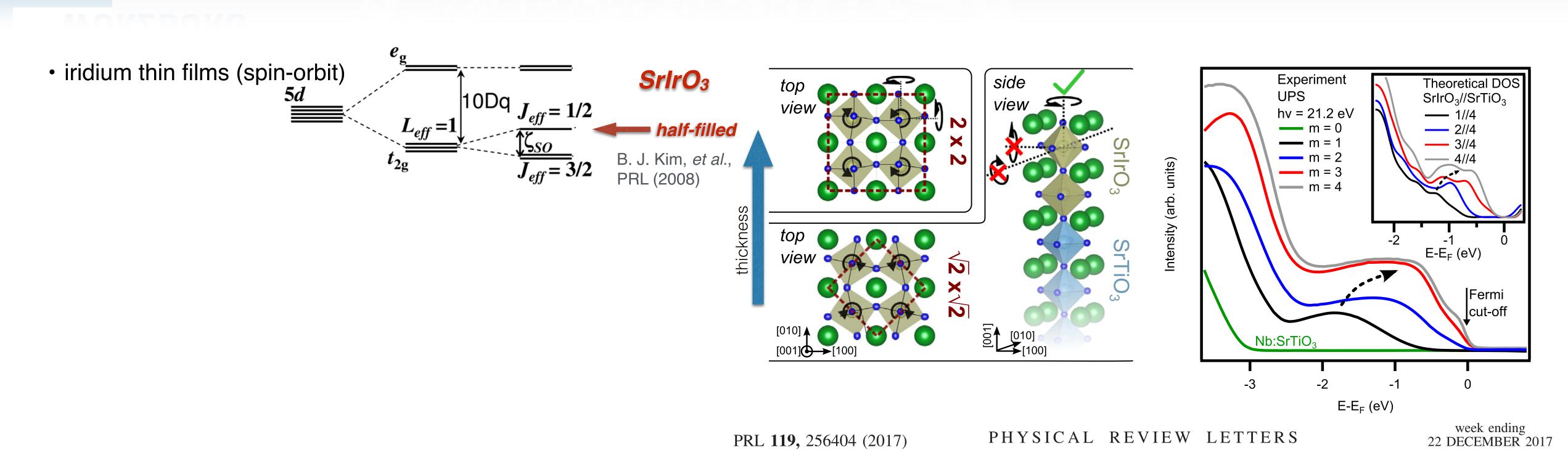


DFT by Marius Fuchs (Würzburg) spectra by Matthias Pickem (group of K. Held and J. DFT+DMFT

Julius-MaximiliansUNIVERSITÄT WÜRZBURG

other examples of thickness induced MIT





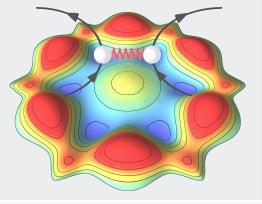
Dimensionality-Driven Metal-Insulator Transition in Spin-Orbit-Coupled SrIrO₃

P. Schütz, D. Di Sante, L. Dudy, J. Gabel, M. Stübinger, M. Kamp, Y. Huang, M. Capone, M.-A. Husanu, N. V. N. Strocov, G. Sangiovanni, M. Sing, and R. Claessen

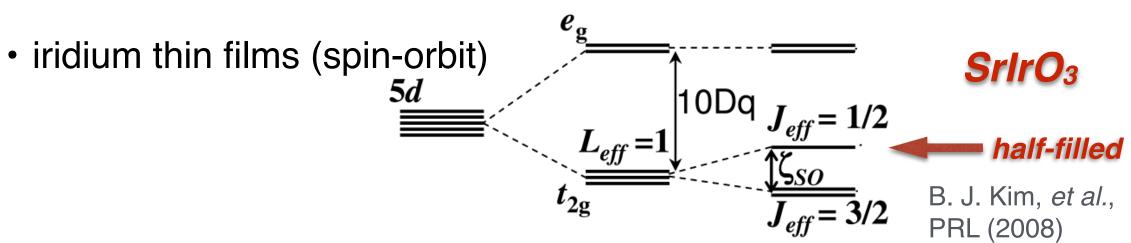
Julius-MaximiliansUNIVERSITÄT WÜRZBURG

other examples of thickness induced MIT

PRL **119,** 256404 (2017)

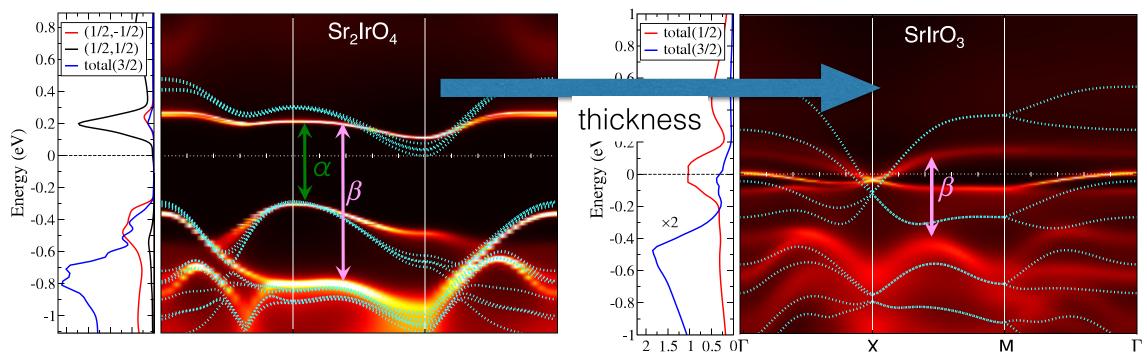


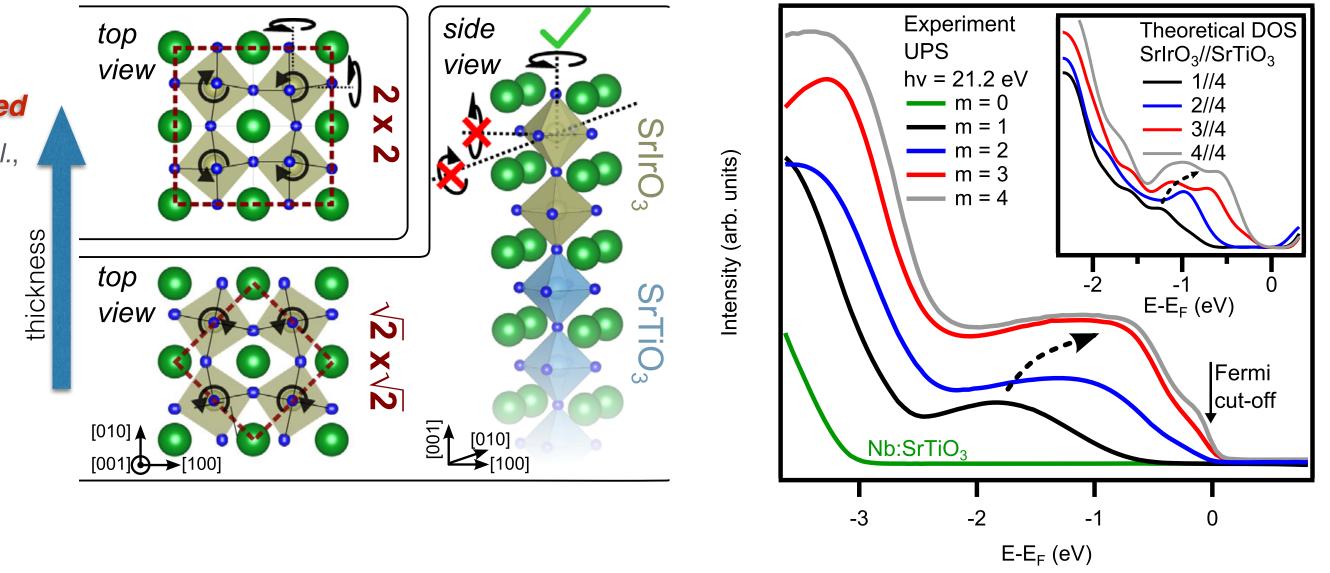
week ending 22 DECEMBER 2017



mimicking the Ruddlesden-Popper series:

H. Zhang, et al. PRL (2013)





Dimensionality-Driven Metal-Insulator Transition in Spin-Orbit-Coupled SrIrO₃

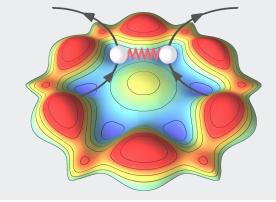
PHYSICAL REVIEW LETTERS

P. Schütz,¹ D. Di Sante,² L. Dudy,¹ J. Gabel,¹ M. Stübinger,¹ M. Kamp,¹ Y. Huang,³ M. Capone,⁴ M.-A. Husanu,^{5,6} V. N. Strocov,⁶ G. Sangiovanni,² M. Sing,¹ and R. Claessen¹



other examples of thickness induced MIT

PRL **119**, 256404 (2017)



Theoretical DOS

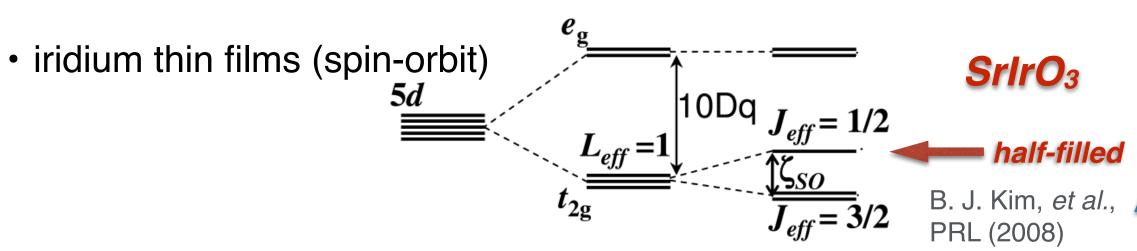
SrlrO₃//SrTiO₃

-1 E-E_F (eV)

Fermi

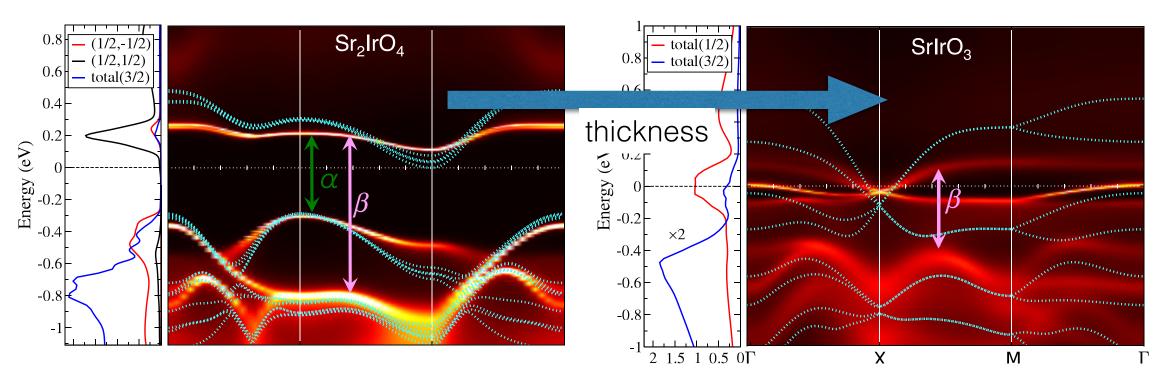
cut-off

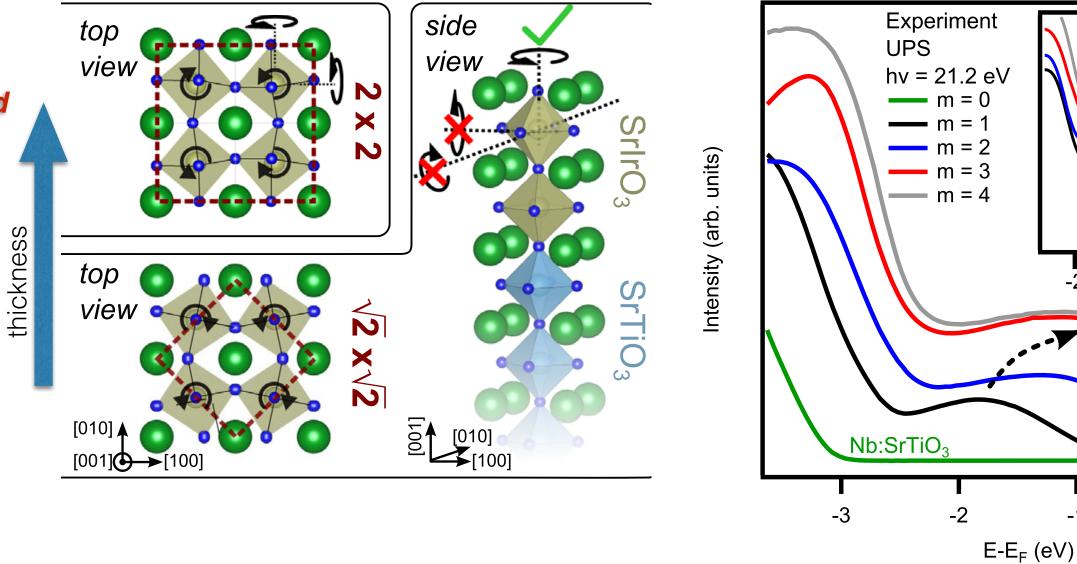
week ending 22 DECEMBER 2017



mimicking the Ruddlesden-Popper series:

H. Zhang, et al. PRL (2013)





Dimensionality-Driven Metal-Insulator Transition in Spin-Orbit-Coupled SrIrO₃

PHYSICAL REVIEW LETTERS

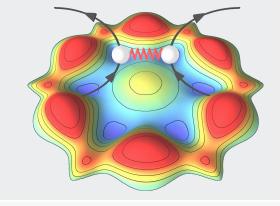
P. Schütz,¹ D. Di Sante,² L. Dudy,¹ J. Gabel,¹ M. Stübinger,¹ M. Kamp,¹ Y. Huang,³ M. Capone,⁴ M.-A. Husanu,^{5,6} V. N. Strocov,⁶ G. Sangiovanni,² M. Sing,¹ and R. Claessen¹

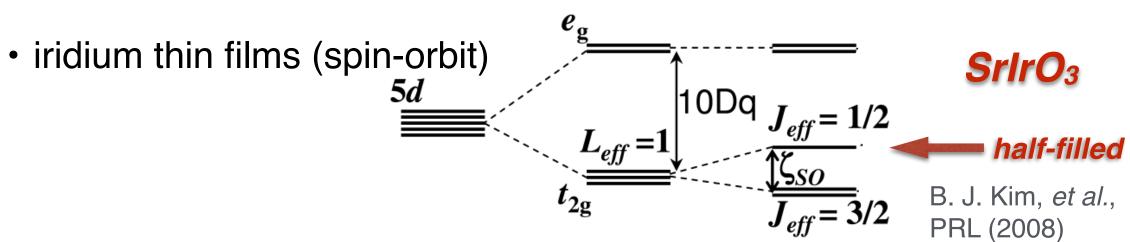
- interplay between SOC, structural distortions and magnetism
- see poster by Severino Adler on 5d³ Osmates





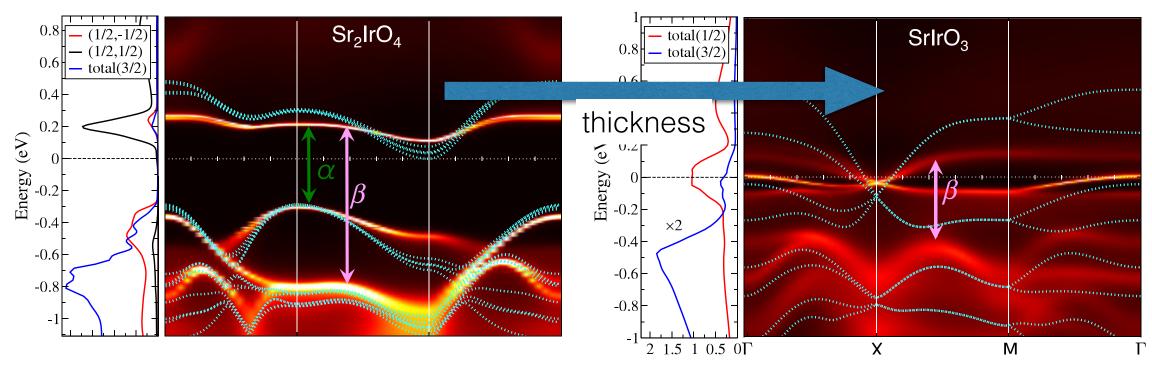
other examples of thickness induced MIT

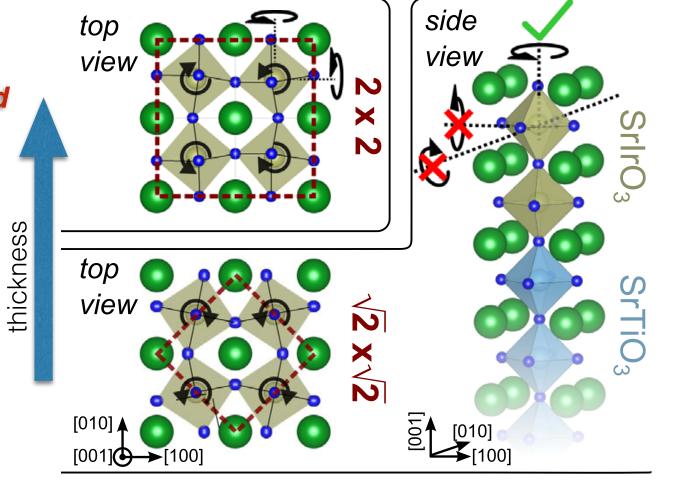


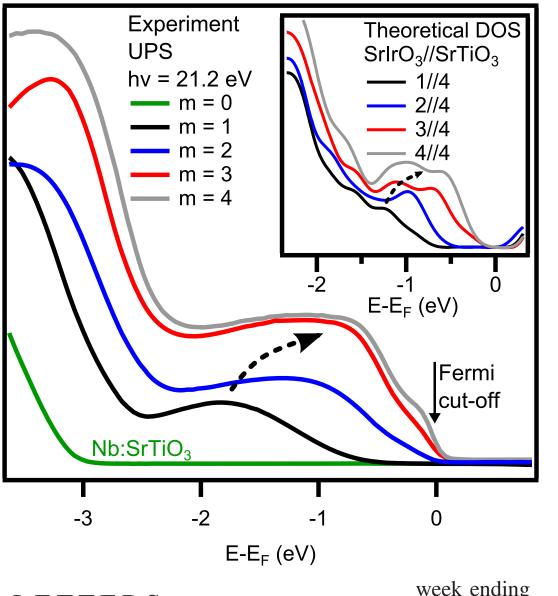


mimicking the Ruddlesden-Popper series:

H. Zhang, et al. PRL (2013)





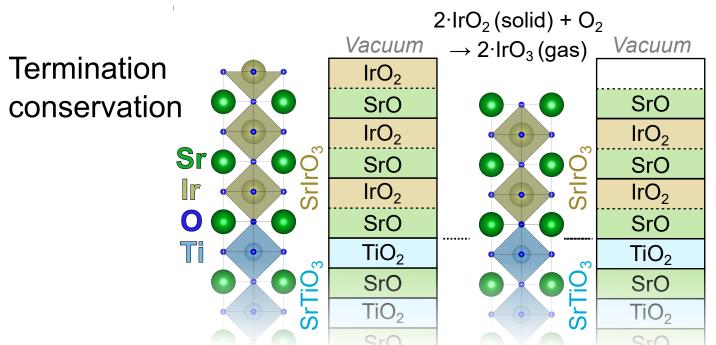


PRL **119**, 256404 (2017)

PHYSICAL REVIEW LETTERS

Intensity (arb. units)

week ending 22 DECEMBER 2017



Termination conversion

confirmed by DFT+U calculations (Domenico Di Sante)

P. Schütz, et al. submitted

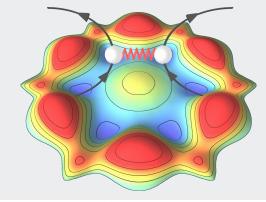
Dimensionality-Driven Metal-Insulator Transition in Spin-Orbit-Coupled SrIrO₃

P. Schütz,¹ D. Di Sante,² L. Dudy,¹ J. Gabel,¹ M. Stübinger,¹ M. Kamp,¹ Y. Huang,³ M. Capone,⁴ M.-A. Husanu,^{5,6} V. N. Strocov,⁶ G. Sangiovanni,² M. Sing,¹ and R. Claessen¹

- interplay between SOC, structural distortions and magnetism
- see poster by Severino Adler on 5d³ Osmates





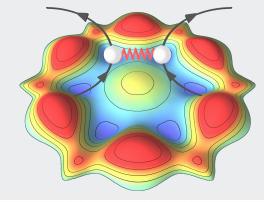


- in nickel heterostructures: when the *d*-shell gets closer to d⁸
- Hund's tendecy to high-spin triplet Mott insulator in the e_g doublet

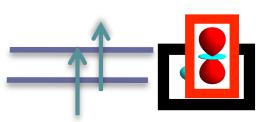




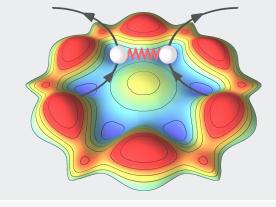




- in nickel heterostructures: when the *d*-shell gets closer to d⁸
- Hund's tendecy to high-spin triplet Mott insulator in the e_g doublet







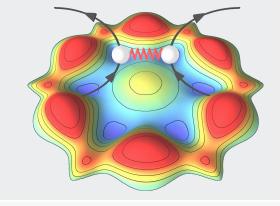
- in nickel heterostructures: when the *d*-shell gets closer to d⁸
- Hund's tendecy to high-spin triplet Mott insulator in the e_g doublet
- HgTe (BHZ model) A. Bernevig, et al. Science (2006)
- Two orbitals (spin 1/2)
- Time-reversal
- U(1)_{spin} symmetry

$$\mathbf{H}_{4\times4}(\mathbf{k}) = \begin{pmatrix} \hat{h}_0(\mathbf{k}) & \mathbf{k} \\ \mathbf{h}_0(\mathbf{k}) & \hat{h}_0^*(-\mathbf{k}) \end{pmatrix}$$

Pauli matrices in orbital space
$$\hat{h}_0(\mathbf{k}) = \vec{d}(\mathbf{k}) \cdot \vec{\tau}$$

$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \cos k_x - \cos k_y \end{pmatrix}$$

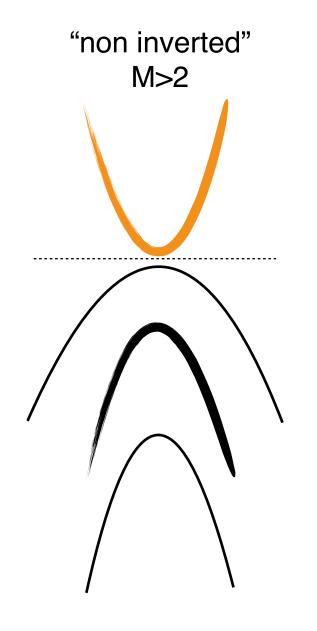


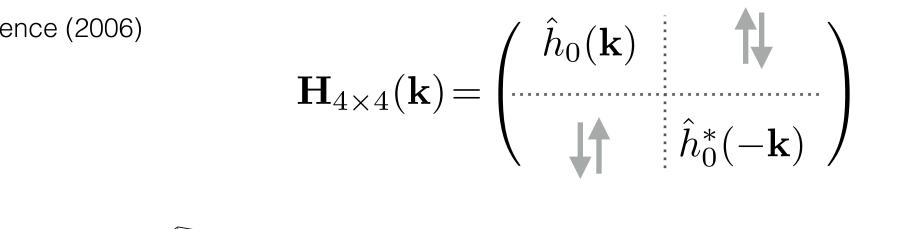


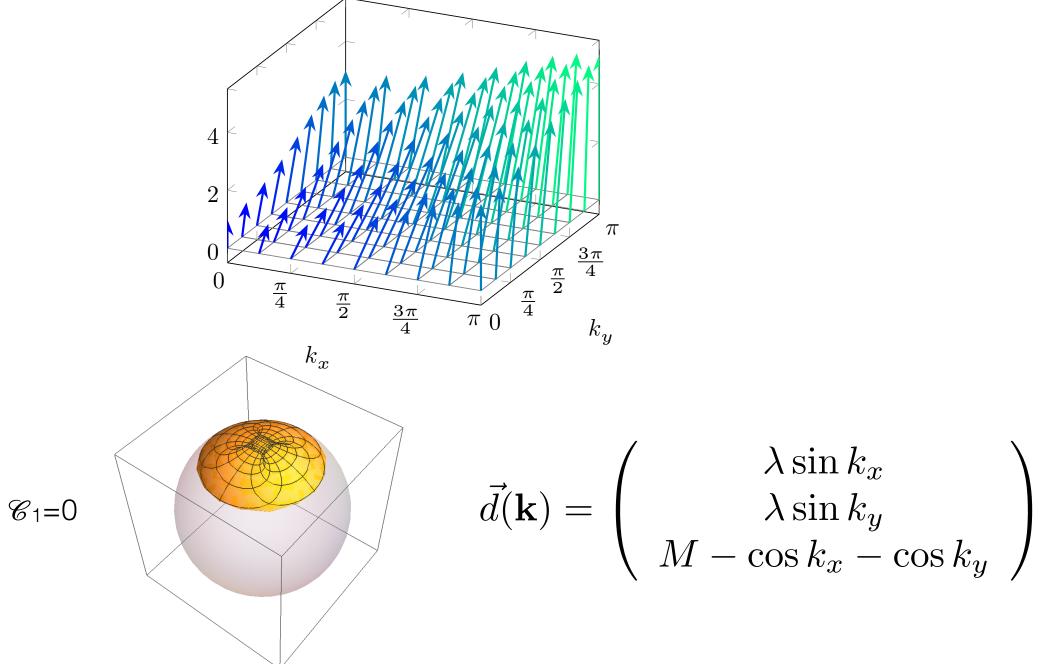
- in nickel heterostructures: when the *d*-shell gets closer to d⁸
- Hund's tendecy to high-spin triplet Mott insulator in the e_g doublet

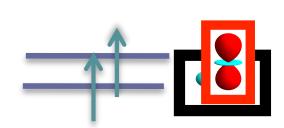


- Two orbitals (spin 1/2)
- Time-reversal
- U(1)_{spin} symmetry



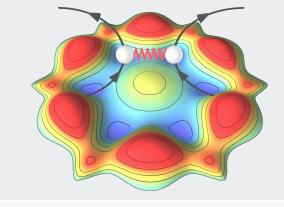






Pauli matrices in orbital space $\hat{h}_0(\mathbf{k}) = \vec{d}(\mathbf{k}) \cdot \vec{\tau}$

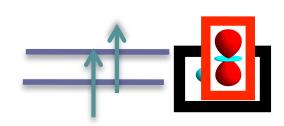




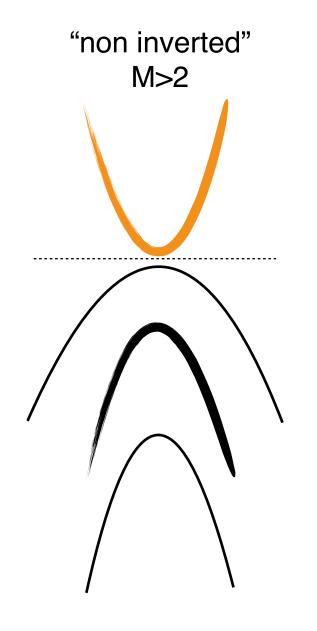
• in nickel heterostructures: when the *d*-shell gets closer to d⁸

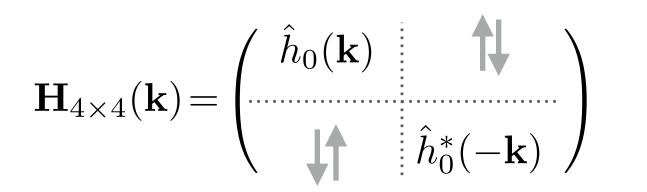
 $\mathscr{C}_1=0$

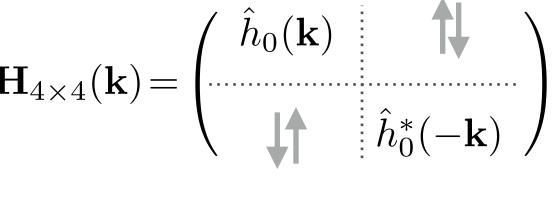
• Hund's tendecy to high-spin triplet Mott insulator in the e_g doublet

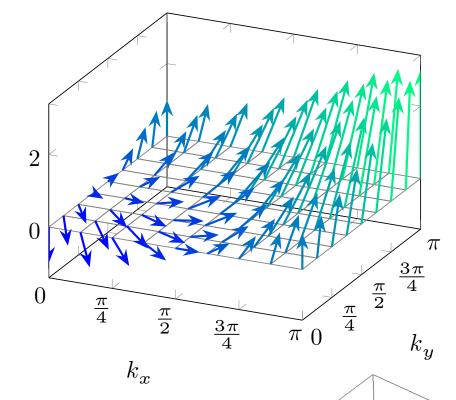


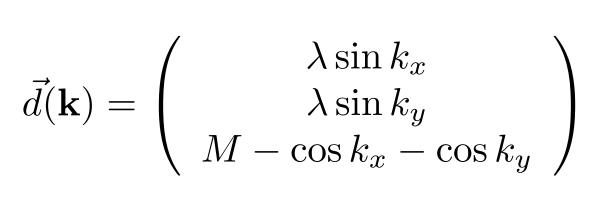
- HgTe (BHZ model) A. Bernevig, et al. Science (2006)
- Two orbitals (s p) and spin 1/2
- Time-reversal
- U(1)_{spin} symmetry

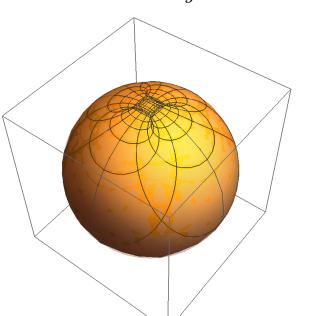




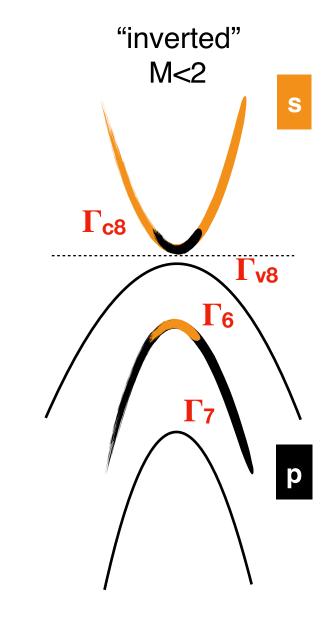






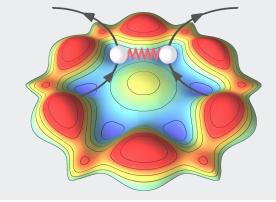


 $\hat{h}_0(\mathbf{k}) = \vec{d}(\mathbf{k}) \cdot \vec{\tau}$



Pauli matrices in orbital space

BHZ-Hubbard model



- orbital structure of interaction for the BHZ + Hubbard U, Hund J
- simplest local interaction term [see A. Georges, L. de' Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

$$\mathcal{H}_{int}(i) = (U - J) \frac{N_i(N_i - 1)}{2} - J \left(\frac{N_i^2}{4} + S_{zi}^2 - 2T_{zi}^2 \right)$$





$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \cos k_x - \cos k_y \end{pmatrix}$$

Y. Tada, et al. PRB (2012)

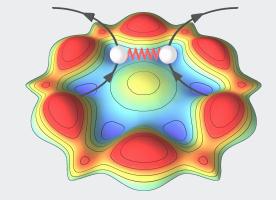
T. Yoshida, et al. PRB (2012)

L. Wang, *et al.* EPL (2012)

J. Budich, et al. PRB (2012)

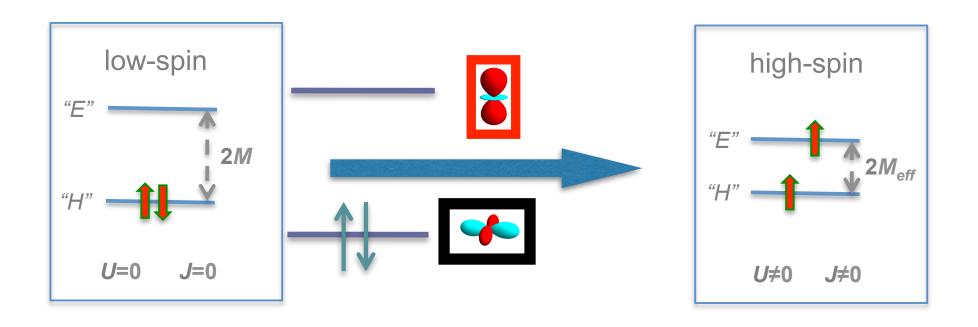
J. Budich, *et al.* PRB (2013)





- orbital structure of interaction for the BHZ + Hubbard *U*, Hund *J*
- simplest local interaction term [see A. Georges, L. de' Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

$$\mathcal{H}_{int}(i) = (U - J) \frac{N_i(N_i - 1)}{2} - J \left(\frac{N_i^2}{4} + S_{zi}^2 - 2T_{zi}^2 \right)$$



$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \cos k_x - \cos k_y \end{pmatrix}$$

Y. Tada, et al. PRB (2012)

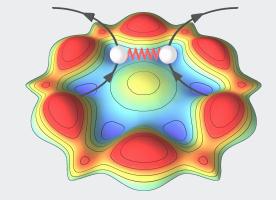
T. Yoshida, et al. PRB (2012)

L. Wang, *et al.* EPL (2012)

J. Budich, *et al.* PRB (2012)

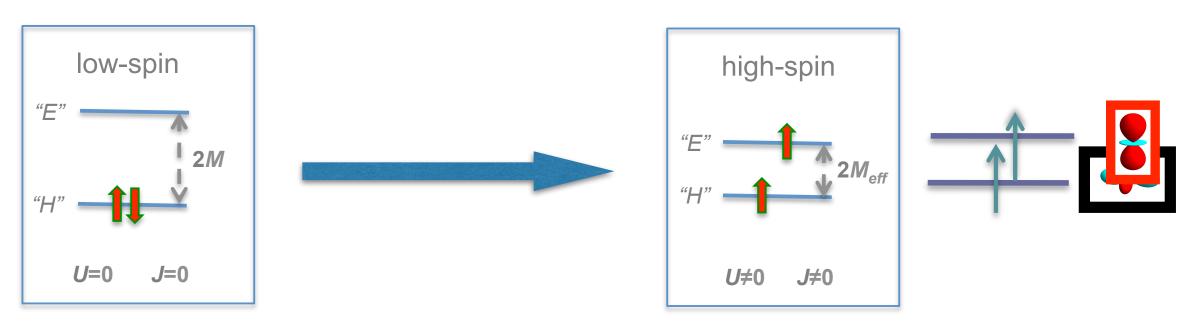
J. Budich, *et al.* PRB (2013)





- orbital structure of interaction for the BHZ + Hubbard *U*, Hund *J*
- simplest local interaction term [see A. Georges, L. de' Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

$$\mathcal{H}_{\text{int}}(i) = (U - J) \frac{N_{i}(N_{i} - 1)}{2} - J \left(\frac{N_{i}^{2}}{4} + S_{zi}^{2} - 2T_{zi}^{2} \right)$$



- Intra- + inter-orbital *J* (Hund) interaction
- *U* suppresses double occupancies \Longrightarrow reduced effective orbital splitting $M_{\rm eff}$

$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$

zeroth-order correction: Meff

Y. Tada, et al. PRB (2012)

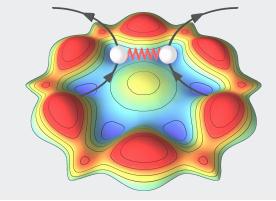
T. Yoshida, et al. PRB (2012)

L. Wang, *et al.* EPL (2012)

J. Budich, *et al.* PRB (2012)

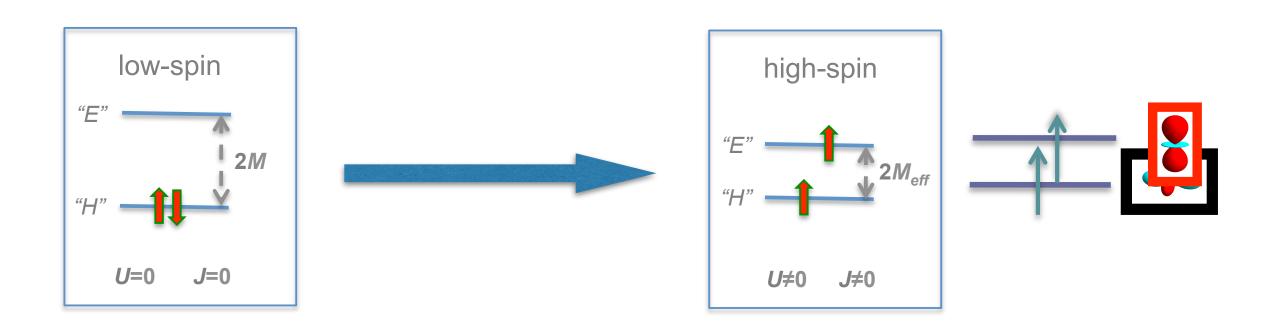
J. Budich, *et al.* PRB (2013)





- orbital structure of interaction for the BHZ + Hubbard *U*, Hund *J*
- simplest local interaction term [see A. Georges, L. de' Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

$$\mathcal{H}_{int}(i) = (U - J) \frac{N_i(N_i - 1)}{2} - J \left(\frac{N_i^2}{4} + S_{zi}^2 - 2T_{zi}^2 \right)$$

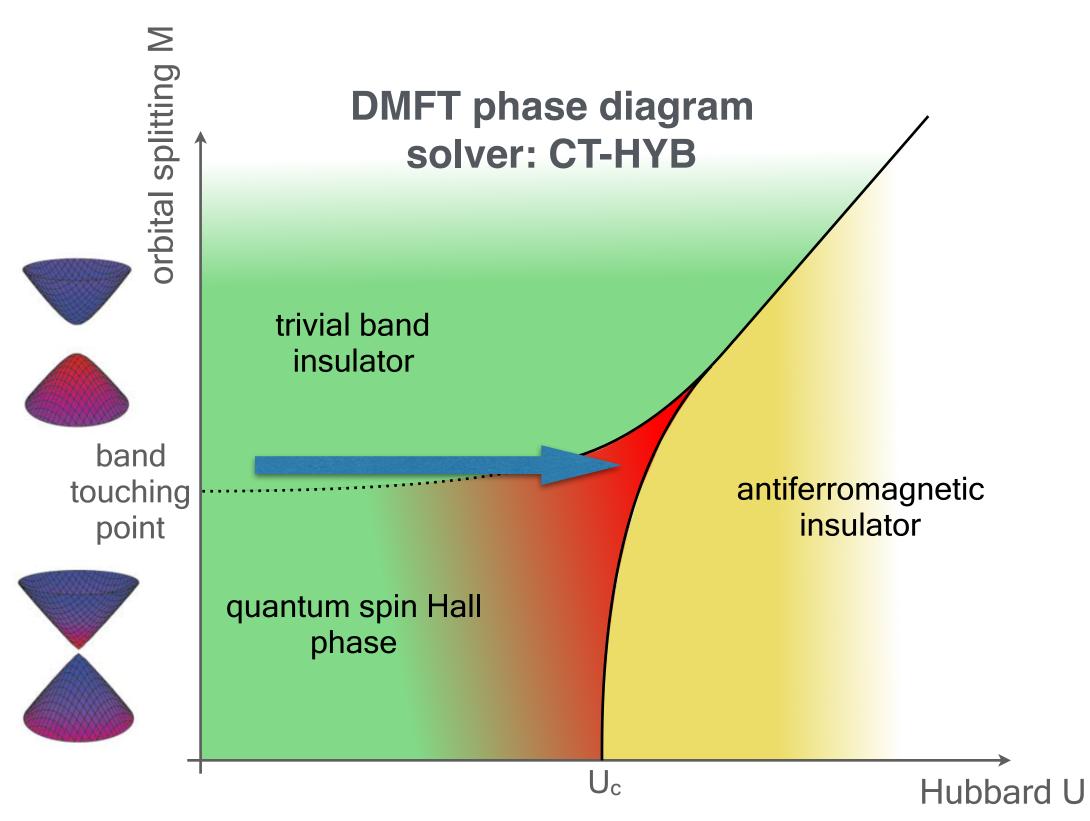


- Intra- + inter-orbital *J* (Hund) interaction
- U suppresses double occupancies \Longrightarrow reduced effective orbital splitting $M_{\rm eff}$
- QSH extends at large-*U* and large-*M*, as a "precursor" of the high-spin phase

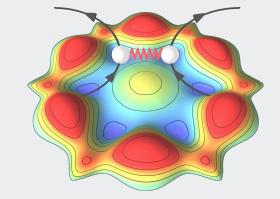
$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$

zeroth-order correction: Meff

- Y. Tada, et al. PRB (2012)
- T. Yoshida, et al. PRB (2012)
- L. Wang, *et al.* EPL (2012)
- J. Budich, *et al.* PRB (2012)
- J. Budich, et al. PRB (2013)

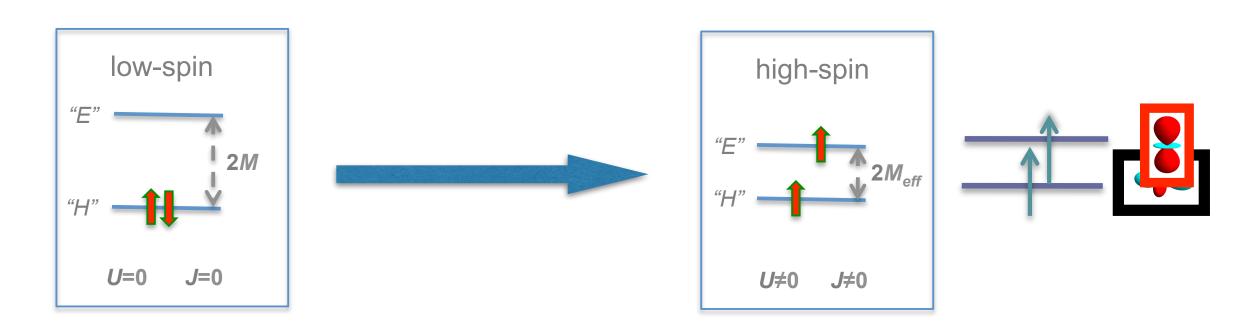






- orbital structure of interaction for the BHZ + Hubbard *U*, Hund *J*
- simplest local interaction term [see A. Georges, L. de' Medici and J. Mravlje, Annu. Rev. Condens. Matter Phys. (2013)]

$$\mathcal{H}_{int}(i) = (U - J) \frac{N_i(N_i - 1)}{2} - J \left(\frac{N_i^2}{4} + S_{zi}^2 - 2T_{zi}^2 \right)$$

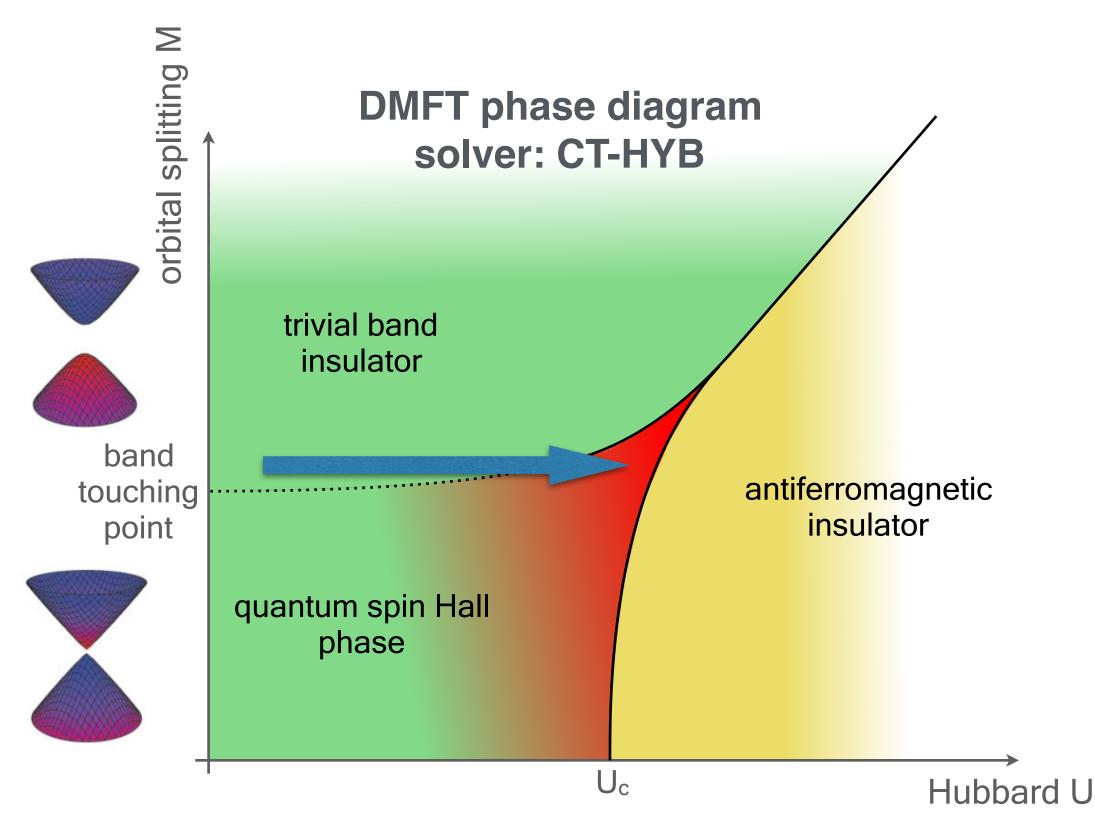


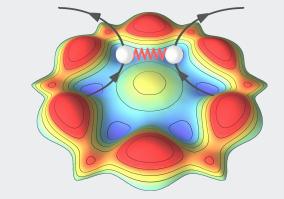
- Intra- + inter-orbital J (Hund) interaction
- U suppresses double occupancies \Longrightarrow reduced effective orbital splitting $M_{\rm eff}$
- QSH extends at large-*U* and large-*M*, as a "precursor" of the high-spin phase
- ...but there is more to that: see color coding in the phase diagram!

$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$

zeroth-order correction: Meff

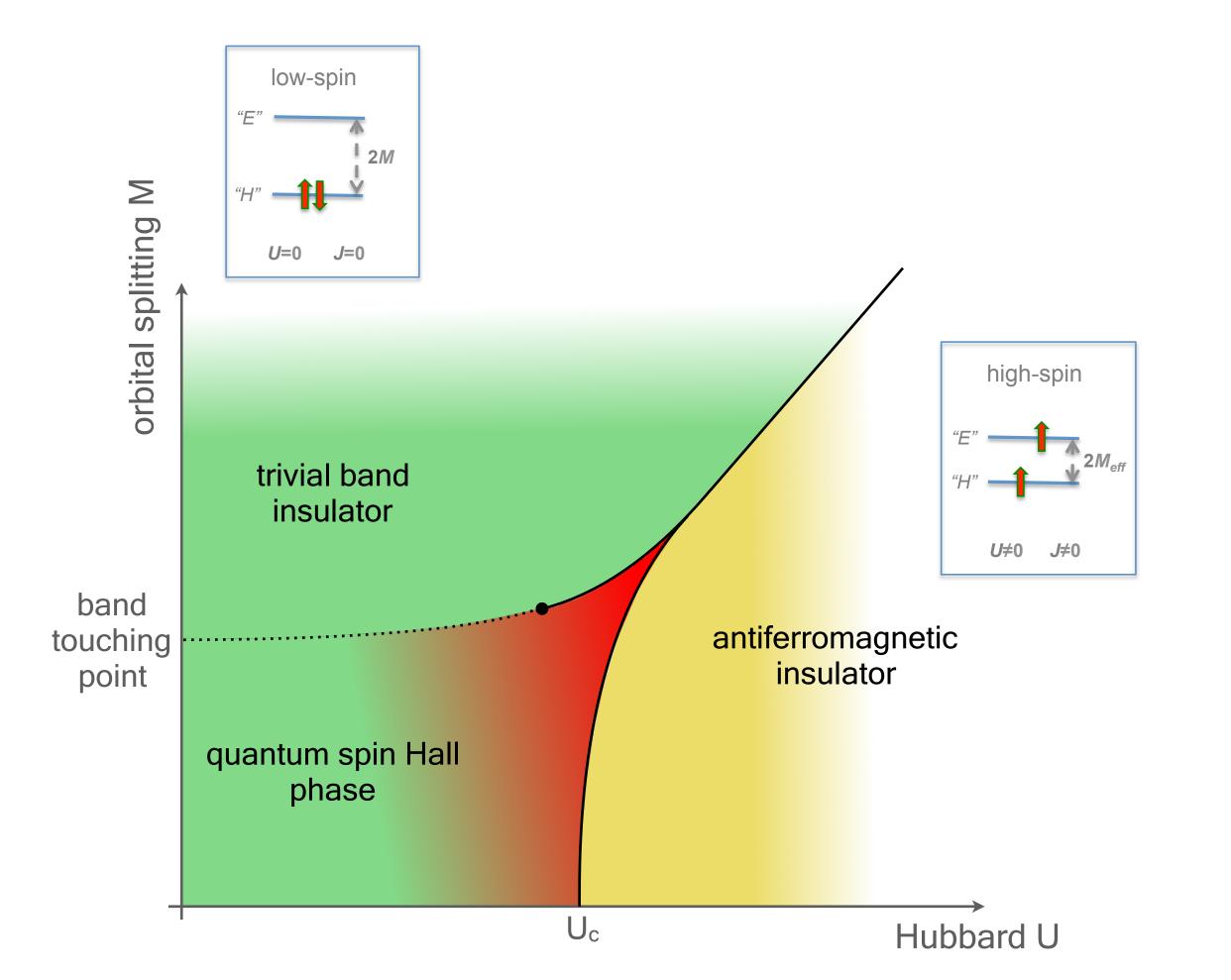
- Y. Tada, *et al.* PRB (2012)
- T. Yoshida, et al. PRB (2012)
- L. Wang, *et al.* EPL (2012)
- J. Budich, *et al.* PRB (2012)
- J. Budich, et al. PRB (2013)

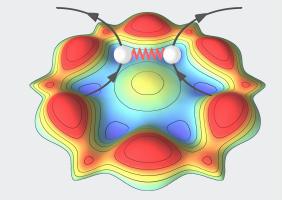




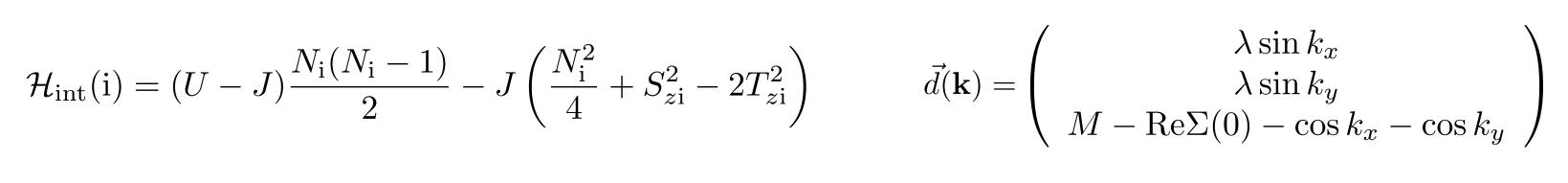
$$\mathcal{H}_{\text{int}}(i) = (U - J) \frac{N_{i}(N_{i} - 1)}{2} - J \left(\frac{N_{i}^{2}}{4} + S_{zi}^{2} - 2T_{zi}^{2} \right)$$

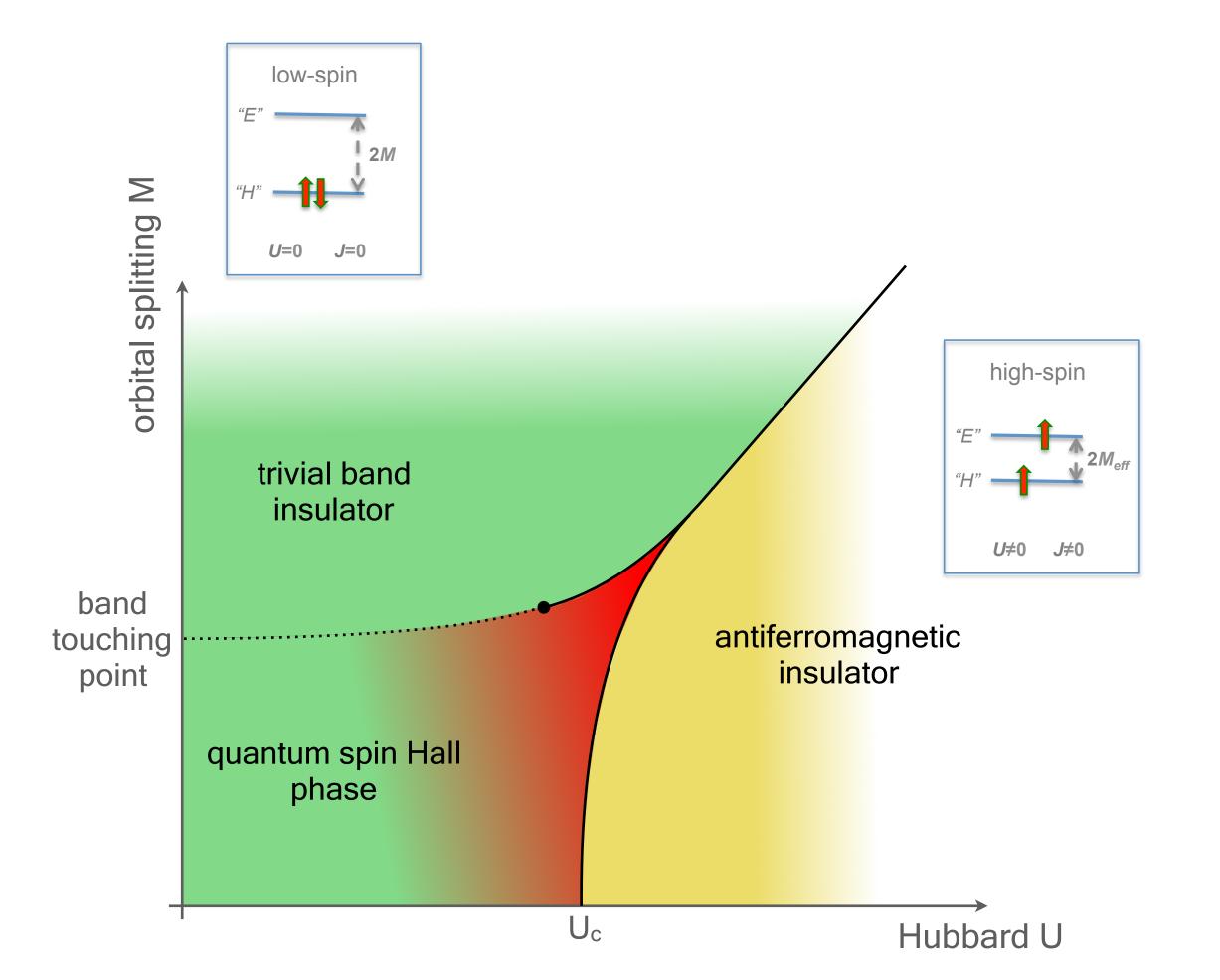
$$\mathcal{H}_{\text{int}}(\mathbf{i}) = (U - J) \frac{N_{\mathbf{i}}(N_{\mathbf{i}} - 1)}{2} - J \left(\frac{N_{\mathbf{i}}^2}{4} + S_{z\mathbf{i}}^2 - 2T_{z\mathbf{i}}^2 \right) \qquad \vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$



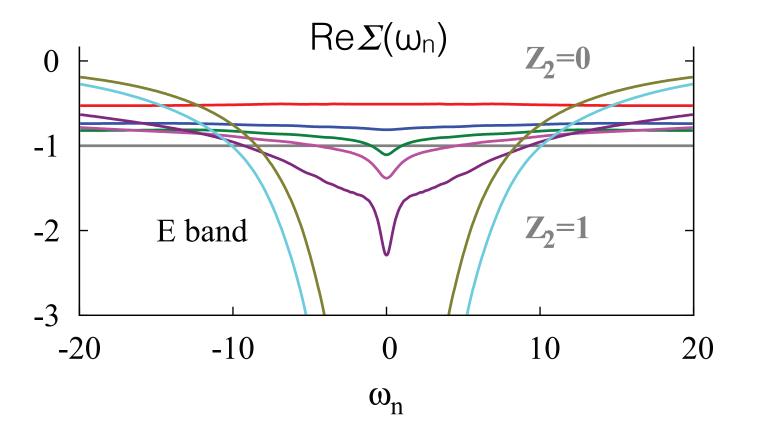


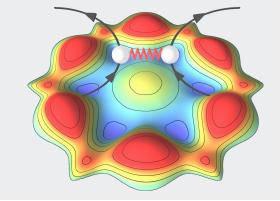
$$\mathcal{H}_{\text{int}}(i) = (U - J) \frac{N_{i}(N_{i} - 1)}{2} - J \left(\frac{N_{i}^{2}}{4} + S_{zi}^{2} - 2T_{zi}^{2} \right)$$





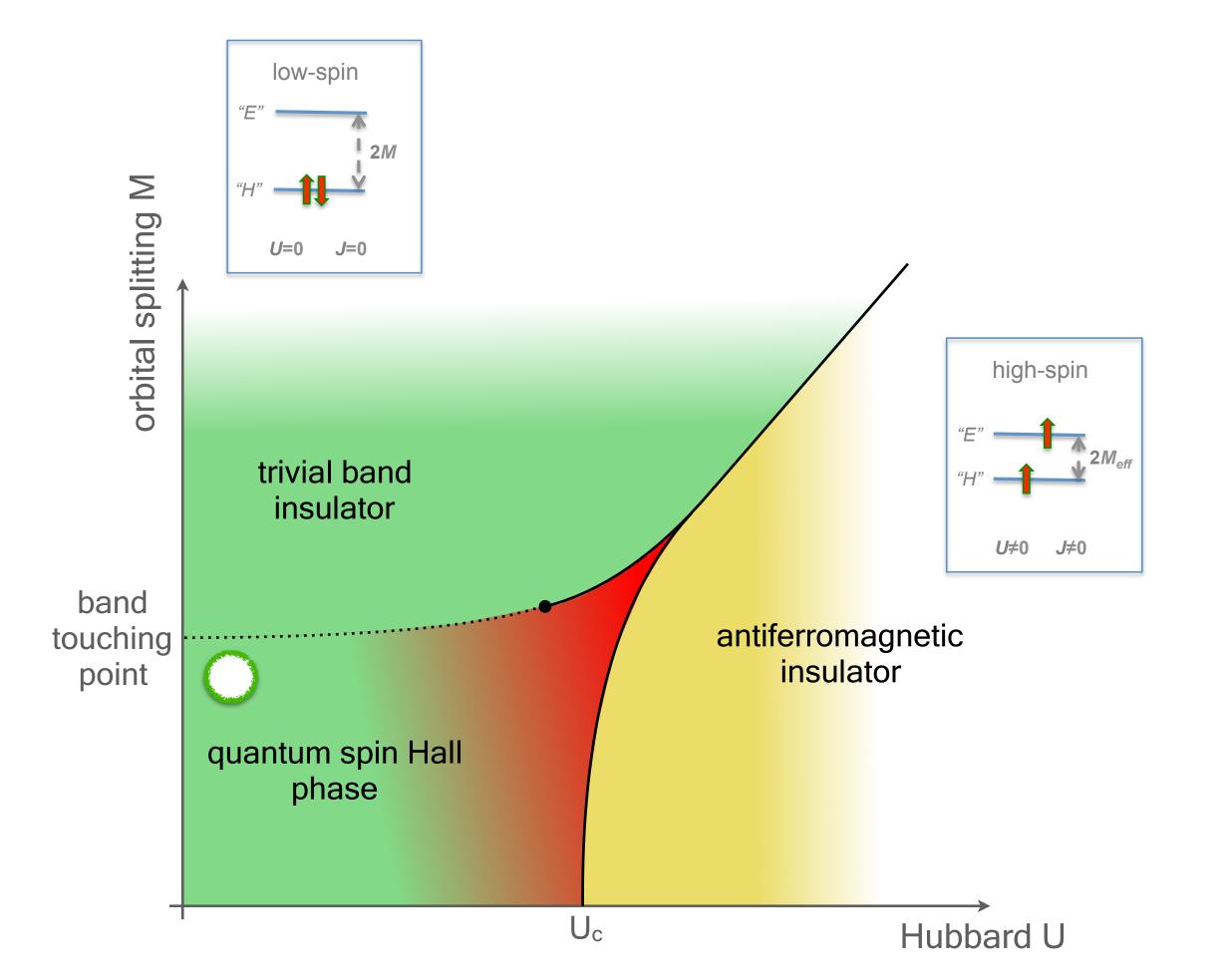
- distinction between flat "Hartree-Fock" and
- pronounced ω-structure of many-body nature



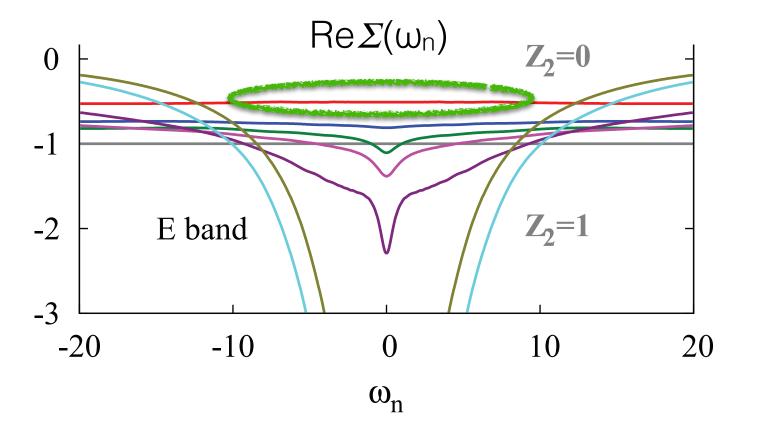


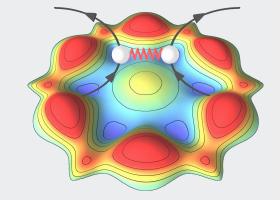
$$\mathcal{H}_{\text{int}}(i) = (U - J) \frac{N_{i}(N_{i} - 1)}{2} - J \left(\frac{N_{i}^{2}}{4} + S_{zi}^{2} - 2T_{zi}^{2} \right)$$

$$\mathcal{H}_{\text{int}}(\mathbf{i}) = (U - J) \frac{N_{\mathbf{i}}(N_{\mathbf{i}} - 1)}{2} - J \left(\frac{N_{\mathbf{i}}^2}{4} + S_{z\mathbf{i}}^2 - 2T_{z\mathbf{i}}^2 \right) \qquad \vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$



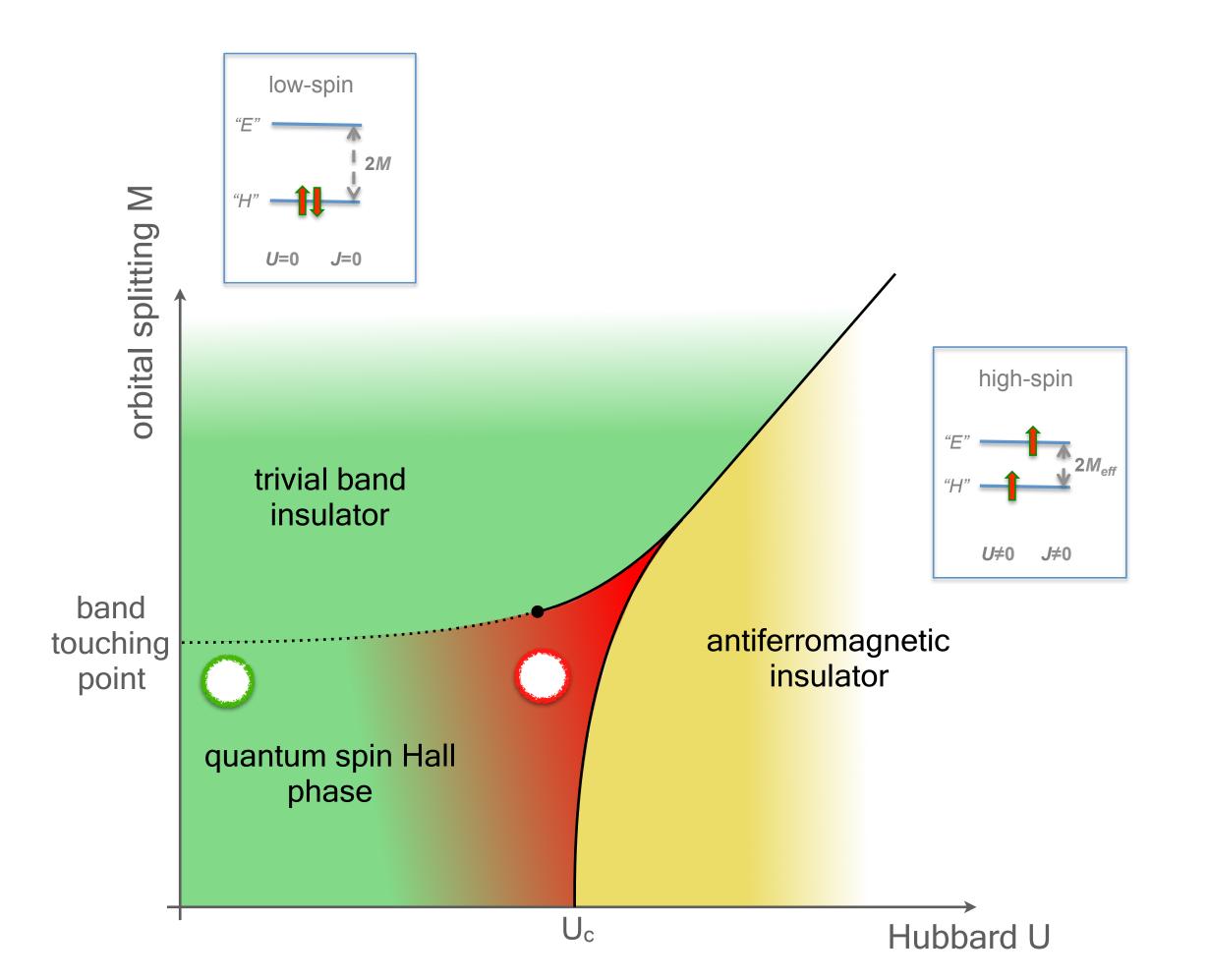
- distinction between flat "Hartree-Fock" and
- pronounced ω-structure of many-body nature





$$\mathcal{H}_{int}(i) = (U - J) \frac{N_i(N_i - 1)}{2} - J \left(\frac{N_i^2}{4} + S_{zi}^2 - 2T_{zi}^2 \right)$$

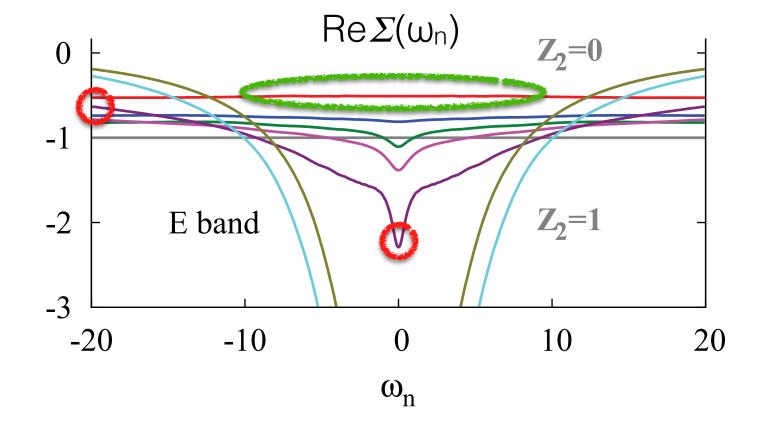
$$\mathcal{H}_{\mathrm{int}}(\mathbf{i}) = (U - J) \frac{N_{\mathbf{i}}(N_{\mathbf{i}} - 1)}{2} - J \left(\frac{N_{\mathbf{i}}^2}{4} + S_{z\mathbf{i}}^2 - 2T_{z\mathbf{i}}^2 \right) \qquad \vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \operatorname{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$

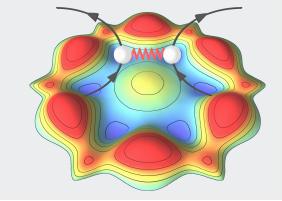


- distinction between flat "Hartree-Fock" and
- pronounced ω-structure of many-body nature



$$|\mathrm{Re}\Sigma(\omega=0)-\mathrm{Re}\Sigma(\omega=\infty)|$$

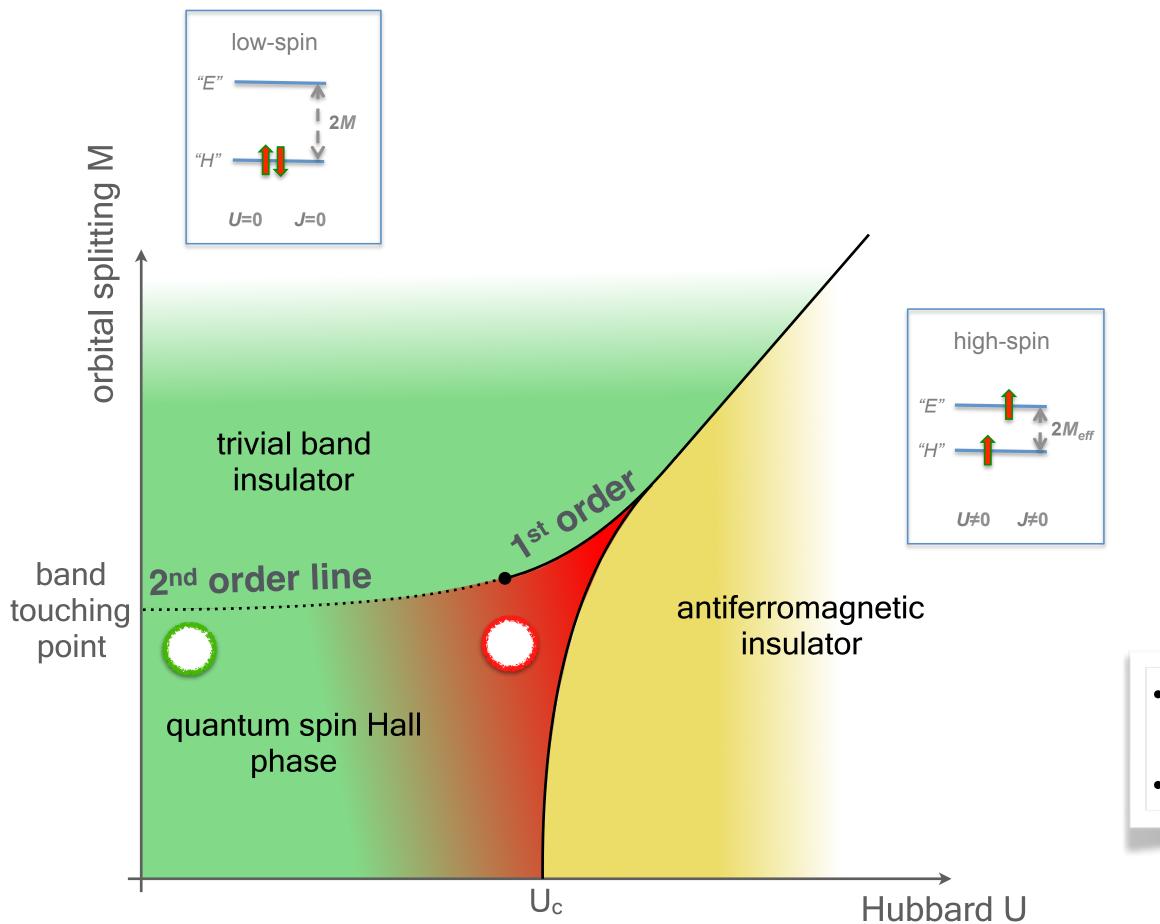




where do the colors come from?

$$\mathcal{H}_{\text{int}}(\mathbf{i}) = (U - J) \frac{N_{\mathbf{i}}(N_{\mathbf{i}} - 1)}{2} - J \left(\frac{N_{\mathbf{i}}^2}{4} + S_{z\mathbf{i}}^2 - 2T_{z\mathbf{i}}^2 \right) \qquad \vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$

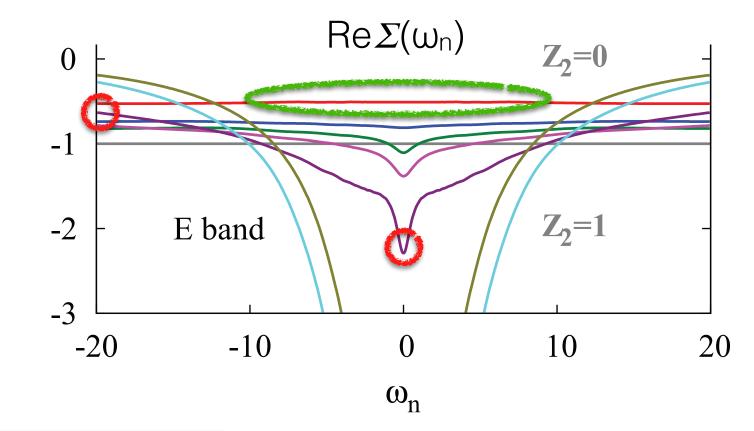
$$\vec{d}(\mathbf{k}) = \begin{pmatrix} \lambda \sin k_x \\ \lambda \sin k_y \\ M - \text{Re}\Sigma(0) - \cos k_x - \cos k_y \end{pmatrix}$$



- distinction between flat "Hartree-Fock" and
- pronounced ω-structure of many-body nature



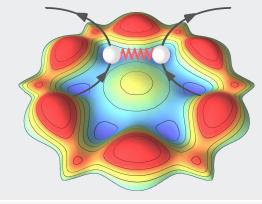
 $|\mathrm{Re}\Sigma(\omega=0)-\mathrm{Re}\Sigma(\omega=\infty)|$



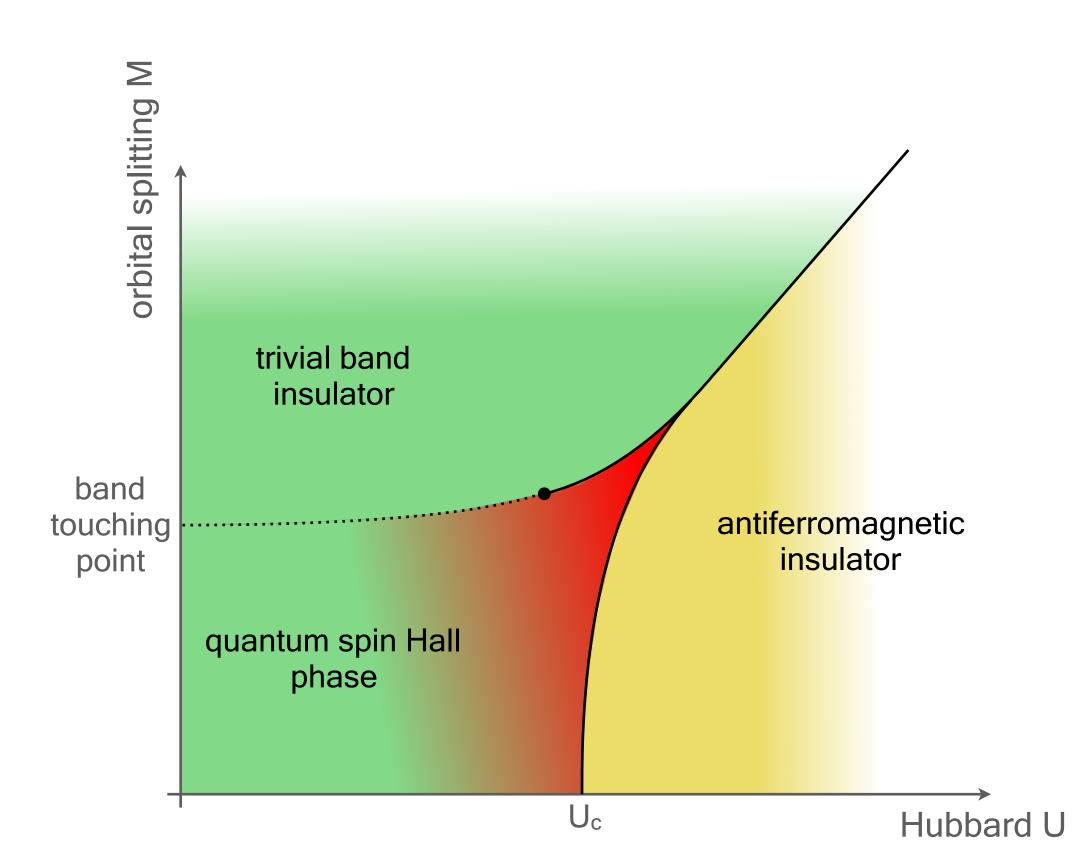
- QSHI and BI no longer smoothly connected
- Gap inversion occurring via a jump

1st-order QSH transition also in Xue&MacDonald PRL (2018)

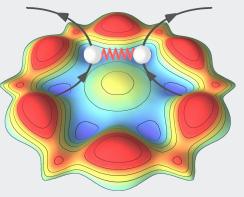




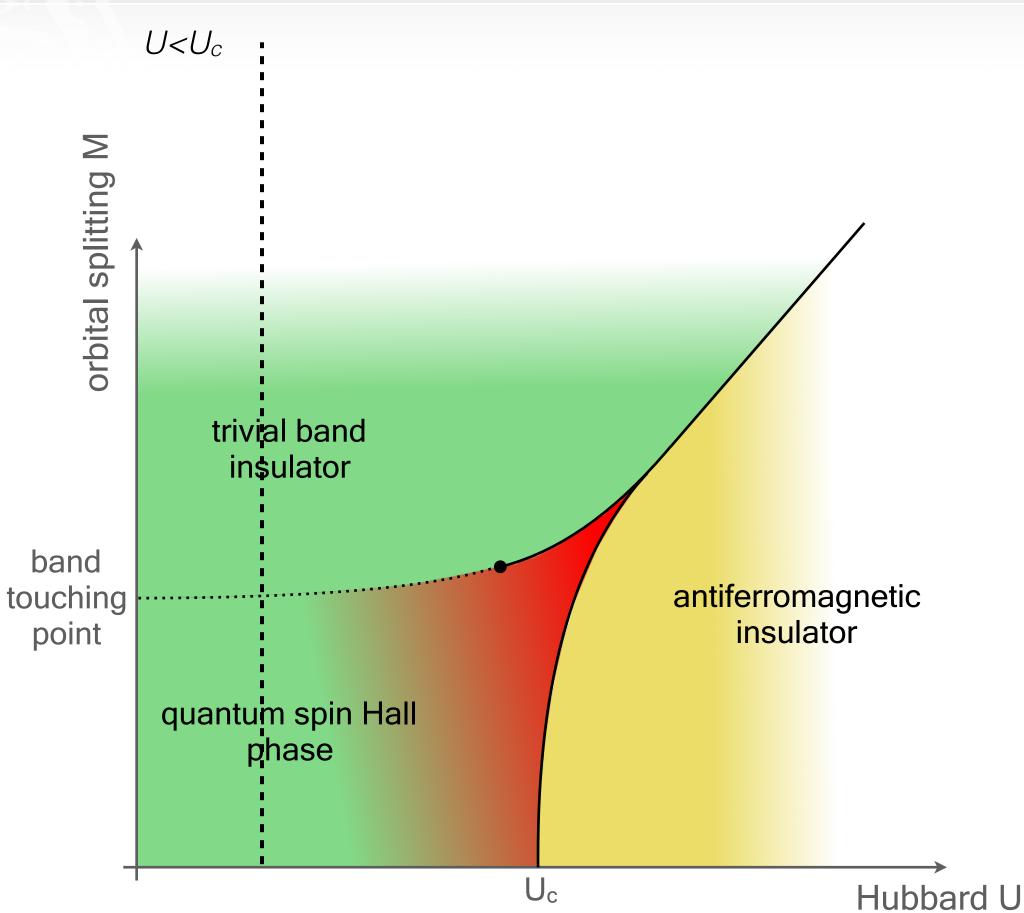
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description



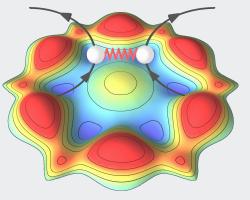




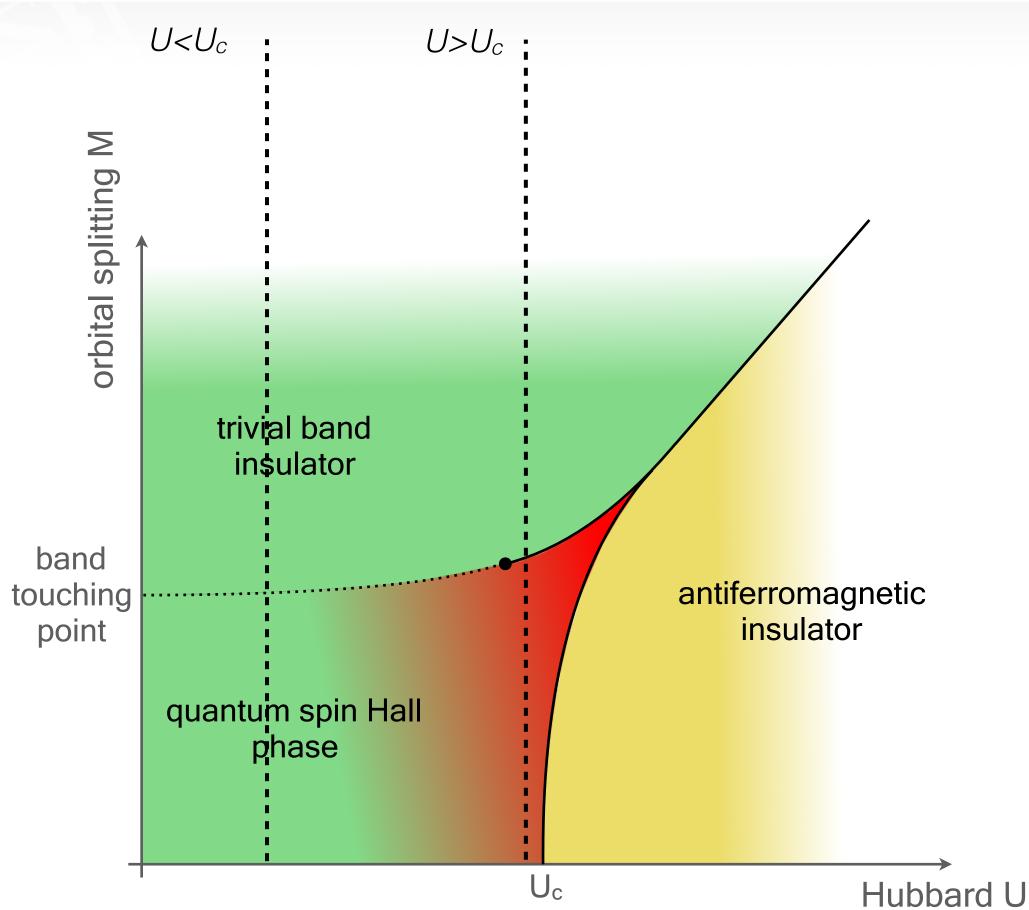
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description



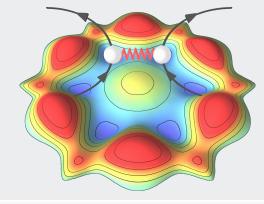




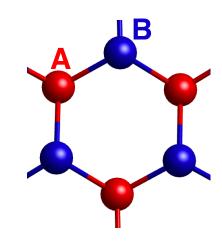
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description

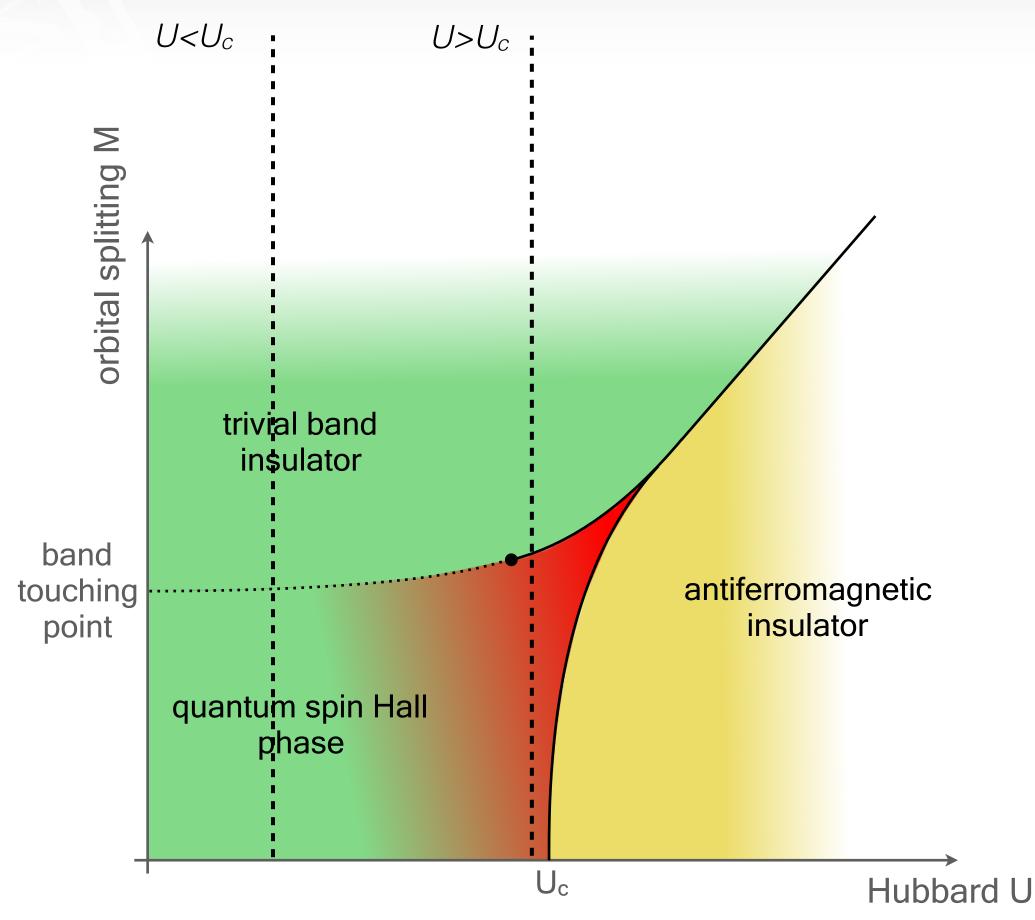






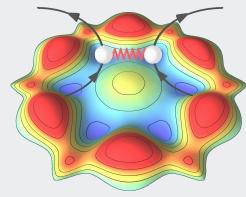
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description
- analogy with the Kane-Mele-Hubbard and Haldane-Hubbard models



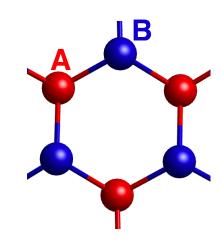


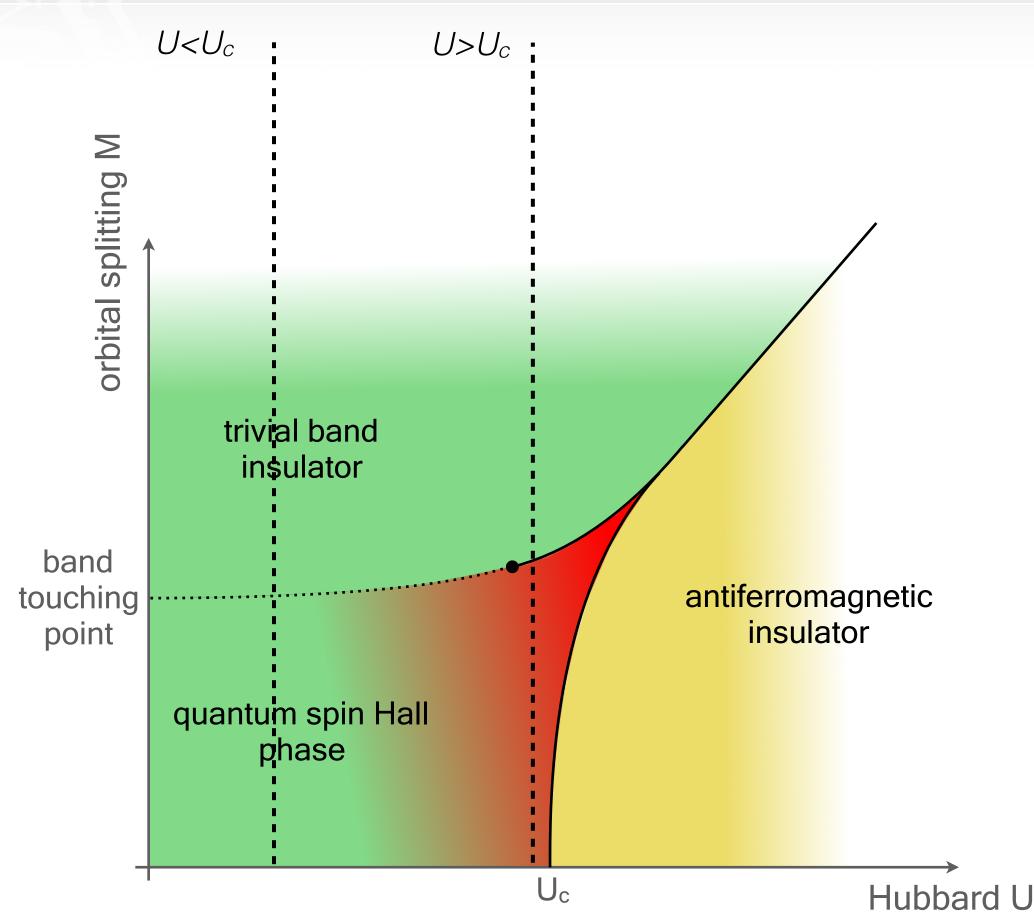
$$H = t \sum_{\langle ij \rangle, \alpha} c_{i,\alpha}^{\dagger} c_{j,\alpha} + i \lambda_{SO} \sum_{\langle \langle ij \rangle \rangle, \alpha\alpha'} \nu_{ij} c_{i,\alpha}^{\dagger} s_{\alpha\alpha'}^{z} c_{j,\alpha'} + i \lambda_{R} \sum_{\langle ij \rangle, \alpha\alpha'} c_{i,\alpha}^{\dagger} (\mathbf{s} \times \hat{\mathbf{d}}_{ij})_{\alpha\alpha'}^{z} c_{j,\alpha'}$$





- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description
- analogy with the Kane-Mele-Hubbard and Haldane-Hubbard models

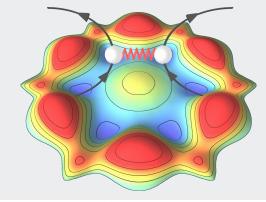




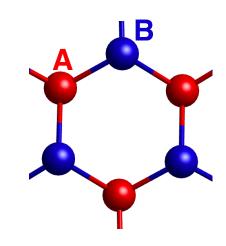
A/B splitting

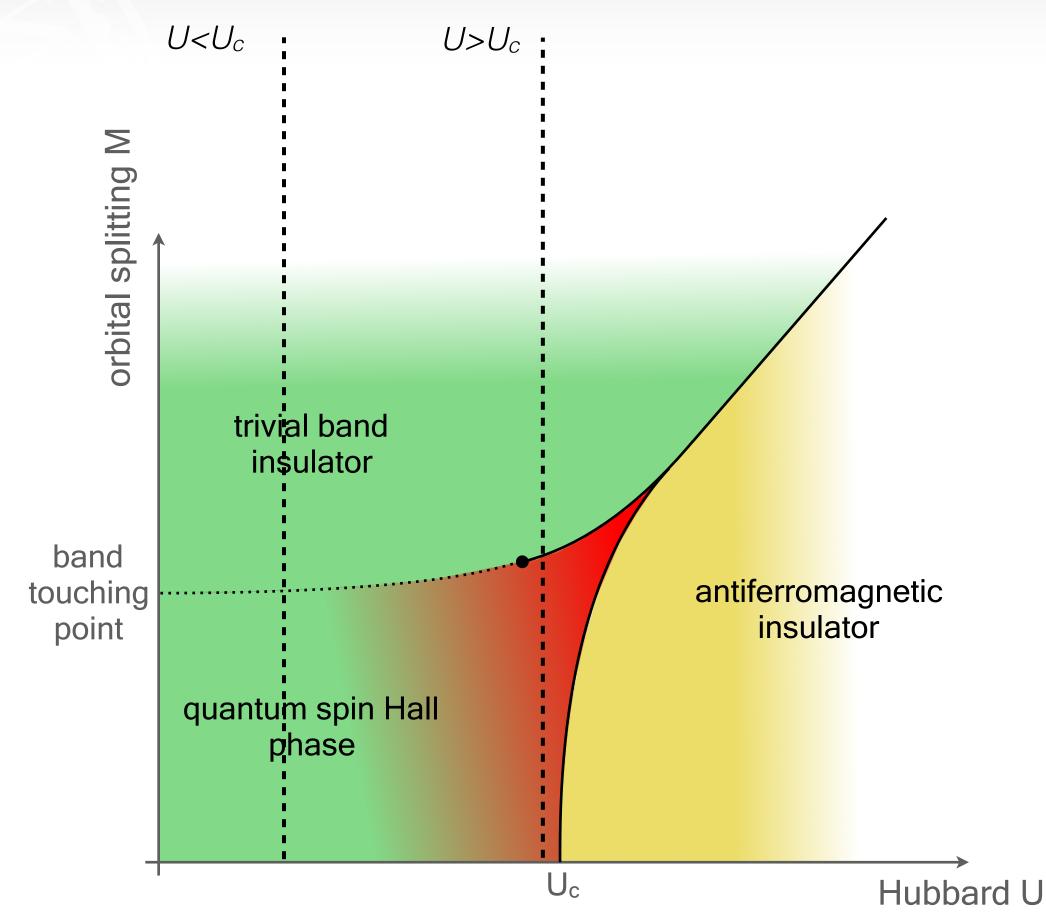
$$H = t \sum_{\langle ij \rangle, \alpha} c^{\dagger}_{i,\alpha} c_{j,\alpha} + i \lambda_{\text{SO}} \sum_{\langle \langle ij \rangle \rangle, \alpha\alpha'} \nu_{ij} c^{\dagger}_{i,\alpha} s^{z}_{\alpha\alpha'} c_{j,\alpha'} + i \lambda_{R} \sum_{\langle ij \rangle, \alpha\alpha'} c^{\dagger}_{i,\alpha} (\mathbf{s} \times \hat{\mathbf{d}}_{ij})^{z}_{\alpha\alpha'} c_{j,\alpha'} + \mathbf{M} \sum_{i,\alpha}^{\mathsf{A,B}} \xi_{i} c^{\dagger}_{i,\alpha} c_{i,\alpha}$$



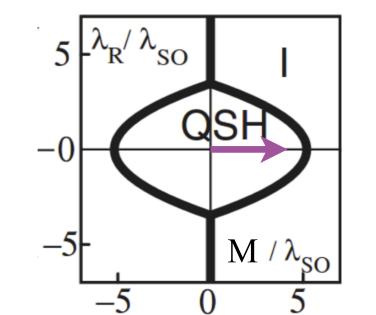


- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description
- analogy with the Kane-Mele-Hubbard and Haldane-Hubbard models



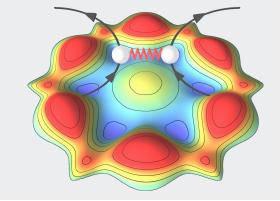


$$H = t \sum_{\langle ij \rangle, \alpha} c^{\dagger}_{i,\alpha} c_{j,\alpha} + i \lambda_{\text{SO}} \sum_{\langle \langle ij \rangle \rangle, \alpha\alpha'} \nu_{ij} c^{\dagger}_{i,\alpha} s^{z}_{\alpha\alpha'} c_{j,\alpha'} + i \lambda_{R} \sum_{\langle ij \rangle, \alpha\alpha'} c^{\dagger}_{i,\alpha} (\mathbf{s} \times \hat{\mathbf{d}}_{ij})^{z}_{\alpha\alpha'} c_{j,\alpha'} + \mathbf{M} \sum_{i,\alpha}^{\mathsf{A, B}} \xi_{i} c^{\dagger}_{i,\alpha} c_{i,\alpha}$$



C. Kane & E. Mele, PRL (2005)

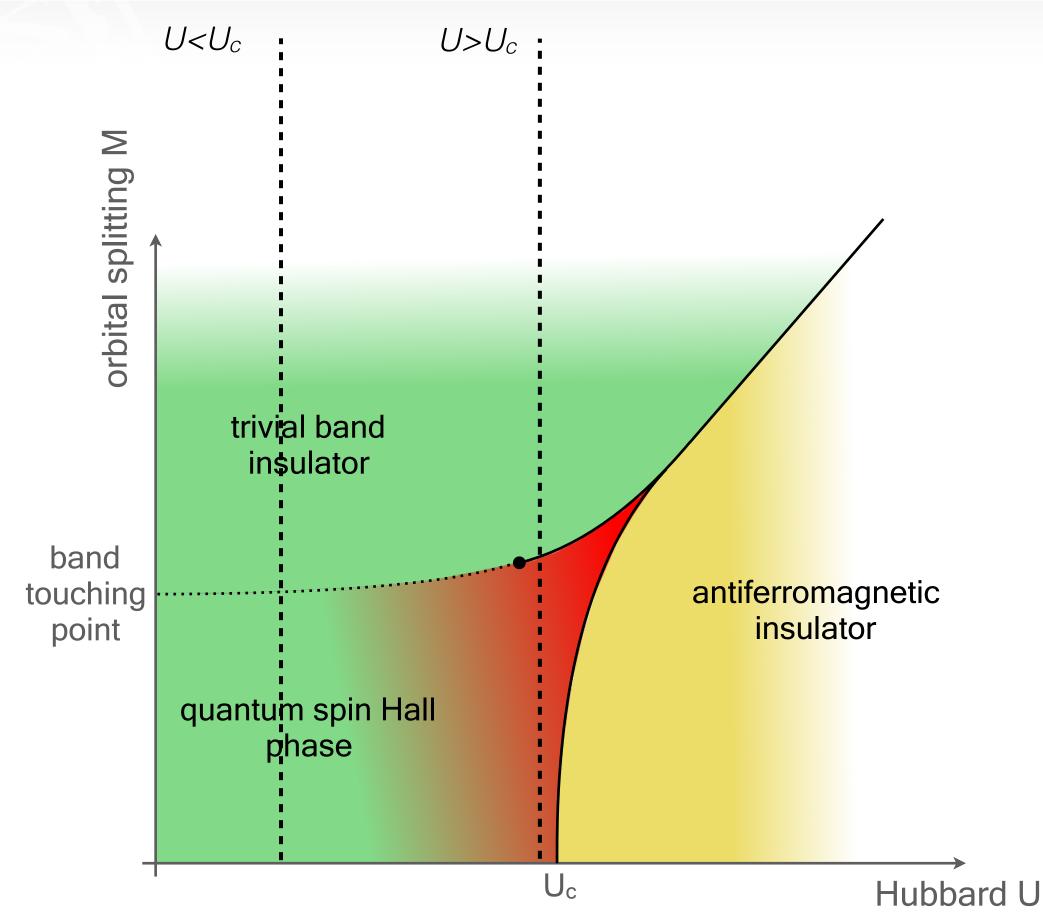




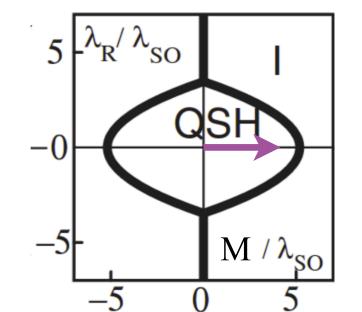
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description
- analogy with the Kane-Mele-Hubbard and Haldane-Hubbard models

interaction term in this case: $U\sum n_{i,\uparrow}n_{i,\downarrow}$

simpler "single-orbital"



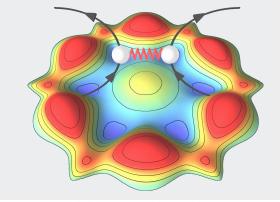
$$H = t \sum_{\langle ij \rangle, \alpha} c^{\dagger}_{i,\alpha} c_{j,\alpha} + i \lambda_{\text{SO}} \sum_{\langle \langle ij \rangle \rangle, \alpha\alpha'} \nu_{ij} c^{\dagger}_{i,\alpha} s^{z}_{\alpha\alpha'} c_{j,\alpha'} + i \lambda_{R} \sum_{\langle ij \rangle, \alpha\alpha'} c^{\dagger}_{i,\alpha} (\mathbf{s} \times \hat{\mathbf{d}}_{ij})^{z}_{\alpha\alpha'} c_{j,\alpha'} + \mathbf{M} \sum_{i,\alpha}^{\mathbf{A}, \mathbf{B}} \xi_{i} c^{\dagger}_{i,\alpha} c_{i,\alpha}$$



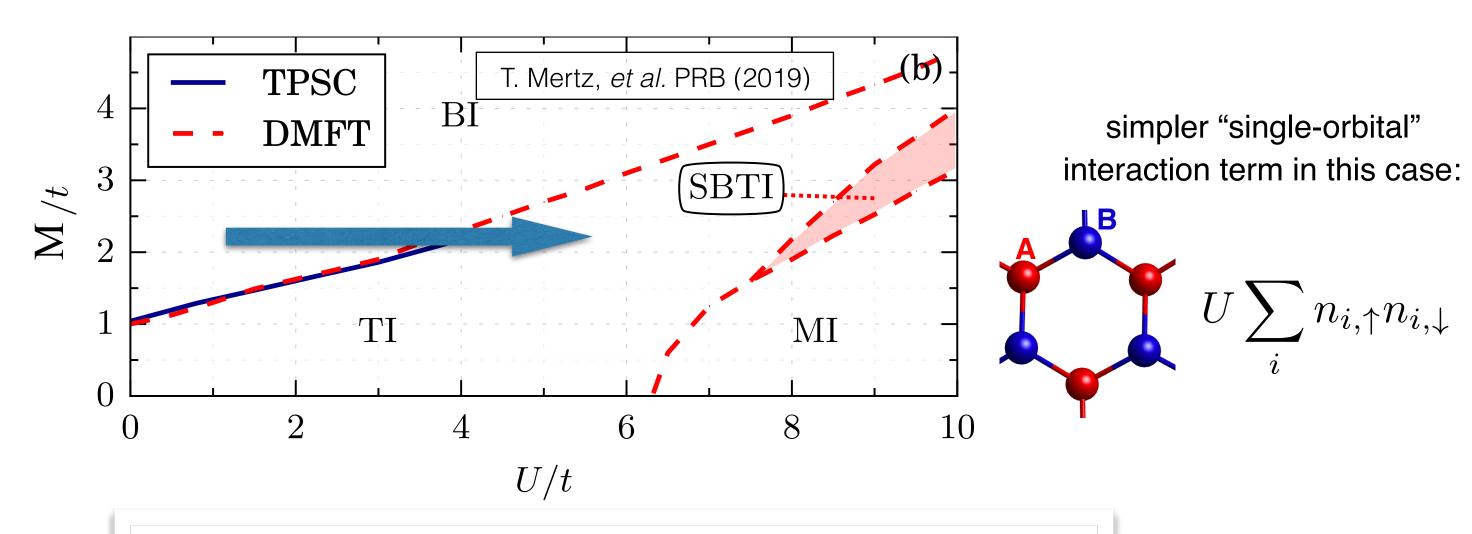
A/B splitting

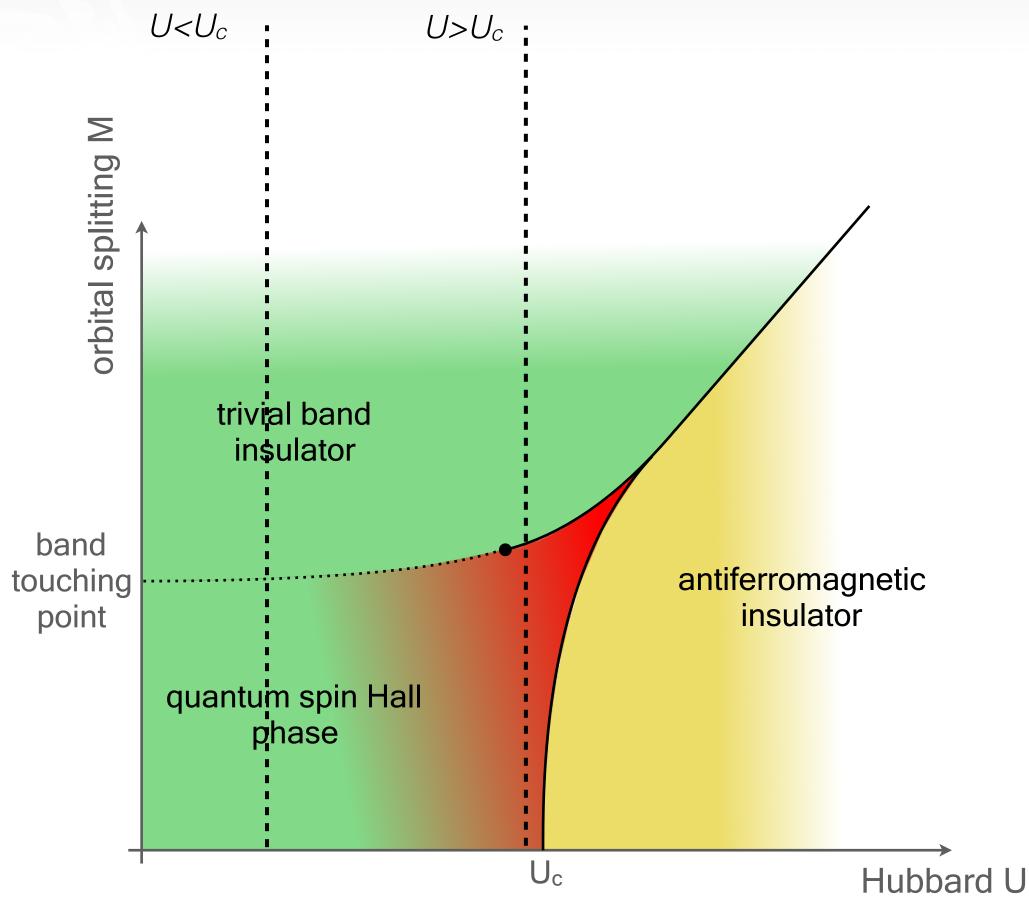
C. Kane & E. Mele, PRL (2005)





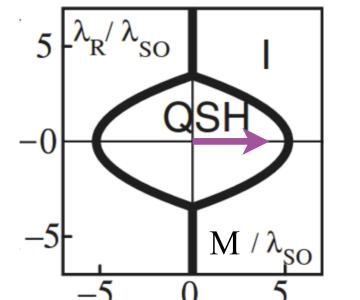
- gap closing: for $U < U_c$ smooth topological phase transition (green \rightarrow green)
- no semimetal for $U>U_c$ when the \mathbb{Z}_2 topological invariant changes (green \rightarrow red)!
- new termodynamics, beyond single-particle effective description
- analogy with the Kane-Mele-Hubbard and Haldane-Hubbard models





suppression of staggered potential and U-driven TI phase

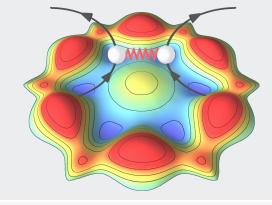
$$H = t \sum_{\langle ij \rangle, \alpha} c^{\dagger}_{i,\alpha} c_{j,\alpha} + i \lambda_{\text{SO}} \sum_{\langle \langle ij \rangle \rangle, \alpha\alpha'} \nu_{ij} c^{\dagger}_{i,\alpha} s^{z}_{\alpha\alpha'} c_{j,\alpha'} + i \lambda_{R} \sum_{\langle ij \rangle, \alpha\alpha'} c^{\dagger}_{i,\alpha} (\mathbf{s} \times \hat{\mathbf{d}}_{ij})^{z}_{\alpha\alpha'} c_{j,\alpha'} + \mathbf{M} \sum_{i,\alpha}^{\mathbf{A}, \mathbf{B}} \xi_{i} c^{\dagger}_{i,\alpha} c_{i,\alpha}$$



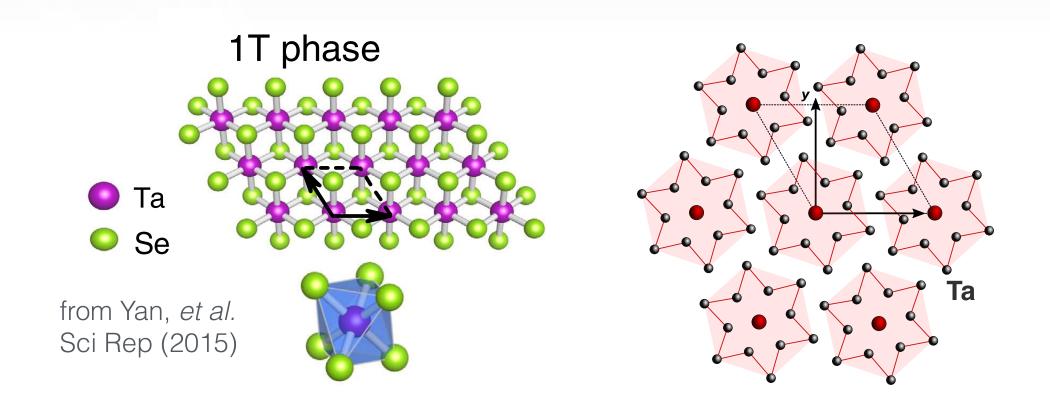
A/B splitting

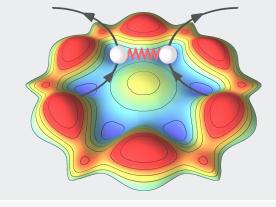
C. Kane & E. Mele, PRL (2005)



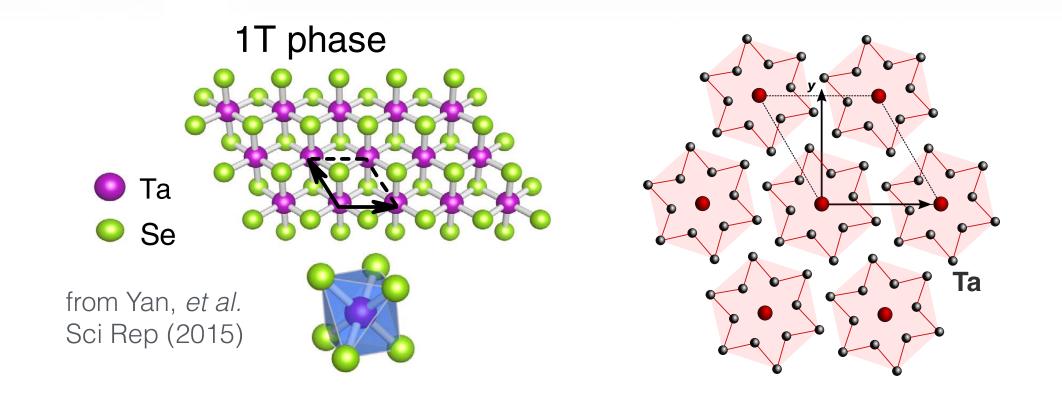


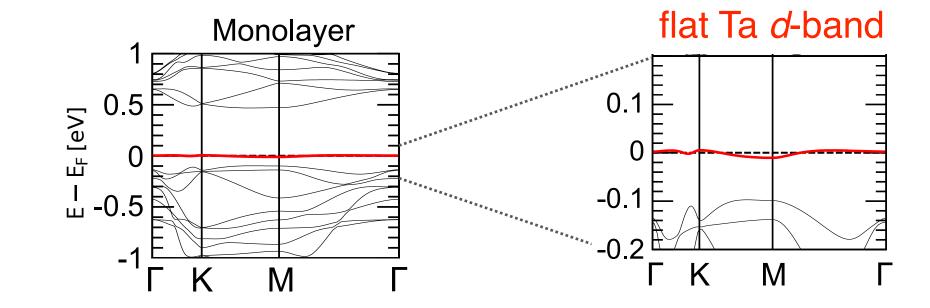
- TaSe₂ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome)
 + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" √13 x √13 CDW reconstructions

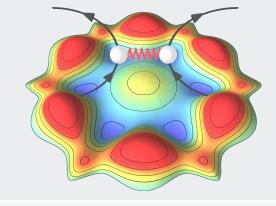




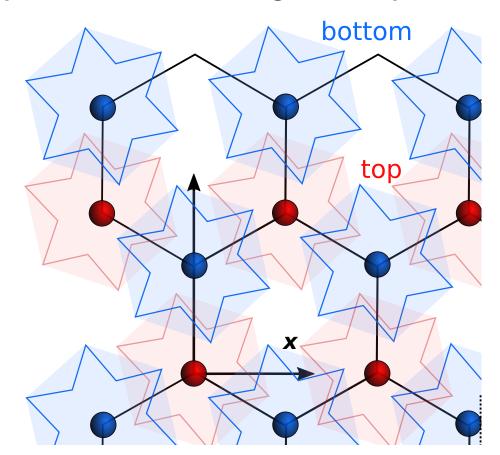
- TaSe₂ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome) + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" √13 x √13 CDW reconstructions

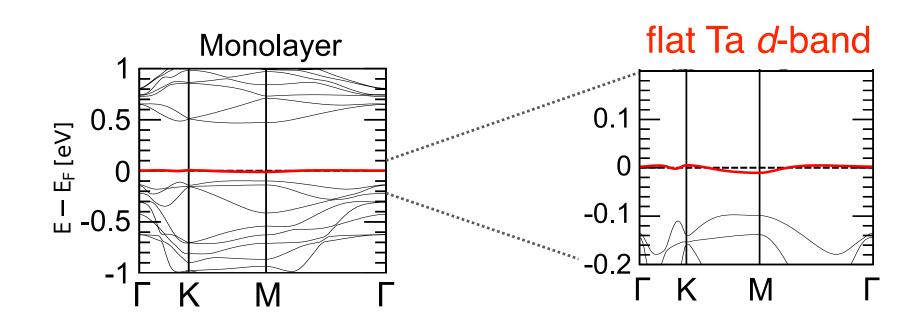


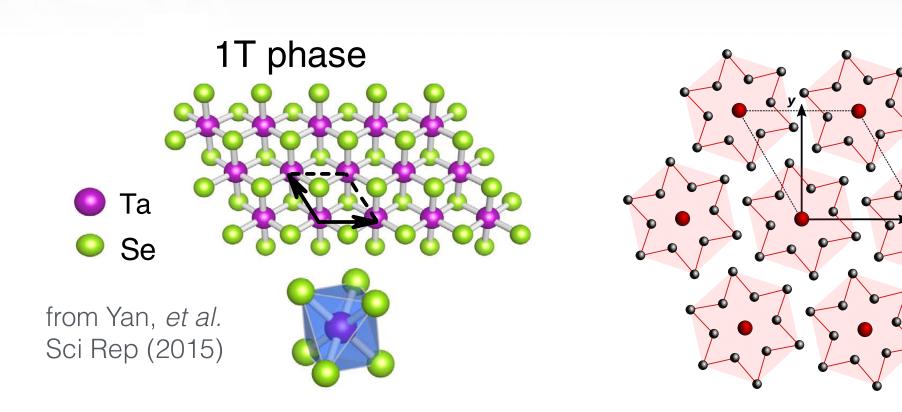


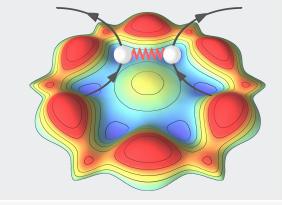


- TaSe₂ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome) + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" √13 x √13 CDW reconstructions
- bilayer: shifted triangular layers → buckled honeycomb!

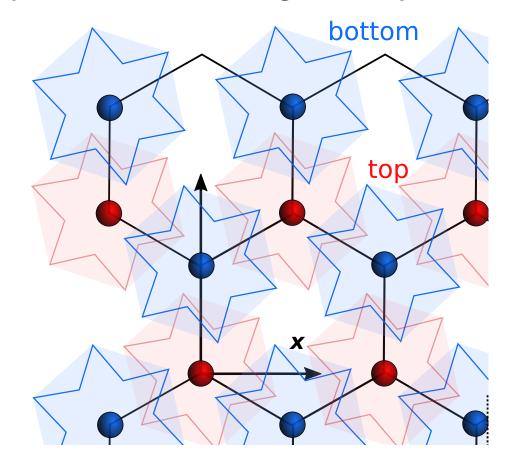


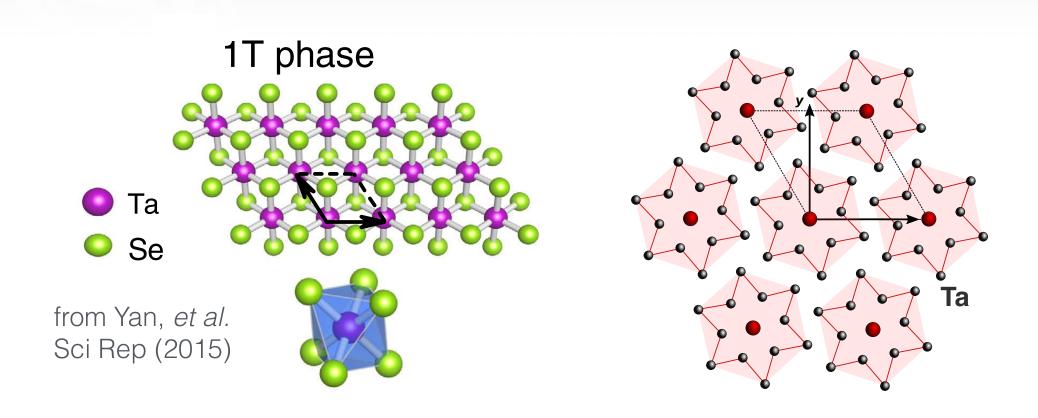




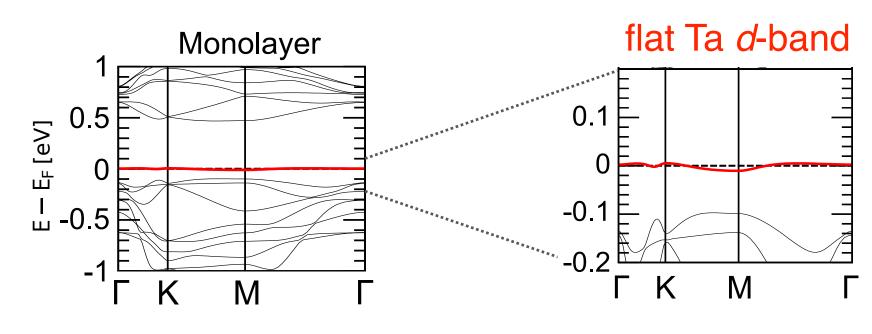


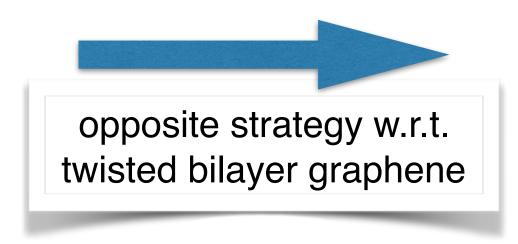
- TaSe₂ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome) + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" √13 × √13 CDW reconstructions
- bilayer: shifted triangular layers ⇒ buckled honeycomb!

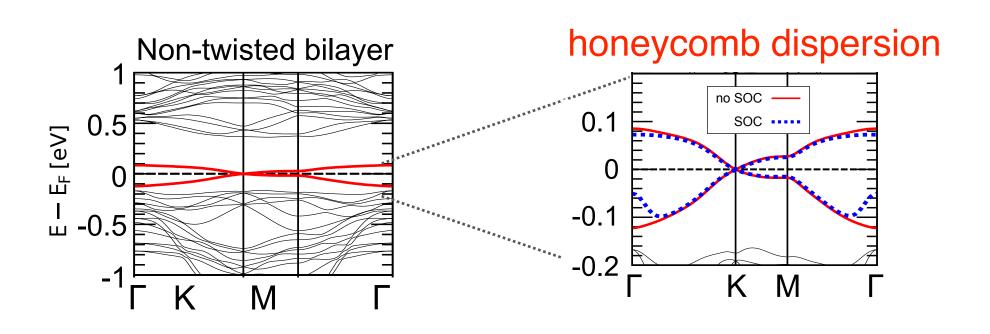


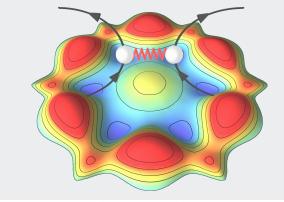


"deconfinement" of Mott localized electrons into correlated Dirac fermions

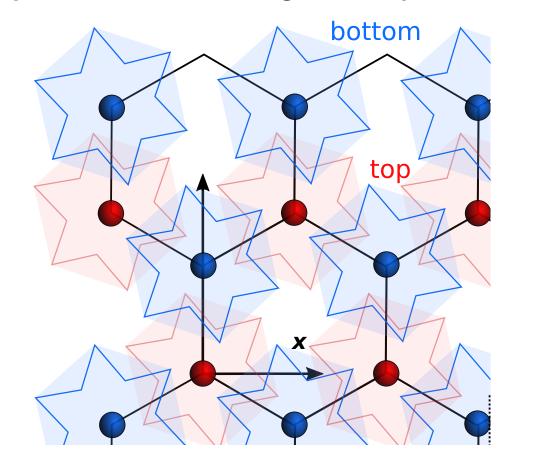


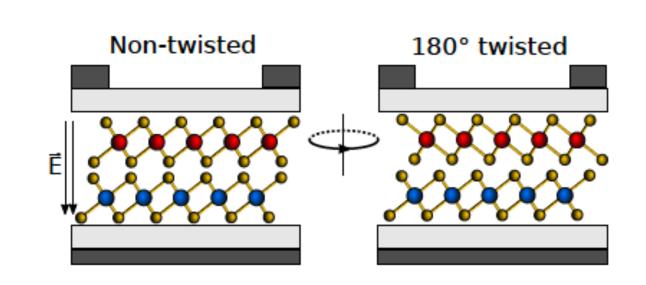


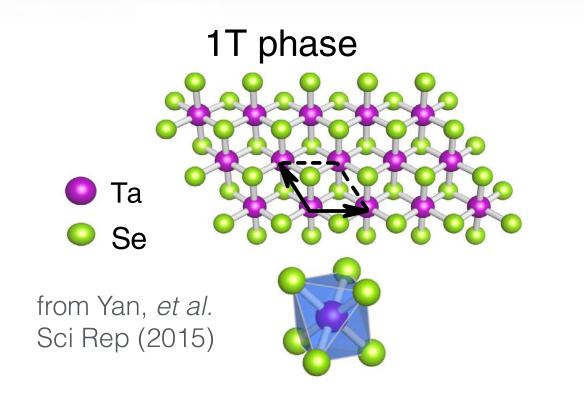


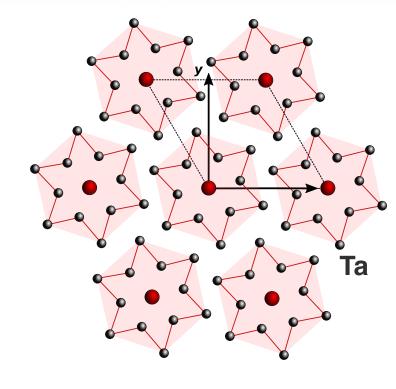


- TaSe₂ [arXiv:2001.04102] in cooperation with S. Adler, P. Barone (Rome) + group of R. Valentí (Frankfurt) and J. M. Pizarro and T. Wehling (Bremen)
- 1T-monolayer: "star-of-David" √13 × √13 CDW reconstructions
- bilayer: shifted triangular layers ⇒ buckled honeycomb!

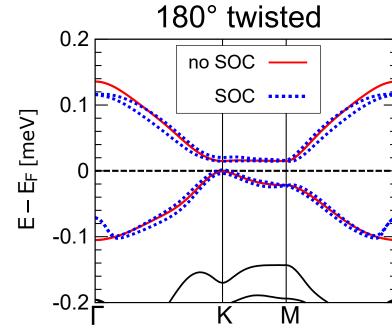




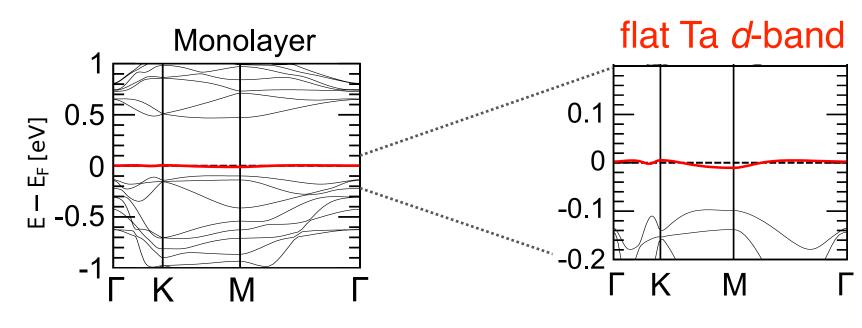


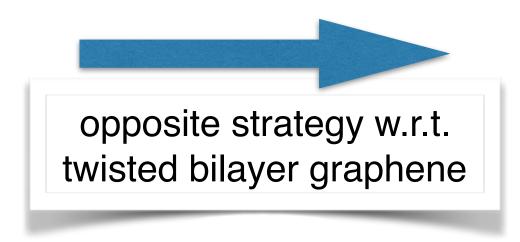


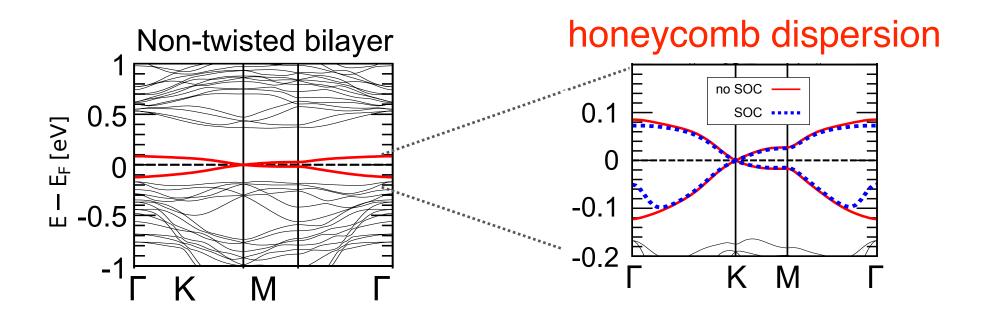
 twisting breaks inversion symmetry and opens a gap



"deconfinement" of Mott localized electrons into correlated Dirac fermions

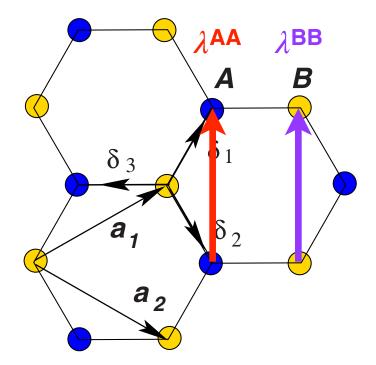


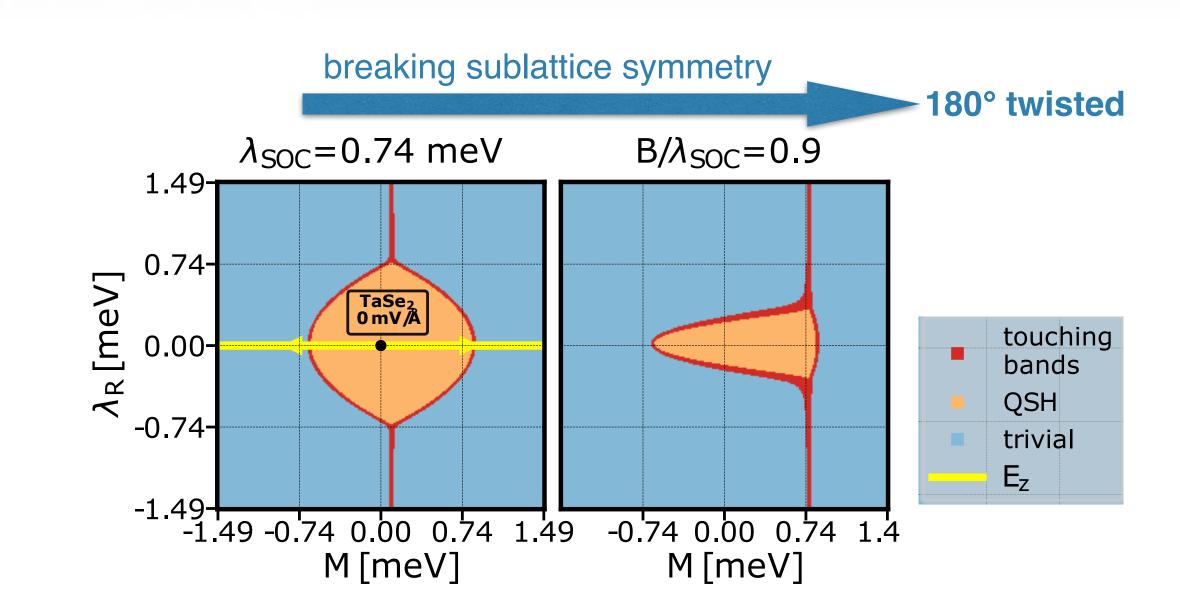




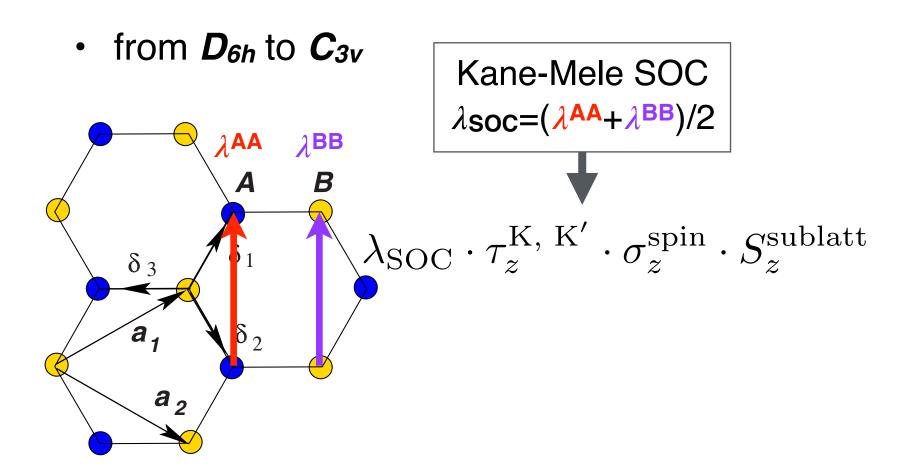


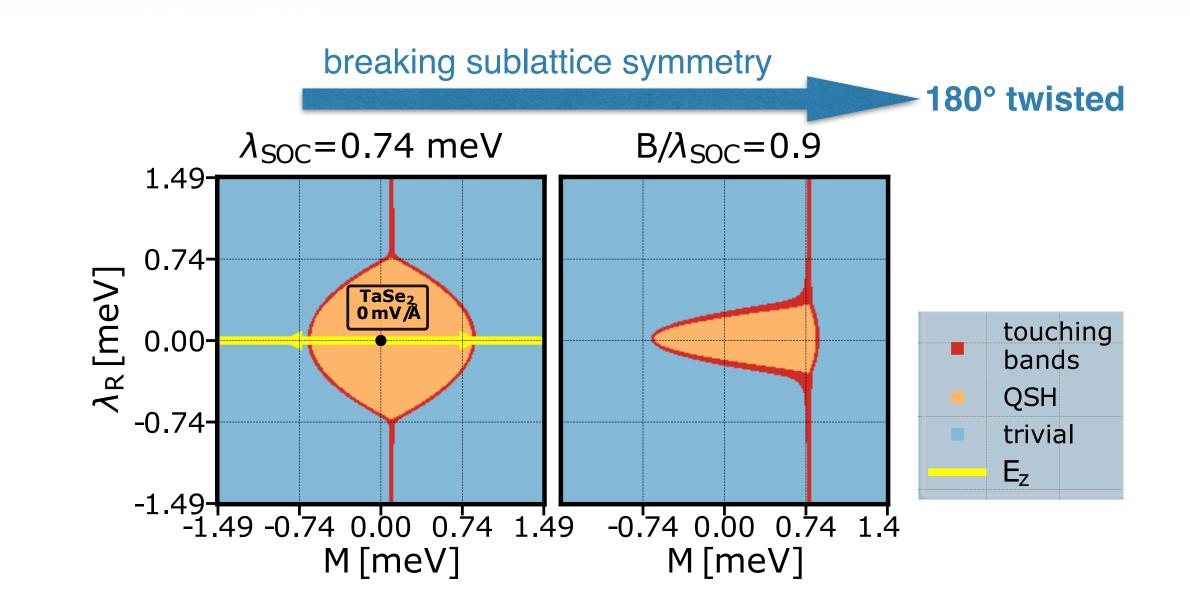
- we can tune M by means of electric field along $z (\sim 1-4 \text{ meV/Å})$
- from D_{6h} to C_{3v}



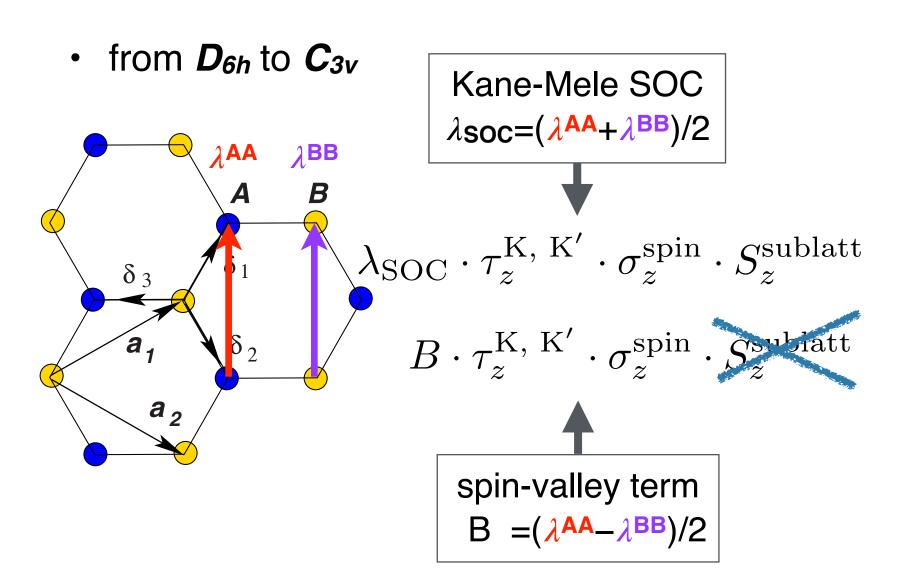


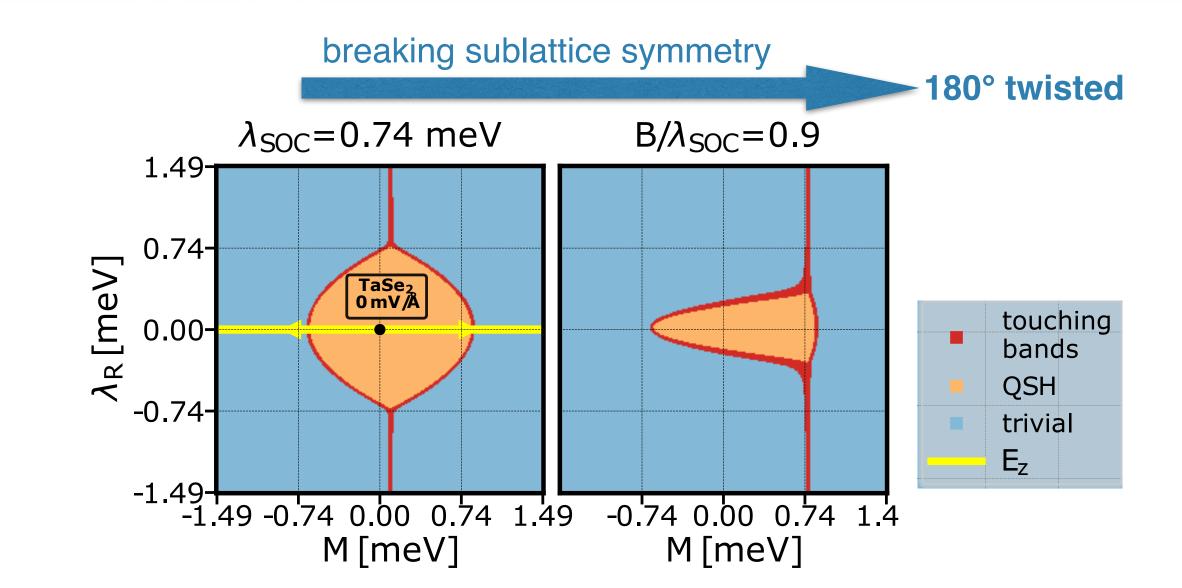
• we can tune M by means of electric field along $z (\sim 1-4 \text{ meV/Å})$



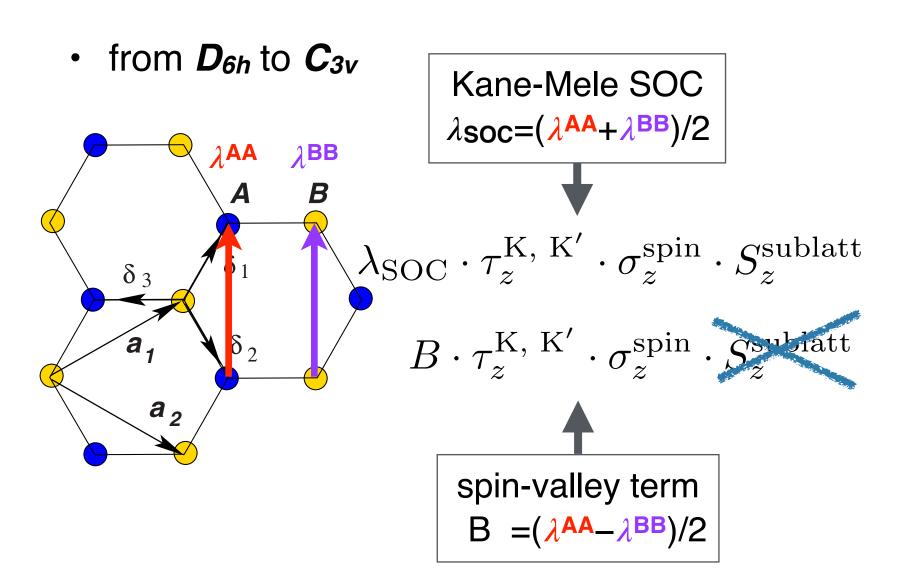


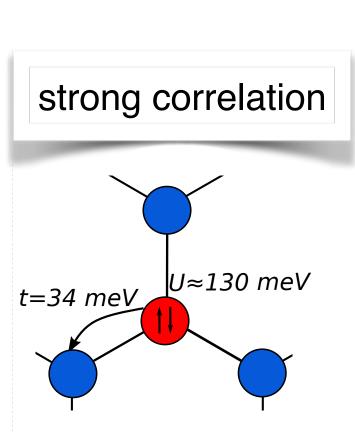
• we can tune M by means of electric field along $z (\sim 1-4 \text{ meV/Å})$

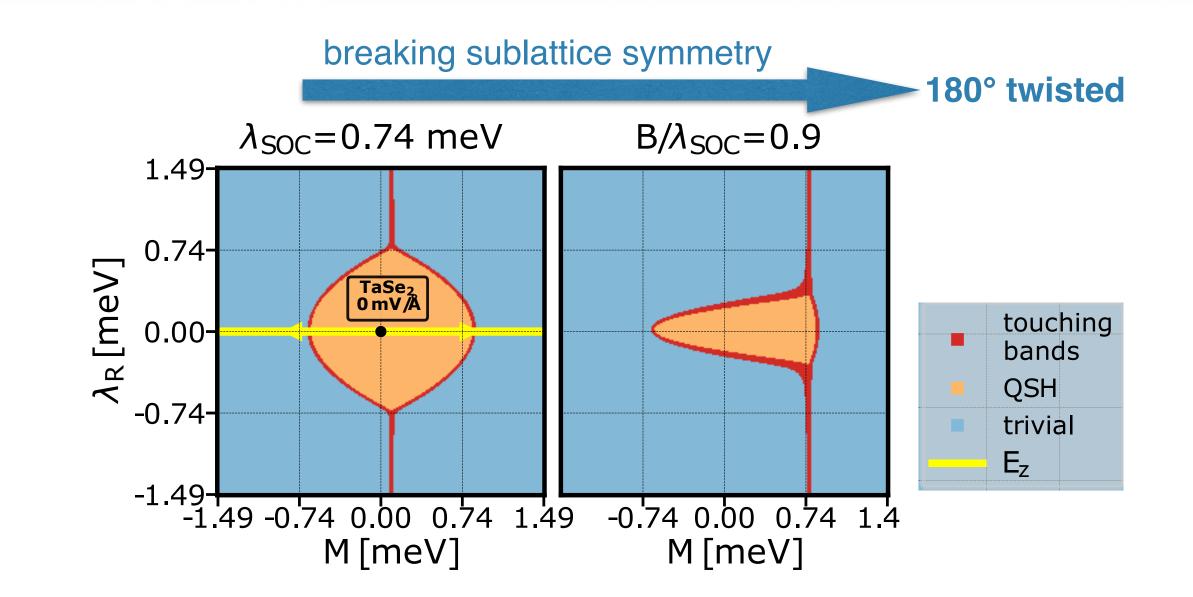




• we can tune M by means of electric field along $z (\sim 1-4 \text{ meV/Å})$

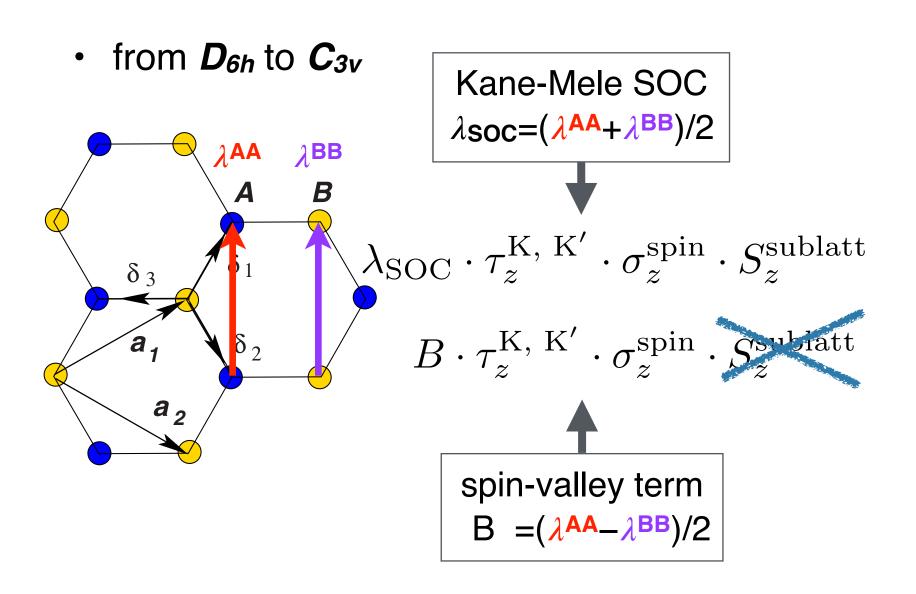


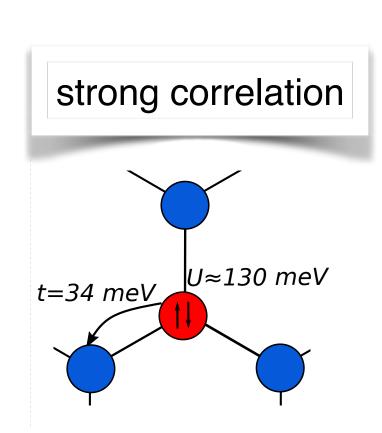


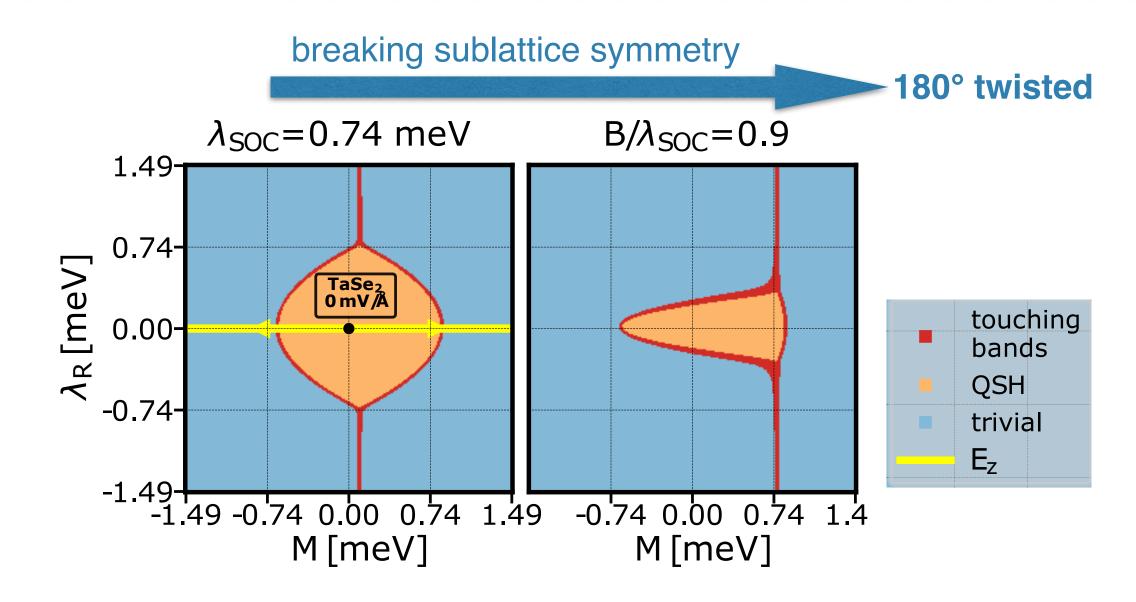




• we can tune M by means of electric field along $z (\sim 1-4 \text{ meV/Å})$



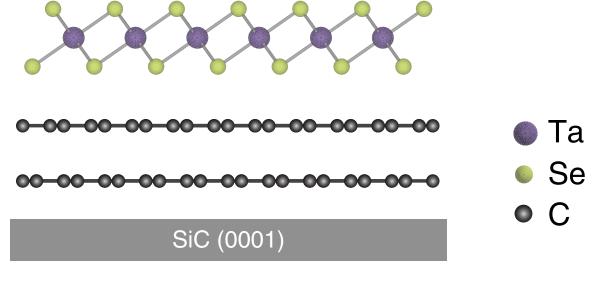




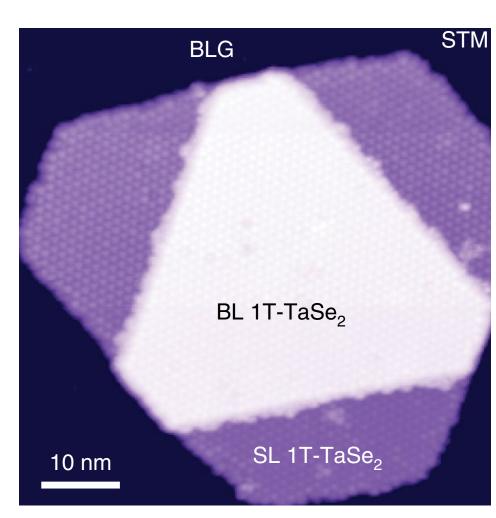
Side view

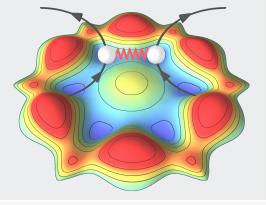
Strong correlations and orbital texture in single-layer 1T-TaSe₂

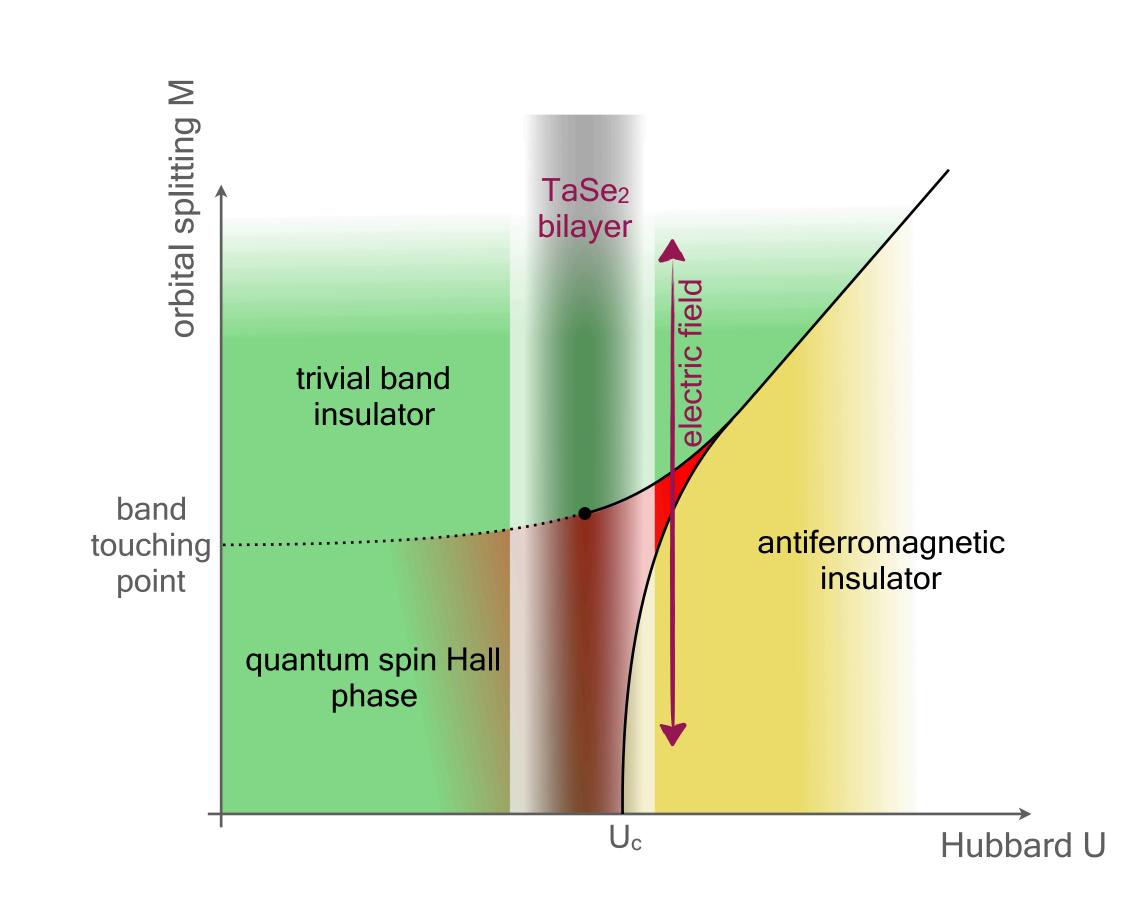
Yi Chen D^{1,2,13}, Wei Ruan^{1,2,13}, Meng Wu^{1,2,13}, Shujie Tang D^{3,4,5,6,7,13}, Hyejin Ryu^{5,8}, Hsin-Zon Tsai^{1,9}, Ryan Lee¹, Salman Kahn¹, Franklin Liou¹, Caihong Jia^{1,2,10}, Oliver R. Albertini¹¹, Hongyu Xiong D^{3,4}, Tao Jia^{3,4}, Zhi Liu D⁶, Jonathan A. Sobota D^{3,5}, Amy Y. Liu¹¹, Joel E. Moore^{1,2}, Zhi-Xun Shen D^{3,4}, Steven G. Louie D^{1,2}, Sung-Kwan Mo D⁵ and Michael F. Crommie D^{1,2,12*}

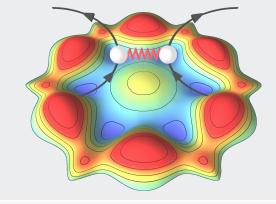




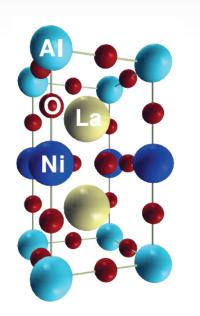


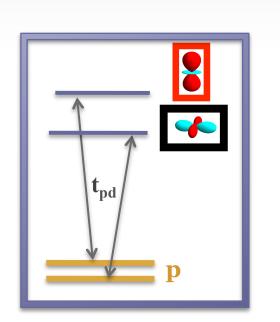


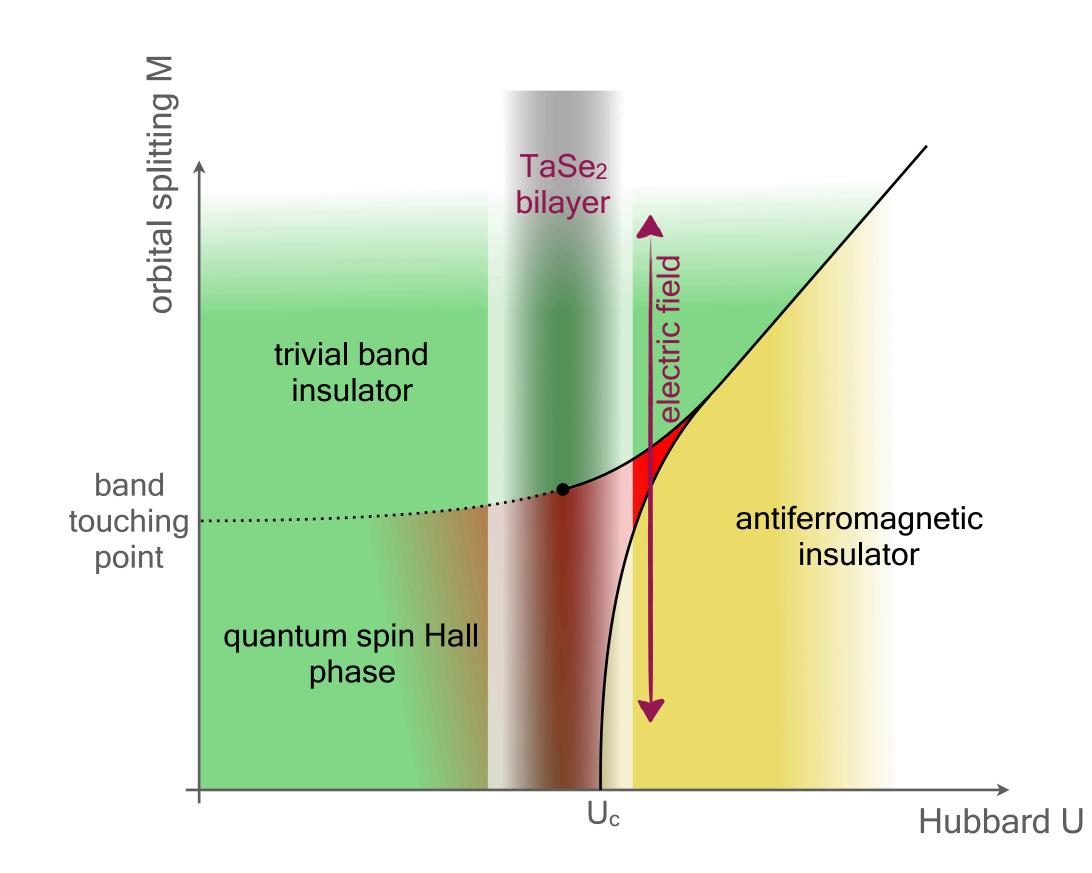




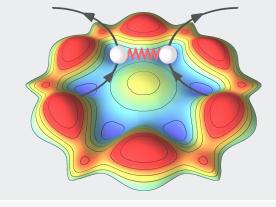
many-body correction to the orbital splitting: either favoring or opposing the bare tendency





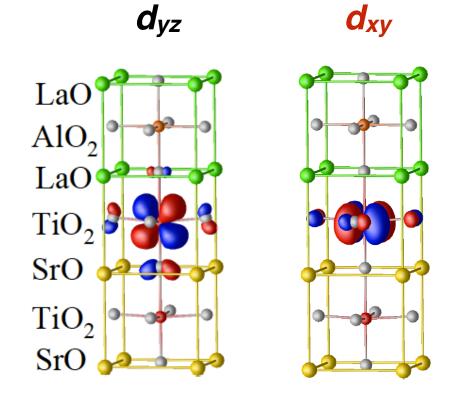




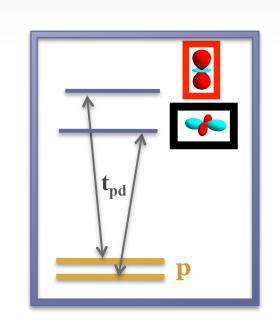


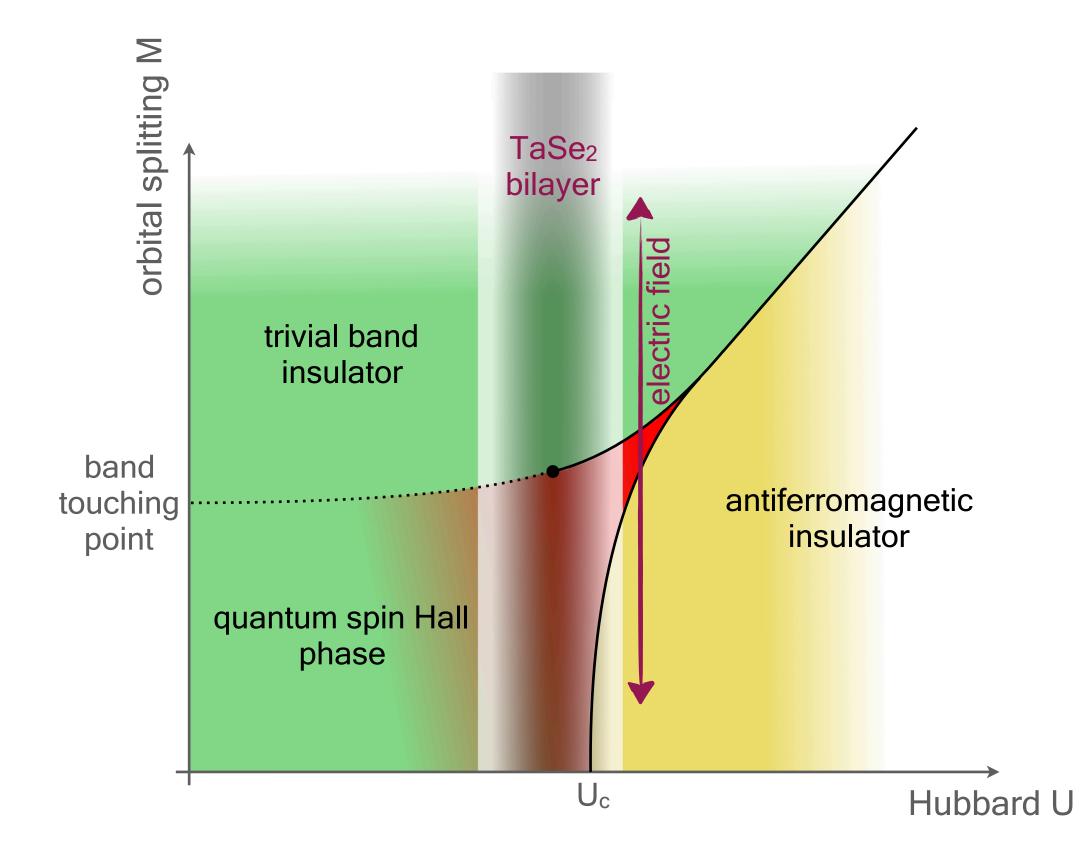
• many-body correction to the orbital splitting: either favoring or opposing the bare tendency

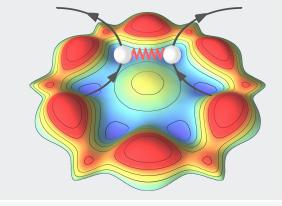
 thickness-induced metal-insulator transition in oxide heterostructures











• many-body correction to the orbital splitting: either favoring or opposing the bare tendency

 thickness-induced metal-insulator transition in oxide heterostructures

 local criticality of orbital fluctuations in correlated topological insulators

 possible material realization and tuning in transition-metal dichalcogenides

